SPIN is the world's most popular, and arguably one of the world's most powerful, tools for detecting software defects in concurrent system designs. Literally thousands of people have used SPIN since it was first introduced almost fifteen years ago. The tool has been applied to everything from the verification of complex call processing software that is used in telephone exchanges, to the validation of intricate control software for interplanetary spacecraft.

This is the most comprehensive reference guide to SPIN, written by the principal designer of the tool. It covers the tool's specification language and theoretical foundation, and gives detailed advice on methods for tackling the most complex software verification problems.

• Design and verify both abstract and detailed verification models of complex systems software

• Develop a solid understanding of the theory behind logic model checking

• Become an expert user of the SPIN command line interface, the Xspin graphical user interface, and the TimeLine editing tool

• Learn the basic theory of omega automata, linear temporal logic, depth-first and breadth-first search, search optimization, and model extraction from source code

The SPIN software was awarded the prestigious Software System Award by the Association for Computing Machinery (ACM), which previously recognized systems such as UNIX, SmallTalk, TCP/IP, Tcl/Tk, and the World Wide Web.
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Preface

"If you don't know where you're going, it doesn't really matter which path you take."

—(Lewis Carroll, 1832–1898)

"You got to be careful if you don't know where you're going, because you might not get there."

—(Yogi Berra, 1925–)

"The worst thing about new books is that they keep us from reading the old ones."

—(Joseph Joubert, 1754–1824)

A system is correct if it meets its design requirements. This much is agreed. But if the system we are designing is a piece of software, especially if it involves concurrency, how can we show this? It is not enough to merely show that a system can meet its requirements. A few tests generally suffice to demonstrate that. The real test is to show that a system cannot fail to meet its requirements.

Dijkstra's well-known dictum on testing[1] applies especially to concurrent software: the non-determinism of concurrent system executions makes it hard to devise a traditional test suite with sufficient coverage. There are fundamental problems here, related to both the limited controllability of events in distributed system executions and to the limited observability of those events.[2]

[1] The quote "Program testing can be used to show the presence of bugs, but never to show their absence" first appeared in Dijkstra [1972], p. 6. The quote has a curious pendant in Dijkstra [1965] that is rarely mentioned: "One can never guarantee that a proof is correct, the best one can say is: 'I have not discovered any mistakes.'"

[2] For instance, process scheduling decisions made simultaneously by different processors at distinct locations in a larger network.

A well-designed system provably meets its design requirements. But, if we cannot achieve this degree of certainty with standard test methods, what else can we do? Using standard mathematics is not much of an option in this domain. A thorough hand proof of even simple distributed programs can challenge the most hardened mathematician. At first blush, mechanical proof procedures also do not seem to hold much promise: it was shown long ago that it is fundamentally impossible to construct a general proof procedure for arbitrary programs.[3] So what gives?

[3] The unsolvability of the halting problem, for instance, was already proven in Turing [1936].

Fortunately, if some modest conditions are met, we can mechanically verify the correctness of distributed systems software. It is the subject of this book to show what these "modest conditions" are and how we can use relatively simple tool-based verification techniques to tackle demanding software design problems.
Logic Model Checking

The method that we will use to check the correctness of software designs is standard in most engineering disciplines. The method is called model checking. When the software itself cannot be verified exhaustively, we can build a simplified model of the underlying design that preserves its essential characteristics but that avoids known sources of complexity. The design model can often be verified, while the full-scale implementation cannot.

Bridge builders and airplane designers apply much the same technique when faced with complex design problems. By building and analyzing models (or prototypes) the risk of implementing a subtly flawed design is reduced. It is often too expensive to locate or fix design errors once they have reached the implementation phase. The same is true for the design of complex software.

The modeling techniques that we discuss in this book work especially well for concurrent software, which, as luck will have it, is also the most difficult to debug and test with traditional means.

The models we will build can be seen as little programs, written in, what may at first look like, a strangely abstract language. The models that are written in this language are in fact executable. The behaviors they specify can be simulated and explored exhaustively by the model checker in the hunt for logic errors. Constructing and executing these high-level models can be fun and insightful. It often also gives a sufficiently different perspective on a programming problem that may lead to new solutions, even before any precise checks are performed.

A logic model checker is designed to use efficient procedures for characterizing all possible executions, rather than a small subset, as one might see in trial executions. Since it can explore all behaviors, the model checker can apply a range of sanity checks to the design model, and it can successfully identify unexecutable code, or potentially deadlocking concurrent executions. It can even check for compliance with complex user-defined correctness criteria. Model checkers are unequalled in their ability to locate subtle bugs in system designs, providing far greater control than the more traditional methods based on human inspection, testing, or random simulation.

Model checking techniques have been applied in large scale industrial applications, to reduce the reliance on testing, to detect design flaws early in a design cycle, or to prove their absence in a final design. Some examples of these applications are discussed in this book.
The SPIN Model Checker

The methodology we describe in this book centers on the use of the model checker SPIN. This verification system was developed at Bell Labs in the eighties and nineties and is freely available from the Web (see Appendix D). The tool continues to evolve and has over many years attracted a fairly broad group of users in both academia and industry. At the time of writing, SPIN is one of the most widely used logic model checkers in the world.

In 2002 SPIN was recognized by the ACM (the Association for Computing Machinery) with its most prestigious Software System Award. In receiving this award, SPIN was placed in the league of truly breakthrough software systems such as UNIX, TeX, Smalltalk, Postscript, TCP/IP, and Tcl/Tk. The award has brought a significant amount of additional attention to the tool and its underlying technology. With all these developments there has been a growing need for a single authoritative and comprehensive user guide. This book is meant to be that guide.

The material in this book can be used either as classroom material or as a self-study guide for new users who want to learn about the background and use of logic model checking techniques. A significant part of the book is devoted to a comprehensive set of reference materials for SPIN that combines information that both novice and experienced users can apply on a daily basis.
**Book Structure**

SPIN can be used to thoroughly check high-level models of concurrent systems. This means that we first have to explain how one can conveniently model the behavior of a concurrent system in such a way that SPIN can check it. Next, we have to show how to define correctness properties for the detailed checks, and how to design abstraction methods that can be used to render seemingly complex verification problems tractable. We do all this in the first part of this book, Chapters 1 to 5.

The second part, Chapters 6 to 10, provides a treatment of the theory behind software model checking, and a detailed explanation of the fundamental algorithms that are used in SPIN.

The third part of the book, Chapters 11 to 15, contains more targeted help in getting started with the practical application of the tool. In this part of the book we discuss the command line interface to SPIN, the graphical user interface XSPIN, and also a closely related graphical tool that can be used for an intuitive specification of correctness properties, the Timeline editor. This part is concluded with a discussion of the application of SPIN to a range of standard problems in distributed systems design.

Chapters 16 to 19, the fourth and last part of the book, include a complete set of reference materials for SPIN and its input language, information that was so far only available in scattered form in books, tutorials, papers, and Web pages. This part contains a full set of manual pages for every language construct and every tool option available in the most recent versions of SPIN and XSPIN.


For courses in model checking techniques, the material included here can provide both a thorough understanding of the theory of logic model checking and hands-on training with the practical application of a well-known model checking system. For a more targeted use that is focused directly on the practical application of SPIN, the more foundational part of the book can be skipped.

A first version of this text was used for several courses in formal verification techniques that I taught at Princeton University in New Jersey, at Columbia University in New York, and at the Royal Institute of Technology in Stockholm, Sweden, in the early nineties. I am most grateful to everyone who gave feedback, caught errors, and made suggestions for improvements, as well as to all dedicated SPIN users who have graciously done this throughout the years, and who fortunately continue to do so.

I especially would like to thank Dragan Bosnacki, from Eindhoven University in The Netherlands, who read multiple drafts for this book with an unusually keen eye for spotting inconsistencies, and intercepting flaws. I would also like to thank Al Aho, Rajeev Alur, Jon Bentley, Ramesh Bharadwaj, Ed Brinksma, Marsha Chechik, Costas Courcoubetis, Dennis Dams, Matt Dwyer, Vic Du, Kousha Etessami, Michael Ferguson, Rob Gerth, Patrice Godefroid, Jan Hajek, John Hatcliff, Klaus Havelund, Leszek Holenderski, Brian Kernighan, Orna Kupferman, Bob Kurshan, Pedro Merino, Alice Miller, Doug McIlroy, Anna Beate Oestreicher, Doron Peled, Rob Pike, Amir Pnueli, Anuj Puri, Norman Ramsey, Jim Reeds, Dennis Ritchie, Willem-Paul de Roever, Judi Romijn, Theo Ruys, Ravi Sethi, Margaret Smith, Heikki Tauriainen, Ken Thompson, Howard Trickey, Moshe Vardi, Phil Winterbottom, Pierre Wolper, Mihalis Yannakakis, and Ozan Yigit, for their often profound influence that helped to shape the tool, and this book.

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Chapter 1. Finding Bugs in Concurrent Systems

"For we can get some idea of a whole from a part, but never knowledge or exact opinion."

—(Polybius, ca. 150 B.C., Histories, Book I:4)

SPIN can be used to verify correctness requirements for systems of concurrently executing processes. The tool works by thoroughly checking either hand-built or mechanically generated models that capture the essential elements of a distributed systems design. If a requirement is not satisfied, SPIN can produce a sample execution of the model to demonstrate this.

There are two basic ways of working with SPIN in systems design. The first method, and the primary focus of this book, is to use the tool to construct verification models that can be shown to have all the required system properties. Once the basic design of a system has been shown to be logically sound, it can be implemented with confidence. A second, less direct, method is to start from an implementation and to convert critical parts of that implementation mechanically into verification models that are then analyzed with SPIN. Automated model extraction tools have been built to convert programs written in mainstream programming languages such as Java and C into SPIN models. A discussion of the latter approach to software verification is given in Chapter 10, and the constructs in SPIN that directly support model extraction techniques are discussed in Chapter 17.

We begin by considering in a little more detail what makes it so hard to test concurrent software systems, and why there is a need for tools such as SPIN.

It is worth noting up front that the difficulty we encounter when trying to reason about concurrent systems is not restricted to software design. Almost everything of interest that happens in our world involves concurrency and access to shared resources. In the supermarket, customers compete for shared resources, both consumable ones (such as food items) and non-consumable ones (such as checkout clerks). Customers follow simple, and very ancient, protocols for breaking ties and resolving conflicts. On the road, cars compete for access to road intersections and parking spots. In telephone systems, similarly, large numbers of simultaneous users compete for shared resources, this time with the unique feature that the users themselves are among the resources being shared. Problems of interaction occur in all these cases, and any new and untried set of rules that we may come up with to solve these problems can backfire in unexpected, sometimes amusing, and sometimes disastrous, ways.
Circular Blocking

As a simple example, we can look at the protocol rules that regulate the movements of cars across intersections. There is no unique solution, or even a best solution to this problem, as testified by the widely different standards that have been adopted in different countries around the world. In the U.S., when two roads intersect, one direction of traffic always explicitly has priority over the other direction, as indicated by markings on the pavement and by road signs. At traffic circles, however, an implicit rule applies, rarely explicitly indicated, giving priority to traffic inside the circle. The implicit rule for circles is sensible, since it gives priority to cars leaving the circle over cars trying to enter it, which can avoid congestion problems.

In some European countries, the implicit and explicit rules are reversed. In the Netherlands, for instance, an implicit rule states that at otherwise unmarked intersections cars approaching from one's right have the right of way. The rule for traffic circles is explicitly marked to override this rule, again giving priority to traffic inside the circle. The implicit rule for unmarked intersections is simple and effective. But this rule can have unexpected consequences under heavy traffic conditions, as illustrated in Figure 1.1. It is not even true that we could avoid this problem with traffic lights that regularly reverse priority rules. One visit to a sufficiently large city will suffice to make it clear that this cannot prevent the problem. A fixed priority rule is not preferable either, since it will allow one direction of traffic to deny access to the other direction for any length of time. On the road, the occurrence of these conditions is typically accepted as just another fact of life. When they occur, they can often only be resolved by breaking the otherwise agreed upon rules. It will be clear that in software systems we cannot rely on such resolutions: The rules must cover all conceivable cases, and unfortunately, they must also cover all the humanly inconceivable ones.

Figure 1.1. Circular Blocking
Deadly Embrace

As another everyday example, to make a person-to-person call, a user must secure exclusive access to at least two shared resources in the telephone system: the line of the calling party and the line of the called party. The resources are allocated in a fixed order. Access is always first granted to the calling party's line and only then to the called party's line. Normally this causes no hardship, but when two subscribers A and B simultaneously attempt to establish a connection to each other, the access rules will prevent this. If both parties repeatedly pick up the receiver simultaneously to dial the connection, and refuse to give up until access is granted, they will repeatedly fail. This is especially curious because the two requests do not actually conflict: both subscribers desire the connection.

A very similar problem is encountered in the management of shared resources in operating systems. Virtually every textbook on operating systems contains a description of the problem. In the example used there, the shared resources are typically a line printer (A) and a card reader (B); the example is indeed that old. Two user processes then compete for exclusive access to these resources, both of which may be needed simultaneously, for instance to print a deck of punchcards. A deadly embrace is entered when both processes succeed in obtaining access to one of the two resources and then decide to wait indefinitely for the other. Of course it will not do to just require the processes to yield resources back to the operating system while waiting for more resources to become available.

The generic sequence of steps leading into the deadly embrace is illustrated in Figure 1.2. The solid arrows indicate the control-flow order in the two user processes. Once the two dashed states are reached simultaneously, there is no way to proceed. The dotted arrows indicate the dependency relations that prevent progress. Before device B can be obtained by the first process, it must first be released by the second process, and before device A can be obtained by the second process, it must first be released by the first. The circular dependencies illustrate the deadly embrace.

Figure 1.2. Deadly Embrace
Mismatched Assumptions

It is a trusted premise of systems engineering that large systems should be built from smaller components, each of which can be designed and tested with a high degree of confidence. Ideally, the final system is then only assembled when all the smaller pieces have been proven correct. Some design problems, though, only become evident at the system level, and the absence of reliable methods for testing system level problems can sometimes take us by surprise. Decisions that are perfectly legitimate at the component level can have unexpected, and sometimes dramatic consequences at the system level.

A good illustration of this phenomenon is what happened September 14, 1993 on the runway at Warsaw airport in Poland. A Lufthansa Airbus A320-200 with 72 people on board was landing in heavy rain. The plane was not getting much traction from the wheels in the landing gear on the wet runway, but the pilots knew that they could count on the thrust reversers on the main engines to bring the plane to a stop. As it happened, the thrust reversers failed to deploy in time, and the plane overshot the end of the runway.


A thrust reverser should, of course, never be activated when a plane is in flight. Most planes, therefore, have elaborate protection built-in to prevent this from happening. This includes, for instance, that the thrust reversers cannot be deployed unless three conditions are met: the landing gear must be down, the wheels must be turning, and the weight of the plane must be carried on the wheels. In this case the landing gear was down, but the wheels were hydroplaning, and an unexpected tailwind provided enough lift on the wings that the control software did not decide until nine seconds after touchdown that the plane had landed. Two people lost their lives when the plane went off the end of the runway.

The most fascinating aspect of an accident like this is that no one really made any mistakes in the design or operation of this plane. All components were designed in a very sensible manner. The control software for the thrust reversers, though, was not designed to cope with the unexpected combination of events that occurred. This software formed one component in a complex system with many other interacting parts, including the dominant weather conditions that can affect a plane's operation.

When complex systems fail, the scenarios that trigger the failures usually could not easily have been imagined by any sensible human designer. For every one failure scenario that is considered, there are a million others that may be overlooked. In cases like this, it is invaluable to have design tools that can hunt down the potential error scenarios automatically, working from a sober description of the individual piece parts that together form a more complex integrated system. Automated tools have no trouble constructing the bizarre scenarios that no sane human could imagine—just the type of scenario that causes real-life systems to crash.

"The most pernicious and subtle bugs are system bugs arising from mismatched assumptions made by the authors of various components."

(Fred Brooks, The Mythical Man-Month, p.142)
Fundamental Problems of Concurrency

The purpose of these few examples is to convince you of two things. First, concurrency-related problems are not rare oddities that appear only in obscure corners of software engineering. They are a fundamental part of life, and they can and do turn up almost everywhere. Secondly, it can be uncommonly hard to predict in advance where the problems in the various schemes can hide. Even the most obvious rules can have unexpected consequences. To find these problems, it never suffices to take a system apart, to study the individual components, and prove them correct. These types of problems have to do uniquely with the interaction of multiple, concurrently executing components. They are caused by the way in which the components are put together.

These types of problems are also extraordinarily hard to identify with standard system testing techniques. To test a piece of code, it should be possible to administer a series of reproducible tests and to evaluate the results. The keyword here is reproducible. Many aspects of the execution in a concurrent system are beyond the control of a tester. This lack of controllability makes it hard, if not impossible, to administer tests in a reproducible manner. This applies especially to the details of process execution and process interleaving that are in part determined by process schedulers, often running on independently executing hosts. The details of process interleaving, and even such subtle things as the relative speed of execution of asynchronously executing processes, can easily affect the outcome of a test. Even if the tester could know exactly how the process executions had to be interleaved in time to reproduce an error scenario, it is in general not possible to enforce such a schedule in a system test.

Limited observability and limited controllability normally restrict a tester's ability to thoroughly exercise concurrent system behaviors. As a result, some of the most difficult to diagnose bugs can slip through and hide as residual defects in production code, with the potential of striking at the least opportune moment in the lifetime of a system. To find these types of problems in a more systematic way, we need a different type of verification method. In the next chapter we begin the description of such a method with a tutorial overview of the language that is used to describe verification models in SPIN.

Traditional methods for testing software systems focus their energy on system description at the lowest level of detail, where higher level design errors are the hardest to find and the most costly to fix. By using verification models, we will be able to describe and verify complex system behavior at any desired level of abstraction, tracking it from concept to code. As noted, in larger systems it is not just the outright blunders that can cause system failure. Every single part of a system may have been designed correctly when considered in isolation. But if in the design of the various parts the system requirements were interpreted in just slightly different ways, the system as a whole can still fail. As system designers, we need tools that can catch all these types of design errors.
Chapter 2. Building Verification Models

"Measure what is measurable, and make measurable what is not so."

—(Galileo Galilei, 1564–1642)

To verify a system we need to describe two things: the set of facts we want to verify, and the relevant aspects of the system that are needed to verify those facts. We investigate the types of facts we may want to prove about distributed systems in the next chapter. Here, we start with a gentle introduction to the art of describing distributed systems behavior at a relatively high level of abstraction, so that an automated verification of salient system facts becomes possible. We call such descriptions verification models.
The tool that we will use to check verification models is called SPIN, and the specification language that it accepts is called PROMELA. The name SPIN was originally chosen as an acronym for Simple PROMELA Interpreter. The tool has arguably outgrown at least two of these three descriptive terms, but the name has stuck. SPIN can be used in two basic modes: as a simulator and as a verifier. In simulation mode, SPIN can be used to get a quick impression of the types of behavior that are captured by a system model, as it is being built. SPIN's graphical user interface, XSPIN (discussed in Chapter 12, p. 267), can conveniently visualize simulation runs, which can be of considerable help in the debugging of models. We use the term debugging intentionally here. No amount of simulation can prove the facts we may be interested in; only a verification run can do so. Nonetheless, when the verifier finds a counterexample to a correctness claim, it relies on the SPIN simulator to display the error trace using guided simulation. Simulation and verification are therefore tightly coupled in SPIN.

In this introductory chapter, we use SPIN primarily in simulation mode, only briefly illustrating how verifications can be set up in some common cases. To keep things simple, we also use the tool only in its basic command-line mode here, and resist the use of the graphical user interface for now. When we do discuss the graphical user interface, it will be a definite advantage if the user already knows the basic operation of SPIN itself, and the most important set of command-line options.

The focus on model building and simulation in this chapter leaves a lot to be explored in the rest of this book. The specification of correctness properties, for instance, is covered in Chapters 4 and 13. The use of SPIN for system verification is discussed in Chapters 11 and 14. And, finally, SPIN's graphical user interface, XSPIN, is discussed in Chapter 12.
PROMELA

PROMELA is an acronym for Process Meta-Language. The use of the term meta is significant in this context. As we shall see, abstraction is often key to successful verification. The specification language is intended to make it easier to find good abstractions of systems designs. PROMELA is not meant to be an implementation language but a systems description language. To make this possible, the emphasis in the language is on the modeling of process synchronization and coordination, and not on computation. The language is also targeted to the description of concurrent software systems, rather than the description of hardware circuits (which is more common for model checking applications).

The basic building blocks of SPIN models are asynchronous processes, buffered and unbuffered message channels, synchronizing statements, and structured data. Deliberately, there is no notion of time, or of a clock; there are no floating point numbers, and there are only few computational functions. These restrictions make it relatively hard to model the computation of, say, a square root in this language (cf. p. 325), but relatively easy to model and verify the behavior of clients and servers in networks of processors (cf. p. 299).
Examples

To get started, we discuss a few small examples of PROMELA specifications. We will prompt you for the things that are worth observing in these models, and for some experiments you can do to explore them further. We do not intend to define the language in full detail here; only to convey the style of system specifications in PROMELA. A more systematic treatment of various aspects of the language can be found, or skipped, in Chapters 3, 7, 16, and 17.
Hello World

The quintessential first program that prints a string on the user's terminal is, of course, hello world. The example dates from the first C programming language manual, Kernighan and Ritchie [1978]. It has been duplicated in virtually every language manual since then. We can specify this famous little first program as a PROMELA model as follows:

```pml
active proctype main()
{
    printf("hello world\n")
}
```

To simulate an execution of this model, assuming that we store it in a file named hello.pml, we can type the following, on a UNIX or UNIX-like system, at the shell prompt:

```
$ spin hello.pml
hello world
1 process created
```

and be rewarded with the gratifying result. The output, which is from SPIN's simulator, also contains a short reminder that PROMELA is a process modeling language, not a programming language. One process was created to simulate the execution of the model; there will usually be many more in a verification model.

The filename extension .pml is not required. SPIN is equally accommodating if other extensions, or none at all, are used.

If you have done some programming in C, all this will look familiar, as will many other features of the language that we encounter later. But there are some important differences. To begin with a few notable ones from this first example: active and proctype are keywords in the language, but main is not. That is, we could have used any other non-reserved word instead of main in this context. Next, there is no semicolon at the end of the printf statement, where in C this would be required. The reason is that the semicolon is defined as a statement separator in our new language, not as a statement terminator. This minor detail can of course quickly become a nuisance, so SPIN's parser is lenient on this issue. If you happen to type a semicolon where none is required, the parser will forgive you and quietly ignore it.

If it is not particularly important that the initial process is named, we can also use a shorthand notation to declare and instantiate an anonymous one, as follows:

```
init {
    printf("hello world\n")
}
```

Clearly, this works for only one single process, so in almost all cases of interest the use of a proctype declaration will be more useful. The keyword init, though, is a reserved word in the language and cannot be used for any other purpose, that is, it cannot be used for variable names or for proctype names.

A SPIN model is used to describe the behavior of systems of potentially interacting processes: multiple, asynchronous threads of execution. The primary unit of execution in a SPIN model is therefore a process, and not a C-style procedure. The keyword proctype in the hello world example denotes that the identifier main that follows,
Producers and Consumers

The hello world example includes just one single process, so there is not much opportunity there to experiment with process interaction. Our next example, shown in Figure 2.1, is a little system of two processes that do interact, by coordinating their actions with the help of a shared global variable.

Figure 2.1 Simple Producer Consumer Example

mtype = { P, C };

mtype turn = P;

active proctype producer()
{
    do
        :: (turn == P) ->
            printf("Produce\n");
            turn = C
        od

    active proctype consumer()
    {
        do
            :: (turn == C) ->
                printf("Consume\n");
                turn = P
            od
    }

The first line of the model declares two symbolic names, P and C. The effect of this declaration is very much like an enum declaration in a C program: the SPIN parser assigns a unique, positive integer value to each name, which represents it internally. As the typename suggests, this type of declaration is often used to define the names of a range of message types used in interprocess message exchanges.

Following the mtype declaration, we find a global declaration of a variable named turn of type mtype. The variable can take any of the values from the mtype declaration, which in this case means that it can be assigned the symbolic values P and C. If left uninitialized, the value of the variable is zero, which is outside the range of possible mtype values. To avoid this, we assigned the initial value P. Next, we see two proctype declarations, both with the prefix active, defining that one process of each type is to be instantiated automatically.

The control structure within each proctype is the same: both contain a loop. A PROMELA loop starts with the keyword do and ends with od. The loop body should contain one or more option sequences, with each separate option sequence preceded by a double colon ::. In this case, the loops have just one single option sequence each. Each of these sequences has three, not two, statements, as we shall soon see.

The first statement after a double colon has special significance: it is called the guard statement, and it alone determines whether or not the execution sequence that follows is selectable for execution. In the case of the producer process, the one option for execution is guarded by the condition (turn==P). This means that the statements that follow this guard can only be executed if and when the variable turn has the value P. PROMELA uses the double equals for the boolean equals operator and single equals for assignment, as in the C language.

The PROMELA loop is similar to another PROMELA control-flow construct: the selection statement. If we write the loop from the producer process with a selection statement, for instance, and use a jump and a label to execute it repeatedly, it looks as follows:

active proctype producer()
{
    again: if
Extending the Example

What will happen to our little device to enforce the alternation between producer and consumer if we instantiate a few more processes of each type? We can do so most easily by adding the desired number of processes to be instantiated to the proctype declarations, as follows:

```pml
active [2] proctype producer() { ... }
```

Suppose we still wanted to enforce a strict alternation of execution of one of multiple running producer processes and one of multiple consumer processes. The earlier solution no longer works, because it is now possible that immediately after a first process of type producer evaluates the guard condition (turn==P) and finds it true, a second process of the same type comes to the same conclusion and also proceeds with its execution, potentially causing havoc.

To avoid this problem, we have to add a little more mechanism. First, we add one more symbolic value that we can use to record that the variable turn is neither P nor C. Let's call this value N. This changes the mtype declaration into:

```pml
mtype = { P, C, N };
```

We could equally well have added the extra definition in a separate declaration, for instance, as:

```pml
mtype = { P, C };
mtype = { N };
```

The declaration and initialization of variable turn itself remains as it was, but we add one extra global variable for bookkeeping purposes. The variable will record the identity of the process that is currently executing as either a producer or a consumer.

```pml
pid who;
```

The type of this new variable is pid, and its name is who. We have left the variable uninitialized, since its initial value does not matter much to us here. If no explicit initial value is specified, the variable is by default initialized to zero.

The new declaration for the producer processes is as follows:

```pml
active [2] proctype producer() {
    do
        :: request(turn, P, N) ->
            printf("P%d\n", _pid);
            assert(who == _pid);
            release(turn, C)
    od
}
```
Mutual Exclusion

Perhaps the best illustration of the difficulty of designing correct coordination schemes for asynchronously executing processes is the classic mutual exclusion problem. The problem here is to find a way to grant mutually exclusive access to a shared resource while assuming only the indivisibility of read and write operations. That is, to solve this problem we cannot assume the availability of atomic sequences to make a series of test and set operations indivisible. One of the first attempted solutions of the problem was described by Edsger Dijkstra in Dijkstra [1965]. Dijkstra gives credit for the algorithm to the Dutch mathematician T.J. Dekker, who first devised it in 1962. It solves the problem for two processes only. The PROMELA version of this algorithm can be written as shown in Figure 2.3.

Figure 2.3 Dekker's Mutual Exclusion Algorithm (1962)

```plaintext
bit    turn;
bool   flag[2];
byte   cnt;

active [2] proctype mutex()
{
    pid i, j;
    i = _pid;
    j = 1 - _pid;
    again:
        :: flag[i] ->
            do
                :: turn == j ->
                    flag[i] = false;
                    (turn != j) -> /* wait until true */
                    flag[i] = true
                :: else ->
                    skip /* do nothing */
            fi
            :: else ->
                break /* break from loop */
            od;
        cnt++;
        assert(cnt == 1); /* critical section */
        cnt--;
        turn = j;
        flag[i] = false;
        goto again
}
```

The algorithm uses a bit variable named turn with a similar function as in our previous producer/consumer example. Since there are just two processes in the system, the turn variable can point to one or the other using just a zero or a one. Note, though, that this time we cannot assume that the two processes will be content to alternate their access to the critical part of the code where the shared resource is accessed. If only one of the two processes needs access, it should be able to acquire it arbitrarily often. This makes the problem much harder to solve correctly. Dekker's algorithm uses an array of two booleans called flag to track the progress of the two processes. In our PROMELA model we have also added a global variable cnt of type byte to count how many processes can succeed in accessing the critical section in the code simultaneously. If all is well, this variable can never be assigned a value greater than one or less than zero. An assertion in the code can check if this is indeed the case.

We use a local variable, i of type pid, to record the instantiation numbers of the running process. Each process must also know the pid of its competitor, and since we only have two processes here, predictably with pid numbers zero and one, each process can obtain the pid of its peer by subtracting its own pid from one.

The attempt to gain access to the critical section in the code starts by setting an element of boolean array flag to true. This is necessary so that the process can set the flag back to false if it decides to abort early. Since we have two processes, each process can verify that it is the only one with flag[i] true by testing turn[i].
Message Passing

So far we have not shown any example of the use of message passing between asynchronous processes. We will remedy that now. The following example illustrates the basic mechanism. The specification in Figure 2.6 models a protocol that was proposed in 1981 at Bell Labs for use in a new data switch.

**Figure 2.6 Data Transfer Protocol**

```plaintext
mtype = { ini, ack, dreq, data, shutup, quiet, dead };

chan M = [1] of { mtype };
chan W = [1] of { mtype };

active proctype Mproc()
{
    W!ini;       /* connection */
    M?ack;       /* handshake */
    timeout ->   /* wait */
    if
    :: W!shutup  /* start shutdown */
    :: W!dreq;   /* or request data */
        M?data -> /* receive data */
        do
        :: W!data   /* send data */
        :: W!shutup; /* or shutdown */
        break
    od
    fi;

    M?shutup;     /* shutdown handshake */
    W!quiet;
    M!dead
}

active proctype Wproc()
{
    W?ini;       /* wait for ini */
    M!ack;       /* acknowledge */
    do            /* 3 options: */
    :: W!dreq -> /* data requested */
        M!data  /* send data */
    :: W?data -> /* receive data */
        skip    /* no response */
    :: W?shutup ->
        M!shutup; /* start shutdown */
    break
    od;

    W?quiet;
    M!dead
}
```

The first line of the specification contains a declaration of symbolic names for seven different types of messages, using an mtype declaration as before. Next, we see a new data type called chan. On two subsequent lines, two buffered message channels are declared, each with a capacity to store one message. The messages themselves that can be stored in these channels are in both cases declared to be of type mtype (i.e., one of the values from the mtype declaration on the first line). In general, there can be any number of message fields, of arbitrary types, which could be specified in a comma-separated list in the spot where we now find only the one mtype keyword.

Two types of processes are declared and instantiated, as stipulated by the prefix active. The first process, of type Mproc, receives messages via channel M and sends them to its peer via channel W. The second process, of type Wproc, receives messages via channel W and sends them to its peer via channel M. Both processes also have the capability to initiate a shutdown handshake, either by sending a message of type shutup or by waiting for a corresponding acknowledgment message.
In Summary

In this chapter we have taken a first look at some small examples of PROMELA verification models. The examples are not meant to give an exhaustive overview of the PROMELA language, but they are meant to give an idea of its main focus, which is to model the behavior of interacting asynchronous processes in distributed systems. The aim of the SPIN verifier is not to verify the computational aspects of an application; it is to reliably identify problems that are caused by process interaction. This means that we are interested in the quirky problems of process coordination, and not in the properties of local, sequential, or deterministic computations.

At this point, two types of criticism of the language we have discussed may legitimately be raised. The first is that the language is too permissive, making it too easy to encode dubious constructs, such as arbitrary goto jumps, and unrestricted access to global variables or message channels. Another valid criticism can be that the language is too restrictive, lacking many of the more salient features of implementation languages such as C.

To counter the first criticism, it suffices to note that the purpose of this modeling language is not to prevent the construction of dubious constructs, but to allow the user to investigate them thoroughly with the help of formal verification. The language allows us to expose dubious constructs not by argument but by verification, especially in cases where the designer never suspected that there could possibly be a problem.

So if the language is not too permissive, is it too restrictive? Why, for instance, not use full C as the specification language for SPIN? The sobering answer is that we would quickly find that virtually all properties of interest would become undecidable. We can only obtain an effectively useful verification system by imposing some reasonable limits on what can be specified. There is no possibility, for instance, to define an infinite buffer in basic PROMELA, or to describe systems that would require the creation of an infinite number data objects or processes to execute. Attempts to do so are pedantically flagged as errors by the SPIN verifier. Fortunately, we will see that it is not hard to live within the self-imposed limits. With some experience in model construction, we can prove or disprove critical correctness properties of even very substantial systems. The parsimony of PROMELA has another benefit, which is that compared to more elaborate implementation or specification languages, it takes most users relatively little time to learn the main concepts well enough to start writing models with confidence.

Curiously, in this context, one of the more interesting recent extensions of the PROMELA language has broken with the strict enforcement of the rule of parsimony by allowing the inclusion of embedded fragments of C code into SPIN models. This extension allows us to come very close to the modeling of implementation level code, especially when we use automated model extraction tools. With the additional power come additional dangers. As Brian Kernighan and Rob Pike once put it: "C is a razor-sharp tool, with which one can create an elegant and efficient program or a bloody mess."

We discuss model extraction techniques and the extensions that allow the use of embedded C code in SPIN models in Chapters 10 and 17.
Bibliographic Notes

The quote about C from the last section appeared first on page 71 of Kernighan and Pike [1999].

The producer-consumer problem is one of the many intriguing problems in concurrent systems design that were first introduced and solved by Edsger Dijkstra. The example first appeared in a series of lecture notes that Dijkstra wrote in early 1965, and made available to friends and colleagues as EWD123. A revised version of the report was later distributed more broadly as Dijkstra [1968].

The mutual exclusion problem that we referred to in this chapter also has a long and colorful history. The problem was first clearly articulated in Dijkstra [1965], and has triggered a long series of papers and books that continues to this day. We will not attempt to summarize the debate about mutual exclusion here. A good starting point for a study can be Raynal [1986], or Lamport [1986].

A start with the design of the PROMELA language was made in 1979 to support the specification of verification models for SPIN's earliest predecessor PAN, [5] as described in Holzmann [1981]. There was no firm name for the language at first, although for brief moments we used the terms PSL, short for Process Specification Language, PROTO, short for Proto-typing language, and even the non-acronym "Argos" in Holzmann [1987].

[5] PAN was originally the name of a stand-alone tool, and was short for Protocol Analyzer. Many years later, we reused the name for the verifiers that can be generated by SPIN. The name is now more comfortably understood as an acronym for Process Analyzer.

The language was influenced in important ways by Dijkstra [1975]. Dijkstra's proposal for a non-deterministic guarded command language, though, did not contain primitives for message passing. The syntax for the notation that was adopted in PROMELA was taken from Hoare's CSP language, as documented in Hoare [1978].

A third influence on the design of PROMELA that is often mentioned is the programming language C, as first described in Kernighan and Ritchie [1978]. This influence is also mostly restricted to syntax. Though PROMELA was influenced by several other languages, there are important differences that we will discuss in more detail in Chapter 3. The differences are motivated by the unique purpose that PROMELA has. PROMELA models are not meant to be analyzed manually, and they are not meant to be used as implementations. The purpose of a PROMELA model is solely to support the effective, automated verification of problems in distributed systems design.
Chapter 3. An Overview of PROMELA

"What we see depends on mainly what we look for."

—(Sir John Lubbock, 1834–1913)

In the last chapter we saw that the emphasis in PROMELA models is placed on the coordination and synchronization aspects of a distributed system, and not on its computational aspects. There are some good reasons for this choice. First, the design and verification of correct coordination structures for distributed systems software tends to be much harder in practice than the design of a non-interactive sequential computation, such as the computation of compound interest or square roots. Second, the curious situation exists that the logical verification of the interaction in a distributed system, though often computationally expensive, can be done more thoroughly and more reliably today than the verification of even the simplest computational procedure. The specification language we use for systems verification is therefore deliberately designed to encourage the user to abstract from the purely computational aspects of a design, and to focus on the specification of process interaction at the system level.

As a result of this specialization, PROMELA contains many features that are not found in mainstream programming languages. These features are intended to facilitate the construction of high-level models of distributed systems. The language supports, for instance, the specification non-deterministic control structures; it includes primitives for process creation, and a fairly rich set of primitives for interprocess communication. The other side of the coin is that the language also lacks some features that are found in most programming languages, such as functions that return values, expressions with side effects, data and functions pointers, etc. The reason is simple: PROMELA is not a programming language. PROMELA is a language for building verification models.

A verification model differs in at least two important ways from a program written in a mainstream programming language such as Java or C.

- A verification model represents an abstraction of a design that contains only those aspects of a system that are relevant to the properties one wants to verify.

- A verification model often contains things that are typically not part of an implementation. It can, for instance, include worst-case assumptions about the behavior of the environment that may interact with the modeled system, and, most importantly, it either explicitly or implicitly contains a specification of correctness properties.

Even though it can be attractive to have a single specification that can serve as both a verification model and as an implementation of a system design—verification and implementation have some fundamentally different objectives. A verification model is comparable in its purpose to the prototype or design model that a civil engineer might construct: it serves to prove that the design principles are sound. Design models are normally not expected to be part of the final implementation of a system.

A full system implementation typically contains more information, and far more detail, than a design model. This means that it can be difficult to find automatic procedures for converting design models into system implementations. The reverse, however, is not necessarily true. In Chapter 10 we will explore means for mechanically extracting the main elements of a verification model directly from an implementation, guided by abstraction techniques. Similarly, in Chapter 17 we will discuss the specific constructs that are available in PROMELA to facilitate model extraction tools. These topics, though, should be considered advanced use of the model checker, so we will conveniently ignore them for now.

In the last chapter we gave a bird's-eye view of the language, briefly touching on some of the main language constructs that are available to build verification models. In this chapter we cover the language more thoroughly. We will try to cover all main language features in a systematic way, starting with the most general constructs, and slowly descending into more of the specifics. We restrict ourselves here to the mechanisms that are at our disposal for describing process behavior and process interaction. In the next chapter we will continue the discussion with a description of the various means we have to define correctness claims. After we have covered these basics, we move on to discuss methods for exploiting design abstraction techniques as an aid in the control of verification complexity.
Types of Objects

PROMELA derives many of its notational conventions from the C programming language. This includes, for instance, the syntax for boolean and arithmetic operators, for assignment (a single equals) and equality (a double equals), for variable and parameter declarations, variable initialization and comments, and the use of curly braces to indicate the beginning and end of program blocks. But there are also important differences, prompted by the focus in PROMELA on the construction of high-level models of the interactions in distributed systems.

A PROMELA model is constructed from three basic types of objects:

- Processes
- Data objects
- Message channels

Processes are instantiations of proctype declarations, and are used to define behavior. There must be at least one proctype declaration in a model, and for the model to be of much use there will normally also be at least one process instantiation.

A proctype body consists of zero or more data declarations, and one or more statements. The semantics of statement execution is somewhat special in PROMELA, since it also doubles as the primary mechanism for enforcing process synchronizations. We have seen some of this in the last chapter, and we will return to it in more detail in the section on executability (p. 51).

Process types are always declared globally. Data objects and message channels can be declared either globally, that is, outside all process type declarations, or locally, that is, within a process type declaration. Accordingly, there are only two levels of scope in PROMELA: global and process local. It is, for instance, not possible to restrict the scope of a global object to only a subset of the processes, or to restrict the scope of a local object to only part of a proctype body.

The next three sections contain a more detailed discussion of each of the three basic types of objects in PROMELA. This is followed by a discussion of PROMELA's rules for executability, and a more comprehensive overview of the primitives in PROMELA for defining flow of control.
Processes

In the last chapter we saw that we can declare and instantiate processes by prefixing a proctype declaration with the keyword active. There are several ways to instantiate processes in PROMELA. We can create multiple instantiations of a given proctype by adding the desired number in square brackets to the active prefix, for instance as follows:

active [2] proctype you_run()
{
    printf("my pid is: \%d\n", _pid)
}

Each running process has a unique process instantiation number. These instantiation numbers are always non-negative, and are assigned in order of creation, starting at zero for the first created process. Each process can refer to its own instantiation number via the predefined local variable _pid. Simulating the example above, for instance, produces the following output:

$ spin you_run.pml
my pid is: 0
    my pid is: 1
2 processes created

The two processes that are instantiated here each print the value of their process instantiation number and then terminate. The two lines of output happen to come out in numeric order here, but since process execution is asynchronous, it could just as well have been the opposite. By default, during simulation runs, SPIN arranges for the output of each active process to appear in a different column: the pid number is used to set the number of tab stops used to indent each new line of output that is produced by a process. [1]

[1] We can now see that the string hello world in the last chapter was printed left justified by a happy coincidence. It was because the process executing the statement had pid zero. We can suppress the default indentations by invoking spin with option -T (see p. 513).

There is also another way to instantiate new PROMELA processes. Any running process can start other processes by using a predefined operator called run. For instance, we could rewrite the last example as follows:

proctype you_run(byte x)
{
    printf("x = \%d, pid = \%d\n", x, _pid)
}

init {
    run you_run(0);
    run you_run(1)
}

A disadvantage of this solution is that it often creates one process more than strictly necessary (i.e., the init process). For simulation or implementation, the extra process would not matter too much, but in system verification we usually take every possible precaution to keep the system descriptions at a minimum: avoiding all unnecessary elements.

A simulation run of the last model produces the following result:

$ spin you_run2.pml
my pid is: 0
    my pid is: 1
my pid is: 2
2 processes created

my pid is: 0
    my pid is: 1
7 processes created

...
Provided Clauses

Process execution is normally only guided by the rules of synchronization captured in the statement semantics of proctype specifications. It is possible, though, to define additional global constraints on process executions. This can be done with the help of the keyword provided which can follow the parameter list of a proctype declaration, as illustrated in the following example:

```c
bool toggle = true;       /* global variables */
short cnt;                /* visible to A and B */

active proctype A() provided (toggle == true)
{
    cnt++;            /* means: cnt = cnt+1 */
    printf("A: cnt=%d\n", cnt);
    toggle = false;    /* yield control to B */
    goto L             /* do it again */
}

active proctype B() provided (toggle == false)
{
    cnt--;            /* means: cnt = cnt-1 */
    printf("B: cnt=%d\n", cnt);
    toggle = true;    /* yield control to A */
    goto L
}
```

The provided clauses used in this example force the process executions to alternate, producing an infinite stream of output:

```
$ spin toggle.pml | more
A: cnt=1
    B: cnt=0
A: cnt=1
    B: cnt=0
A: cnt=1
    B: cnt=0
A: cnt=1
...
```

A process cannot take any step unless its provided clause evaluates to true. An absent provided clause defaults to the expression true, imposing no additional constraints on process execution.

Provided clauses can be used to implement non-standard process scheduling algorithms. This feature can carry a price-tag in system verification, though. The use of provided clauses can disable some of SPIN's most powerful search optimization algorithms (cf. Chapter 9).
Data Objects

There are only two levels of scope in PROMELA models: global and process local. Naturally, within each level of scope, all objects must be declared before they can first be referenced. Because there are no intermediate levels of scope, the scope of a global variable cannot be restricted to just a subset of processes, and the scope of a process local variable cannot be restricted to specific blocks of statements. A local variable can be referenced from its point of declaration to the end of the proctype body in which it appears, even when it appears in a nested block (i.e., a piece of code enclosed in curly braces). This is illustrated by the following example:

Table 3.1. Basic Data Types

<table>
<thead>
<tr>
<th>Type</th>
<th>Typical Range</th>
</tr>
</thead>
<tbody>
<tr>
<td>bit</td>
<td>0, 1</td>
</tr>
<tr>
<td>bool</td>
<td>false, true</td>
</tr>
<tr>
<td>byte</td>
<td>0..255</td>
</tr>
<tr>
<td>chan</td>
<td>1..255</td>
</tr>
<tr>
<td>mtype</td>
<td>1..255</td>
</tr>
<tr>
<td>pid</td>
<td>0..255</td>
</tr>
<tr>
<td>short</td>
<td>–215 .. 215 – 1</td>
</tr>
<tr>
<td>int</td>
<td>–231 .. 231 – 1</td>
</tr>
<tr>
<td>unsigned</td>
<td>0 .. 2n – 1</td>
</tr>
</tbody>
</table>

init {
  /* x declared in outer block */
  int x;
  { /* y declared in inner block */
    int y;
    printf("x = %d, y = %d\n", x, y);
    x++;
    y++;
  } /* y remains in scope */
  printf("x = %d, y = %d\n", x, y);
}

When simulated this model produces the output:

$ spin scope.pml
x = 0, y = 0
Data Structures

PROMELA has a simple mechanism for introducing new types of record structures of variables. The following example declares two such structures, and uses them to pass a set of data from one process to another in a single, indivisible operation:

```proctype me(Field z) {
    z.g = 12
}
init {
    Record goo;
    Field foo;
    run me(foo)
}
```

We have defined two new data types named Field and Record, respectively. The local variable goo in the init process is declared to be of type Record. As before, all fields in the new data types that are not explicitly initialized (e.g., all fields except f in variables of type Field) are by default initialized to zero. References to the elements of a structure are written in a dot notation, as in for instance:

```goo.a[2] = goo.fld2.f + 12```

A variable of a user-defined type can be passed as a single argument to a new process in run statements, as shown in the example, provided that it contains no arrays. So in this case it is valid to pass the variable named foo as a parameter to the run operator, but using goo would trigger an error message from SPIN about the hidden arrays. In the next section we shall see that these structure type names can also be used as a field declarator in channel declarations.

The mechanism for introducing user-defined types allows for an indirect way of declaring multidimensional arrays, even though PROMELA supports only one-dimensional arrays as first class objects. A two-dimensional array can be created, for instance, as follows:

```typedef Array {
    byte el[4]
};
Array a[4];```
Message Channels

Message channels are used to model the exchange of data between processes. They are declared either locally or globally. In the declaration

```plaintext
chan qname = [16] of { short, byte, bool }
```

the typename chan introduces a channel declaration. In this case, the channel is named qname, and it is declared to be capable of storing up to sixteen messages. There can be any finite number of fields per message. In the example, each message is said to consist of three fields: the first is declared to be of type short, the second is of type byte, and the last is of type bool. Each field must be either a user-defined type, such as Field from the last section, or a predefined type from Table 3.1. In particular, it is not possible to use an array as a type declarator in a message field. An indirect way of achieving this effect is again to embed the array into a user-defined type, and to use the type name as the type declarator for the message field. Note also that since the type chan appears in Table 3.1, it is always valid to use chan itself as a field declarator. We can make good use of this capability to pass channel identifiers from one process to another.

The statement

```plaintext
qname!expr1,expr2,expr3
```

sends a message with the values of the three expressions listed to the channel that we just created. The value of each expression is cast to the type of the message field that corresponds with its relative position in the list of message parameters. By default [2] the send statement is only executable if the target channel is not yet full, and otherwise it blocks.

[2] This default can be changed with SPIN option -m into one where the send statement is always executable, but the message will be lost when an attempt is made to send a message to a full channel.

The statement

```plaintext
qname?var1,var2,var3
```

retrieves a message from the head of the same buffer and stores the values from the three fields into the corresponding variables.

The receive statement is executable only if the source channel is non-empty.

It is an error to send or receive either more or fewer message fields than were declared for the message channel that is addressed.

An alternative, and equivalent, notation for the send and receive operations is to use the first message field as a message type indication, and to enclose the remaining fields in parentheses, for instance, as follows:

```plaintext
qname!expr1(expr2,expr3)
```
Channel Poll Operations

It is also possible to limit the effect of a receive statement to just the copying of parameter values from message fields, without removing the message from the channel. These operations are called channel poll operations. Any receive statement can be turned into a poll operation by placing angle brackets around its list of parameters. For instance, assuming that we have declared a channel q with two message fields of type int, the receive statement

\[ q?\langle \text{eval}(y),x \rangle \]

where \( x \) and \( y \) are variables, is executable only if channel \( q \) contains at least one message and if the first field in that message has a value that is equal to the current value of variable \( y \). When the statement is executed the value of the second field in the incoming message is copied into variable \( x \), but the message itself is not removed from the channel.
Sorted Send And Random Receive

Two other types of send and receive statements are used less frequently: sorted send and random receive. A sorted send operation is written with two, instead of one, exclamation marks, as follows:

\[ qname!!msg0 \]

A sorted send operation inserts a message into the channel's buffer in numerical, rather than in FIFO, order. For instance, if a process sends the numbers from one to ten into a channel in random order, but using the sorted send operation, the channel automatically sorts them, and stores them in numerical order.

When a sorted send operation is executed, the existing contents of the target channel is scanned from the first message towards the last, and the new message is inserted immediately before the first message that follows it in numerical order. To determine the numerical order, all message fields are taken into account and are interpreted as integer values.

The counterpart of the sorted send operation is the random receive. It is written with two, instead of one, question marks:

\[ qname??msg0 \]

A random receive operation is executable if it is executable for any message that is currently buffered in a message channel (instead of being restricted to a match on the first message in the channel). In effect, the random receive operation as implemented in SPIN will always return the first message in the channel buffer that matches, so the term "random receive" is a bit of a misnomer.

Normal send and receive operations can freely be combined with sorted send and random receive operations. As a small example, if we consider the channel with the sorted list of integers from one to ten, a normal receive operation can only retrieve the first message, which will be the smallest value one. A random receive operation on the same channel would succeed for any of the values from one to ten: the message need not be at the head of the queue. Of course, a random receive operation only makes sense if at least one of the parameters is a constant, and not a variable. (Note that the value of a variable is not evaluated to a constant unless forced with an eval function.)
Rendezvous Communication

So far we have talked about asynchronous communication between processes via message channels that are declared for instance as

\[
\text{chan qname} = [N] \text{ of } \{ \text{byte} \}
\]

where \( N \) is a positive constant that defines the maximum number of messages that can be stored in the channel. A logical extension is to allow for the declaration

\[
\text{chan port} = [0] \text{ of } \{ \text{byte} \}
\]

to define a rendezvous port. The channel capacity is now zero, that is, the channel port can pass, but cannot store messages. Message interactions via such rendezvous ports are by definition synchronous. Consider the following example:

\[
\text{mtype} = \{ \text{msgtype} \};
\]

\[
\text{chan name} = [0] \text{ of } \{ \text{mtype, byte} \};
\]

\[
\text{active proctype A}() \\
\{ \\
\quad \text{name!msgtype(124)}; \\
\quad \text{name!msgtype(121)}
\}
\]

\[
\text{active proctype B}() \\
\{ \\
\quad \text{byte state}; \\
\quad \text{name?msgtype(state)}
\}
\]

Channel name is a rendezvous port. The two processes synchronously execute their first statement: a handshake on message msgtype and a transfer of the value 124 from process A into local variable state in process B. The second statement in process A is unexecutable (it blocks), because there is no matching receive operation for it in process B.

If the channel name is defined with a non-zero buffer capacity, the behavior is different. If the buffer size is at least two, the process of type A can complete its execution, before its peer even starts. If the buffer size is one, the sequence of events is as follows. The process of type A can complete its first send action, but it blocks on the second, because the channel is now filled to capacity. The process of type B can then retrieve the first message and terminate. At this point A becomes executable again and also terminates, leaving its second message as a residual in the channel.

Rendezvous communication is binary: only two processes, a sender and a receiver, can meet in a rendezvous handshake.

Message parameters are always passed by value in PROMELA. This still leaves open the possibility to pass the value of a locally declared and instantiated message channel from one process to another. The value stored in a variable of type chan is nothing other than the channel identity that is needed to address the channel in send and receive operations. Even though we cannot send the name of the variable in which a channel identity is stored, we can send the identity itself as a value, and thereby make even a local channel accessible to other processes. When the process that declares and instantiates a channel dies, though, the corresponding channel object disappears, and any attempts to access it from another process fail (causing an error that can be caught in verification mode).
Rules For Executability

The definition of PROMELA centers on its semantics of executability, which provides the basic means in the language for modeling process synchronizations. Depending on the system state, any statement in a SPIN model is either executable or blocked. We have already seen four basic types of statements in PROMELA: print statements, assignments, i/o statements, and expression statements. A curiosity in PROMELA is indeed that expressions can be used as if they were statements in any context. They are "executable" (i.e., passable) if and only if they evaluate to the boolean value true, or equivalently to a non-zero integer value. The semantics rules of PROMELA further state that print statements and assignments are always unconditionally executable. If a process reaches a point in its code where it has no executable statements left to execute, it simply blocks.

For instance, instead of writing a busy wait loop

```plaintext
while (a != b) /* while is not a keyword in Promela */
  skip; /* do nothing, while waiting for a==b */
```

we achieve the same effect in PROMELA with the single statement

```plaintext
(a == b); /* block until a equals b */
```

The same effect could be obtained in PROMELA with constructions such as

```plaintext
L:    /* dubious */
  if
    :: (a == b) -> skip
    :: else -> goto L
  fi
```

or

```plaintext
do    /* also dubious */
  :: (a == b) -> break
  :: else -> skip
od
```

but this is always less efficient, and is frowned upon by PROMELA natives. (We will cover selection and repetition structures in more detail starting at p. 56.)

We saw earlier that expressions in PROMELA must be side effect free. The reason will be clear: a blocking expression statement may have to be evaluated many times over before it becomes executable, and if each evaluation could have a side effect, chaos would result. There is one exception to the rule. An expression that contains the run operator we discussed earlier can have a side effect, and it is therefore subject to some syntactic restrictions. The main restriction is that there can be only one run operator in an expression, and if it appears it cannot be combined with any other operators. This, of course, still allows us to use a run statement as a potentially blocking expression. We can indicate this effect more explicitly if instead of writing

```plaintext
run you_run(0);      /* potentially blocking */
```

we write

```plaintext
(run you_run(0)) -> /* potentially blocking */
```

Consider, for instance, what the effect is if we use such a run expression in the following model, as a variation on the model we saw on p. 39.

```plaintext
active proctype new_splurge(int n)
{
  printf("%d\n", n);
  run new_splurge(n+1)
}
```

As before, because of the bound on the number of processes that can be running simultaneously, the 255th attempt to instantiate a new process will fail. The failure causes the run expression to evaluate to zero, and thereby it permanently blocks the process. The blocked process can now not reach the end of its code and it therefore cannot terminate or die. As a result, none of its predecessors can die either. The system of 255 processes comes to a grinding halt with 254 processes terminated but blocked in their attempt to die, and one process blocked in its attempt to start a new process.

If the evaluation of the run expression returns zero, execution blocks, but no side effects have occurred, so there is again no danger of repeated side effects in consecutive tests for executability. If the evaluation returns non-zero, there is a side effect as the execution of the statement completes, but the statement as a whole cannot block now. It would decidedly be dubious if compound conditions could be built with run operators. For instance,

```plaintext
run you_run(0) && run you_run(1) /* not valid */
```

would block if both processes could not be instantiated, but it would not reveal whether one process was created or none at all. Similarly,

```plaintext
run you_run(0) || run you_run(1) /* not valid */
```

would block if both attempts to instantiate a process fail, but if successful would not reveal which of the two processes was created.
Assignments And Expressions

As in C, the assignments

\[ c = c + 1; \ c = c - 1 \ /* \text{valid} */ \]

can be abbreviated to

\[ c++; \ c-- \ /* \text{valid} */ \]

but, unlike in C,

\[ b = c++ \]

is not a valid assignment in PROMELA, because the right-hand side operand is not a side effect free expression. There is no equivalent to the shorthands

\[ --c; ++c \ /* \text{not valid} */ \]

in PROMELA, because assignment statements such as

\[ c = c-1; \ c = c+1 \ /* \text{valid} */ \]

when taken as a unit are not equivalent to expressions in PROMELA. With these constraints, a statement such as \(--c\) is always indistinguishable from \(c--\), which is supported.

In assignments such as

\[ \text{variable} = \text{expression} \]

the values of all operands used in the expression on the right-hand side of the assignment operator are first cast to signed integers, before any of the operands are applied. The operator precedence rules from C determine the order of evaluation, as reproduced in Table 3.2. After the evaluation of the right-hand side expression completes, and before the assignment takes place, the value produced is cast to the type of the target variable. If the right-hand side yields a value outside the range of the target type, truncation of the assigned value can result. In simulation mode SPIN issues a warning when this occurs; in verification mode, however, this type of truncation is not intercepted.

It is also possible to use C-style conditional expressions in any context where expressions are allowed. The syntax, however, is slightly different from the one used in C. Where in C one would write

\[ \text{expr1} \ ? \ \text{expr2} \ : \ \text{expr3} \ /* \text{not valid} */ \]

one writes in PROMELA

\[ (\text{expr1} \to \text{expr2} : \text{expr3}) \ /* \text{valid} */ \]

The arrow symbol is used here to avoid possible confusion with the question mark from PROMELA receive operations. The value of the conditional expression is equal to the value of \(\text{expr2}\) if and only if \(\text{expr1}\) evaluates to true and otherwise it equals the value of \(\text{expr3}\). PROMELA conditional expressions must be surrounded by parentheses (round braces) to avoid misinterpretation of the arrow as a statement separator.
**Control Flow: Compound Statements**

So far, we have mainly focused on the basic statements of PROMELA, and the way in which they can be combined to model process behavior. The main types of statements we have mentioned so far are: print and assignment statements, expressions, and send and receive statements.

We saw that `run` is an operator, which makes a statement such as `run sender()` an expression. Similarly, `skip` is not a statement but an expression: it is equivalent to `(1)` or `true`.

There are five types of compound statements in PROMELA:

- Atomic sequences
- Deterministic steps
- Selections
- Repetitions
- Escape sequences

Another control flow structuring mechanism is available through the definition of macros and PROMELA inline functions. We discuss these constructs in the remaining subsections of this chapter.
Atomic Sequences

The simplest compound statement is the atomic sequence. A simple example of an atomic sequence is, for instance:

```atomic {
    /* swap the values of a and b */
    tmp = b;
    b = a;
    a = tmp
}
```

In the example, the values of two variables a and b are swapped in a sequence of statement executions that is defined to be uninterruptable. That is, in the interleaving of process executions, no other process can execute statements from the moment that the first statement of this sequence begins to execute until the last one has completed.

It is often useful to use atomic sequences to initialize a series of processes in such a way that none of them can start executing statements until the initialization of all of them has been completed:

```init {
    atomic {
        run A(1,2);
        run B(2,3)
    }
}
```

Atomic sequences may be non-deterministic. If, however, any statement inside an atomic sequence is found to be unexecutable (i.e., blocks the execution), the atomic chain is broken and another process can take over control. When the blocking statement becomes executable later, control can non-deterministically return to the process, and the atomic execution of the sequence resumes as if it had not been interrupted.

Note carefully that without atomic sequences, in two subsequent statements such as

```nfull(qname) -> qname!msg0```

or

```qname?[msg0] -> qname?msg0```

the second statement is not necessarily executable after the first one is executed. There may be race conditions when access to the channels is shared between several processes. In the first example, another process can send a message to the channel just after this process determined that it was not full. In the second example, another process can steal away the message just after our process determined its presence. On the other, it would be redundant to write

```atomic { qname?[msg0] -> qname?msg0 }
```
Deterministic Steps

Another way to define an indivisible sequence of actions is to use the d_step statement. In the above case, for instance, we could also have written:

```c
    d_step { /* swap the values of a and b */
        tmp = b;
        b = a;
        a = tmp
    }
```

Unlike an atomic sequence, a d_step sequence is always executed as if it were a single statement; it is intended to provide a means for defining new types of primitive statements in PROMELA. This restricts the use of d_step sequences in several ways, compared to atomic sequences:

- The execution of a d_step sequence is always deterministic. If non-determinism is encountered in a d_step sequence, it is resolved in a fixed way, for example, by executing the first true guard in each non-deterministic selection or repetition structure. The precise way in which the non-determinism inside d_step sequences is resolved is undefined.

- No goto jumps into or out of d_step sequences are permitted: they will be flagged as errors by the SPIN parser.

- The execution of a d_step sequence may not be interrupted by blocking statements. It is an error if any statement other than the first one (the guard statement) in a d_step sequence is found to be unexecutable.

None of the above three restrictions apply to atomic sequences. This means that the keyword d_step can always be replaced with the keyword atomic, but not vice versa. It is safe to embed d_step sequences inside atomic sequences, but the reverse is not allowed.
Selection

Using the relative values of two variables $a$ and $b$ we can define a choice between the execution of two different options with a selection structure, as follows:

```plaintext
if :: (a != b) -> option1 :: (a == b) -> option2 fi
```

The selection structure above contains two execution sequences, each preceded by a double colon. Only one sequence from the list will be executed. A sequence can be selected only if its first statement, that is, the first statement that follows the double colon, is executable. The first statement is therefore called the guard of the option sequence.

In the last example the guards are mutually exclusive, but they need not be. If more than one guard is executable, one of the corresponding sequences is selected nondeterministically. If all guards are unexecutable the process will block until at least one of them can be selected. There is no restriction on the type of statements that can be used as a guard: it may include sends or receives, assignments, printf, skip, etc. The rules of executability determine in each case what the semantics of the complete selection structure will be. The following example, for instance, illustrates the use of send statements as guards in a selection.

```plaintext
mtype = { a, b }; chan ch = [1] of { mtype }; active proctype A() { ch?a } active proctype B() { ch?b } active proctype C() { if :: ch!a :: ch!b fi }
```

The example defines three processes and one channel. The first option in the selection structure of the process of type C is executable if channel $ch$ is non-full, a condition that is satisfied in the initial state. Since both guards are executable, the process of type C can arbitrarily pick one, and execute it, depositing a message in channel $ch$. The process of type A can execute its sole statement if the message sent was an $a$, where $a$ is a symbolic constant defined in the $mtype$ declaration at the start of the model. Its peer process of type B can execute its sole statement if the message is of type $b$, where, similarly, $b$ is a symbolic constant.

If we switch all send statements for receive statements, and vice versa, we also get a valid PROMELA model. This time, the choice in C is forced by the message that gets sent into the channel, which in turn depends on the unknown relative speeds of execution of the processes of type A and B. In both versions of the model, one of the three running processes hangs at the end of system execution, and will fail to terminate.

A process of the following type either increments or decrements the value of variable count. Because assignments are always executable, the choice made here is truly a non-deterministic one that is independent of the initial value of the variable count.

```plaintext
byte count; /* initial value defaults to zero */ active proctype counter() { if :: count++ :: count-- fi }
```
Repetition

We can modify the last model to obtain a cyclic program that randomly changes the value of the variable up or down by replacing the selection structure with a repetition.

```plaintext
byte count;

active proctype counter()
{
    do
        :: count++
        :: count--
        :: (count == 0) -> break
    od
}
```

As before, only one option can be selected for execution at a time. After the option completes, the execution of the repetition structure is repeated. The normal way to terminate the repetition structure is with a break statement. In the example, the loop can be broken only when the count reaches zero. Note, however, that it need not terminate since the other two options always remain executable. To force termination we could modify the program as follows:

```plaintext
active proctype counter()
{
    do
        :: (count != 0) ->
            if
                :: count++
                :: count--
            fi
        :: (count == 0) -> break
    od
}
```

A special type of statement that is useful in selection and repetition structures is the else statement. An else statement becomes executable only if no other statement within the same process, at the same control-flow point, is executable. We could try to use it in two places in the example, as follows:

```plaintext
active proctype counter()
{
    do
        :: (count != 0) ->
            if
                :: count++
                :: count--
            fi
        :: else -> break
    od
}
```

The first else, inside the nested selection structure, can never become executable though, and is therefore redundant (both alternative guards of the selection are assignments, which are always executable). The second use of the else, however, becomes executable exactly when !(count != 0) or (count == 0), and therefore preserves the option to break from the loop.

There is also an alternative way to exit the do-loop, without using a break statement: the infamous goto. This is illustrated in the following PROMELA implementation of Euclid's algorithm for finding the greatest common divisor of two non-zero, positive numbers.

```plaintext
proctype Euclid(int x, y)
{
    do
        :: (x > y) -> x = x - y
        :: (x < y) -> y = y - x
        :: (x == y) -> goto done
    od;

done:
    printf("answer: %d\n", x)
}

init { run Euclid(36, 12) }
```

Simulating the execution of this model, with the numbers given, yields:

```
$ spin euclid.pml
answer: 12
2 processes created
```

The goto in this example jumps to a label named done. Multiple labels may be used to label the same statement, but at least one statement is required. If, for instance, we wanted to omit the printf statement behind the label, we must replace it with a dummy skip. Like a skip, a goto statement is always executable and has no other effect than to change the control-flow point of the process that executes it.

With these extra constructs, we can now also define a slightly more complete description of the alternating bit protocol (cf. p. 46).

```plaintext
{       bool seq_out, seq_in;
    do
        :: to_rcvr!msg(seq_out) ->
            to_sndr?ack(seq_in);
        if
            :: seq_in == seq_out ->
                seq_out = 1 - seq_out;
            :: else
                fi
        :: (count == 0) -> break
    od
}

active proctype Receiver()
{       bool seq_in;
    do
        :: to_rcvr?msg(seq_in) ->
            to_sndr!ack(seq_in)
        :: timeout -> /* recover from msg loss */
            to_sndr!ack(seq_in)
    od
}
```

The sender transmits messages of type msg to the receiver, and then waits for an acknowledgement of type ack with a matching sequence number. If an acknowledgement with the wrong sequence number comes back, the sender retransmits the message. The receiver can timeout while waiting for a new message to arrive, and will then retransmit its last acknowledgement.

The semantics of PROMELA's timeout statement is very similar to that of the else statement we saw earlier. A timeout is defined at the system level, though, and an else statement is defined at the process level. timeout is a predefined global variable that becomes true if and only if there are no executable statements at all in any of the currently running processes. The primary purpose of timeout is to allow us to model recovery actions from potential deadlock states. Note carefully that timeout is a predefined variable and not a function: it takes no parameters, and in particular it is not possible to specify a numeric argument with a specific timebound after which the timeout should become executable. The reason is that the types of properties we would like to prove for PROMELA models must be fully independent of all absolute and relative timing considerations. The relative speeds of processes is a fundamentally unknown and unknowable quantity in an asynchronous system.
Escape Sequences

The last type of compound structure to be discussed is the unless statement. This type of statement is used less frequently, but it requires a little more explanation. It is safe to skip this section on a first reading.

The syntax of an escape sequence is as follows:

\[
\{ P \} \text{ unless } \{ E \}
\]

where the letters P and E represent arbitrary PROMELA fragments. Execution of the unless statement begins with the execution of statements from P. Before each statement execution in P the executability of the first statement of E is checked, using the normal PROMELA semantics of executability. Execution of statements from P proceeds only while the first statement of E remains unexecutable. The first time that this 'guard of the escape sequence' is found to be executable, control changes to it, and execution continues as defined for E. Individual statement executions remain indivisible, so control can only change from inside P to the start of E in between individual statement executions. If the guard of the escape sequence does not become executable during the execution of P, then it is skipped entirely when P terminates.

An example of the use of escape sequences is:

\[
A; \\
\text{do} \\
\text{:: b1 }\rightarrow \text{ B1} \\
\text{:: b2 }\rightarrow \text{ B2} \\
\ldots \\
\text{od unless } \{ \text{ c }\rightarrow \text{ C } \}; \\
D
\]

As shown in the example, the curly braces around the main sequence (or the escape sequence) can be deleted if there can be no confusion about which statements belong to those sequences. In the example, condition c acts as a watchdog on the repetition construct from the main sequence. Note that this is not necessarily equivalent to the construct

\[
A; \\
\text{do} \\
\text{:: b1 }\rightarrow \text{ B1} \\
\text{:: b2 }\rightarrow \text{ B2} \\
\ldots \\
\text{:: c }\rightarrow \text{ break} \\
\text{od; C; D}
\]

if B1 or B2 are non-empty. In the first version of the example, execution of the iteration can be interrupted at any point inside each option sequence. In the second version, execution can only be interrupted at the start of the option sequences.

An example application of an escape sequence is shown in Figure 3.1. Shown here is a somewhat naive model of the behavior of a pots (plain old telephone service) system (cf. Chapter 14, p. 299).

Figure 3.1 Simple Model of a Telephone System
Inline Definitions

Some motivation for and examples of the use of PROMELA inline's was already given in the last chapter. The PROMELA inline is meant to provide some of the structuring mechanism of a traditional procedure call, without introducing any overhead during the verification process. The PROMELA parser replaces each point of invocation of an inline with the text of the inline body. If any parameters are used, their actual values from the call will textually replace the formal place holders that are used inside the definition of the inline body. That is, there is no concept of value passing with inline's. The parameter names used inside the definition are mere stand ins for the names provided at the place of call. A small example can clarify the working and intent of this mechanism, as follows:

```plaintext
inline example(x, y) {
    y = a;
    x = b;
    assert(x)
}
init {
    int a, b;
    example(a,b)
}
```

In this example we have defined an inline named example and we gave it two parameters. The parameters do not have a type associated with them. They could in fact be replaced in a call with variables of any type that matches the use of the names inside the inline body.

At the point of invocation the names of two variables are provided as actual parameters. The parser treats this code as if we had written the following specification instead:

```plaintext
init {
    int a, b;
    b = a;
    a = b;
    assert(a)
}
```

This version of the model is obtained by inserting the body of the inline at the point of call, while textually replacing every occurrence of the name x with the name a and every occurrence of y with b, as stipulated by the parameter list at the point of invocation.

We could have achieved the same effect by defining a C-style macro, as follows:

```plaintext
#define example(x, y) \
    y = a; \
    x = b; \
    assert(x)
init {
    int a, b;
    example(a,b)
}
```
On an initial introduction to PROMELA it may strike one as odd that there is a generic output statement to communicate information to the user in the form of the printf, but there is no matching scanf statement to read information from the input. The reason is that we want verification models to be closed to their environment. A model must always contain all the information that could possibly be required to verify its properties. It would be rather clumsy, for instance, if the model checker would have to be stopped dead in its tracks each time it needed to read information from the user’s keyboard.

Outputs, like printf, are harmless in this context, since they generate no new information that can affect future behavior of the executing process, but the executing of an input statement like scanf can cause the modification of variable values that can impact future behavior. If input is required, its source must always be represented in the model. The input can then be captured with the available primitives in PROMELA, such as sends and receives.

In one minor instance we deviate from this rather strict standard. When SPIN is used in simulation mode, there is a way to read characters interactively from a user-defined input. To enable this feature, it suffices to declare a channel of the reserved type STDIN in a PROMELA model. There is only one message field available on this predefined channel, and it is of type int. The model in Figure 3.2 shows a simple word count program as an example.

**Figure 3.2 Word Count Program Using STDIN Feature**

```pml
can STDIN;
int c, nl, nw, nc;
init {
    bool inword = false;
    do
        :: STDIN?c ->
            if
                :: c == -1 ->
                    break /* EOF */
                :: c == '\n' ->
                    nc++;
                    nl++
                :: else ->
                    nc++
            fi;
        if
            :: c == ' '
            || c == '\t'
            || c == '\n' ->
                inword = false
            :: else ->
                if
                    :: !inword ->
                        nw++;
                        inword = true
                    :: else /* do nothing */
                fi
            od;
    assert(nc >= nl);
    printf("%d\t%d\t%d\n", nl, nw, nc)
}
```

We can simulate the execution of this model (but not verify it) by invoking SPIN as follows, feeding the source text for the model itself as input.

```
$ spin wc.pml < wc.pml
27      85         699
1 process created
```

PROMELA supports a small number of other special purpose keywords that can be used to fine-tune verification models for optimal performance of the verifiers that can be generated by SPIN. We mention the most important of these here. (This section can safely be skipped on a first reading.)
Special Features

The verifiers that can be generated by SPIN by default apply a partial order reduction algorithm that tries to minimize the amount of work done to prove system properties. The performance of this algorithm can be improved, sometimes very substantially, if the user provides some hints about the usage of data objects. For instance, if it is known that some of the message channels are only used to receive messages from a single source process, the user can record this knowledge in a channel assertion.

In the example shown in Figure 3.3, for instance, the number of states that has to be searched by the verifier is reduced by 16 percent if the lines containing the keywords xr and xs are included. (The two keywords are acronyms for exclusive read access and exclusive write access, respectively.) These statements are called channel assertions.

Figure 3.3 Using Channel Assertions

mtype = { msg, ack, nak };
chan q = [2] of { mtype, byte };
chan r = [2] of { mtype };
active proctype S()
{       byte s = 1;
          xs q; /* assert that only S sends to chan q */
          xr r; /* and only S receives from chan r */
          do
            :: q!msg(s);
            if
              :: r?ack; s++
              :: r?nak
              fi
          od
}
active proctype R()
{      byte ns, s;
   xs r; /* only R sends messages to chan r */
   xr q; /* only R retrieves messages from chan q */
   do
     :: q?msg(ns);
     if
       :: (ns == s+1) -> s = ns; r!ack
       :: else -> r!nak
       fi
     od
}

The statements are called assertions because the validity of the claims they make about channel usage can, and will, be checked during verifications. If, for instance, it is possible for a process to send messages to a channel that was claimed to be non-shared by another process, then the verifier can always detect this and it can flag a channel assertion violation. The violation of a channel assertion in effect means that the additional reduction that is based on its presence is invalid. The correct counter-measure is to then remove the channel assertion.

The reduction method used in SPIN (more fully explained in Chapter 9) can also take advantage of the fact that the access to local variables cannot be shared between processes. If, however, the verification model contains a globally declared variable that the user knows to be non-shared, the keyword local can be used as a prefix to the variable declaration. For instance, in the last example we could have declared the variable ns from proctype R as a global variable, without incurring a penalty for this change from the partial order reduction algorithm, by declaring it globally as:
Finding Out More

This concludes our overview of the main features of the PROMELA specification language. A few more seldomly used constructs were only mentioned in passing here, but are discussed in greater detail in the manual pages that are included in Chapters 16 and 17. More examples of PROMELA models are included in Chapters 14 and 15. A definition of the operational semantics for PROMELA can be found in Chapter 7.

Alternate introductions to the language can be found in, for instance, Ruys [2001] and Holzmann [1991]. Several other tutorial-style introductions to the language can also be found on the SPIN Web site (see Appendix D).
Chapter 4. Defining Correctness Claims

If the odds are a million to one against something occurring, chances are fifty-fifty that it will.

—(Folklore wisdom)

The goal of system verification is to establish what is possible and what is not. Often, this assessment of what is logically possible will be subject to some set of assumptions about the context in which a system executes, such as the possible behavior of external components that the system will be interacting with. When performing logical verification we are especially interested in determining whether design requirements could possibly be violated, not necessarily in how likely or unlikely such violations might be. Dramatic system failures are almost always the result of seemingly unlikely sequences of events: that is precisely why these sequences of events are often overlooked in the design phase. Once we understand how a requirement may be violated, we can reconsider the original design decisions made, and devise alternate strategies that can prevent the error from occurring. Logical correctness, then, is concerned primarily with possibilities, not with probabilities.
Stronger Proof

This restriction to the possible, rather than the probable, has two implications. For one, it can strengthen the proofs of correctness we can achieve with system verification. If the verifier tells us that there is no possible violation of a given requirement, this is a significantly stronger result than the verdict that violating executions have a low probability of occurrence. Secondly, the restriction makes it possible to perform verification more efficiently than if we attempted to consider also the probability of execution scenarios. The results of probability estimates are further undermined by the difficulty one would face in deriving accurate metrics for the probabilities of execution of specific statements in the system. Any errors of judgment made here are magnified in the verification process, limiting the value of the final results.

We should be able to prove the essential logical correctness properties of a distributed system independently of any assumption about the relative speeds of execution of processes, the time it takes to execute specific instructions, or the probability of occurrence of particular types of events, such as the loss of messages on a transmission channel or the failure of external devices.

The proof of correctness of an algorithm is ideally also implementation independent. Specifically, the correctness of the algorithm should not depend on whether it is implemented on a fast machine or on a slow machine. In the verification process, therefore, we should not rely on such assumptions. It is even desirable that we cannot make such statements at all. Not surprisingly, PROMELA effectively makes it impossible to state any correctness requirement that would violate these rules.

The rules we follow here are specific to our area of interest: the verification of distributed systems software. Different rules apply in, for instance, hardware verification. The correctness of a chip may well depend critically, and unavoidably, on signal propagation delays and the speed of individual circuit elements. Signal propagation times and the layout of circuit elements are part of a chip's design and functionality: they cannot be changed independently from it. The correctness of a data communications protocol or a distributed operating system, on the other hand, should never depend on such issues. The speed of execution of a software system is almost guaranteed to change dramatically over the lifetime of the design.
Basic Types of Claims

In distributed systems design it is standard to make a distinction between two types of correctness requirements: safety and liveness. Safety is usually defined as the set of properties that the system may not violate, while liveness is defined as the set of properties that the system must satisfy. Safety, then, defines the bad things that should be avoided, and liveness defines the good things that capture the required functionality of a system. The function of a verification system, however, is not as lofty. It need not, and indeed cannot, determine what is good or bad; it can only help the designer to determine what is possible and what is not.

From the point of view of the verifier there are also two types of correctness claims: claims about reachable or unreachable states and claims about feasible or infeasible executions (i.e., sequences of states). The former are sometimes called state properties and the latter path properties. Paths, or executions, can be either finite or infinite (e.g., cyclic).

A simple type of state property is a system invariant that should hold in every reachable state of the system. A slightly weaker version is a process assertion that should hold only in specific reachable states. State properties can be combined to build path properties. An example of a path property is, for instance, that every visit to a state with property \( P \) must eventually be followed by a visit to a state with property \( Q \), without in the interim visiting any state with property \( R \). The verifier SPIN can check both state and path properties, and both can be expressed in the specification language PROMELA.

Some types of properties are so basic that they need not be stated explicitly. SPIN checks them by default. One such property is, for instance, the absence of reachable system deadlock states. The user can, however, modify the semantics of also the built-in checks through a simple form of statement labeling. A deadlock, for instance, is by default considered to be an unintended end state of the system. We can tell the verifier that certain specific end states are intended by placing end-state labels, as we shall see shortly.

Correctness properties are formalized in PROMELA through the use of the following constructs:

- Basic assertions
- End-state labels
- Progress-state labels
- Accept-state labels
- Never claims
- Trace assertions

Never claims can be written by hand, or they can (often more easily) be automatically generated from logic formulae or from timeline property descriptions. We will discuss each of these constructs in more detail below.
Basic Assertions

Statements of the form

\[ \text{assert(expression)} \]

are called basic assertions in PROMELA to distinguish them from trace assertions that we will discuss later. The usefulness of assertions of this type was recognized very early on. A mention of it can even be found in the work of John von Neumann (1903-1957). It reads as follows. Of course, the letter \( C \) that is used here does not refer to a programming language that would be created some 30 years later:

It may be true, that whenever \( C \) actually reaches a certain point in the flow diagram, one or more bound variables will necessarily possess certain specified values, or possess certain properties, or satisfy certain relations with each other. Furthermore, we may, at such a point, indicate the validity of these limitations. For this reason we will denote each area in which the validity of such limitations is being asserted, by a special box, which we call an 'assertion box.'

— Goldstein and von Neumann, 1947

PROMELA basic assertions are always executable, much like assignments, and print or skip statements. The execution of this type of statement has no effect provided that the expression that is specified evaluates to the boolean value true, or alternatively to a non-zero integer value. The implied correctness property is that it is never possible for the expression to evaluate to false (or zero). A failing assertion will trigger an error message.

As also noted in Chapter 2 (p. 18), the trivial model:

\[ \text{init} \{ \text{assert(false)} \} \]

results in the following output when executed:

$ spin false.pml
spin: line 1 "false.pml", Error: assertion violated
#processes: 1
  1: proc 0 (:init:) line 1 "false.pml" (state 1)
1 process created

Here SPIN is used in simulation mode. Execution stops at the point in the model where the assertion failure was detected. When the simulation stops, the executing process, with pid zero, is at the internal state numbered one. The simulator will always list the precise state at which execution stops for all processes that have been initiated but that have not yet died. If we change the expression used in the assertion to true, no output of note will appear, because there are no running processes left when the execution stops with the death of the only process.

$ spin true.pml
1 process created

An assertion statement is the only type of correctness property in PROMELA that can be checked during simulation runs with SPIN. All other properties discussed in this chapter require SPIN to be run in verification mode to be checked. If SPIN fails to find an assertion violation in any number of simulation runs, this does not mean that the assertions that are embedded in the model that is simulated cannot be violated. Only a verification run with SPIN can establish that result.
Meta Labels

Labels in a PROMELA specification ordinarily serve merely as targets for unconditional goto jumps. There are three types of labels, though, that have a special meaning when SPIN is run in verification mode. The labels are used to identify:

- End states
- Progress states
- Accept states

End States:

When a PROMELA model is checked for reachable deadlock states, using SPIN in verification mode, the verifier must be able to distinguish valid system end states from invalid ones. By default, the only valid end states, or termination points, are those in which every PROMELA process that was instantiated has reached the end of its code (i.e., the closing curly brace in the corresponding proctype body). Not all PROMELA processes, however, are meant to reach the end of their code. Some may very well linger in a known wait state, or they may sit patiently in a loop ready to spring back to action when new input arrives.

To make it clear to the verifier that these alternate end states are also valid, we can define special labels, called end-state labels. We have done so, for instance, in Figure 4.1 in process type Dijkstra, which models a semaphore with the help of a rendezvous port sema. The semaphore guarantees that only one of three user processes can enter its critical section at a time. The end label defines that it is not an error if, at the end of an execution sequence, the process has not reached its closing curly brace, but waits at the label. Of course, such a state could still be part of a deadlock state, but if so, it is not caused by this particular process.

Figure 4.1 Labeling End States

mtype { p, v };
chan sema = [0] of { mtype };

active proctype Dijkstra()
{
    byte count = 1;

    end: do
        :: (count == 1) ->
            sema!p; count = 0
        :: (count == 0) ->
            sema?v; count = 1
        od
}

active [3] proctype user()
{
    do
        :: sema?p; /* enter */
    critical: skip; /* leave */
        sema?v;
    od
}

There can be any number of end-state labels per PROMELA model, provided that all labels that occur within the same proctype body remain unique.
Fair Cycles

The counterexample shows an infinite execution of the process of type B alone, without participation of any other process in the system. Given the fact that SPIN does not allow us to make any assumptions about the relative speeds of execution of processes, the special-case where the process of type A pauses indefinitely is allowed, and so the counterexample is valid. Still, there may well be cases where we would be interested in the existence of property violations under more realistic fairness assumptions. One such assumption is the finite progress assumption. It says that any process than can execute a statement will eventually proceed with that execution.

There are two variations of this assumption. The stricter version states that if a process reaches a point where it has an executable statement, and the executability of that statement never changes, it will eventually proceed by executing the statement. A more general version states that if the process reaches a point where it has a statement that becomes executable infinitely often, it will eventually proceed by executing the statement. The first version is commonly referred to as weak fairness and the second as strong fairness. In our example enforcing weak fairness in the search for non-progress cycles would rule out the counterexample that is reported in the default search. We can enforce the weak fairness rule as follows during the verification:

$ ./pan -l -f
pan: non-progress cycle (at depth 8)
pan: wrote fair.pml.trail
(Spin Version 4.0.7 -- 1 August 2003)
Warning: Search not completed
+ Partial Order Reduction

Full statespace search for:
nevef claim +
assertion violations + (if within scope of claim)
non-progress cycles + (fairness enabled)
invalid end states - (disabled by never claim)

State-vector 24 byte, depth reached 15, errors: 1
4 states, stored (12 visited)
9 states, matched
21 transitions (= visited+matched)
0 atomic steps
hash conflicts: 0 (resolved)
(max size 2^18 states)
1.573 memory usage (Mbyte)

The new cycle that is reported here should now be consistent with the weak fairness finite progress assumption. A quick look at the new counterexample can confirm this.

$ spin -t -p fair.pml
spin: couldn't find claim (ignored)
  2: proc 1 (B) line 12 "fair.pml" (state 1) [x = (3-x)]
  4: proc 1 (B) line 12 "fair.pml" (state 1) [x = (3-x)]
  6: proc 1 (B) line 12 "fair.pml" (state 1) [x = (3-x)]
  8: proc 0 (A) line 6 "fair.pml" (state 1) [x = (3-x)]
<<<<START OF CYCLE>>>>>
  10: proc 1 (B) line 12 "fair.pml" (state 1) [x = (3-x)]
  12: proc 1 (B) line 12 "fair.pml" (state 1) [x = (3-x)]
  14: proc 1 (B) line 12 "fair.pml" (state 1) [x = (3-x)]

  16: proc 0 (A) line 6 "fair.pml" (state 1) [x = (3-x)]
spin: trail ends after 16 steps
#processes: 2
Never Claims

Up to this point we have talked about the specification of correctness criteria with assertion statements and with meta labels. Powerful types of correctness criteria can already be expressed with these tools, yet so far our only option is to add them into the individual proctype declarations. We cannot easily express the claim, "every system state in which property p is true eventually leads to a system state in which property q is true." The reason we cannot check this property with the mechanisms we have described so far is that we have no way yet of defining a check that would be performed at every single execution step of the system. Note that we cannot make assumptions about the relative speeds of processes, which means that in between any two statement executions any standard PROMELA process can pause for an arbitrary number of steps taken by other system processes. PROMELA never claims are meant to give us the needed capability for defining more precise checks.

In a nutshell: a never claim is normally used to specify either finite or infinite system behavior that should never occur.

How a Never Claim Works

Consider the following execution of the little pots model from the Chapter 3 (p. 64).

```
$ spin -c pots.pml | more
proc 0 = pots
proc 1 = subscriber
q 0 1
 2 . line!offhook,1
 2 line?offhook,1
 1 who!dialtone
 1 . me?dialtone
 1 . me!number
 1 who?number
 1 who!ringing
 1 . me?ringing
 1 who!connected
 1 . me?connected
timeout
 1 . me!hangup
 1 who?hangup
 2 . line!offhook,1
 2 line?offhook,1
 1 who!dialtone
 1 . me?dialtone
 1 . me!number
 1 who?number
 1 who!ringing
 1 . me?ringing
 1 . me!hangup
 1 who?hangup
```

There are twenty-four system execution steps here. Eleven statements were executed by the pots server and thirteen were executed by the subscriber process. Because this is a distributed system, not only the specific sequence of statements executed in each process, is important, but also the way in which these statement executions are interleaved in time to form a system execution.

A never claim gives us the capability to check system properties just before and just after each statement execution, no matter which process performs them. A never claim can define precisely which properties we would like to check at each step. The simplest type of claim would be to check a single property p at each and every step, to make sure that it never fails. It is easy to check system invariants in this way.

A claim to check such an invariant property could be written in several ways. Originally, a never claim was only
The Link With LTL

Never claims provide a powerful mechanism for expressing properties of distributed systems. Admittedly, though, it can be hard to come up with correct formalizations of system properties by directly encoding them into never claims. Fortunately, there are easier ways to do this. One such method is to use SPIN’s built-in translator from formulae in linear temporal logic (LTL) to never claims. The last claim, for instance, corresponds to the LTL formula

\[
\neg[\neg(p \rightarrow (p \lor q))]
\]

We can generate the never claim from this formula with the command:

```
$ spin -f '!![\neg(p \rightarrow (p \lor q))]'
```

Another method is to use a little graphical tool, called the timeline editor, to convert timeline descriptions into never claims. In many cases, temporal logic formulae are simpler to understand and use than never claims, but they are also strictly less expressive. Timeline properties, in turn, are simpler to understand and use than temporal logic formulae, but again less expressive than these. Fortunately, almost all properties of interest can be expressed as either timeline properties or temporal logic formulae. We will discuss temporal logic in more detail in Chapter 6, and the various methods to generate never claims mechanically from either formulae or timelines in, respectively, Chapter 6 (p. 127) and Chapter 13 (p. 283).
Trace Assertions

Like never claims, a trace assertion does not specify new behavior, but instead expresses a correctness requirement on existing behavior in the remainder of the system. A trace assertion expresses properties of message channels, and in particular it formalizes statements about valid or invalid sequences of operations that processes can perform on message channels.

All channel names referenced in a trace assertion must be globally declared, and all message fields must be globally known constants or mtype symbolic constants. A simple example of a trace assertion is as follows:

```plaintext
trace {
  do
    :: q1!a; q2?b
  od
}
```

In this example, the assertion specifies the correctness requirement that send operations on channel q1 alternate with receive operations on channel q2, and furthermore that all send operations on q1 are exclusively messages of type a, and all receive operations on channel q2 are exclusively messages of type b.

Trace assertions apply only to send and receive operations on message channels. They can be used to specify a specific relative order in which these types of operations must always be performed. Only the channel names that are specified in the assertion are considered to be within the scope of the check. All send and receive operations on other channels are ignored. The trace assertion trivially defines an automaton that can step through a finite number of control states while it monitors a system execution. The automaton only changes state when a send or a receive operation is executed that is within its scope. If an operation is executed that is within scope, but that cannot be matched by a transition of the trace automaton, the verifier will immediately report an error.

If at least one send (receive) operation on a channel appears in a trace assertion, then all send (receive) operations on that channel are subject to the check.

As with never claims, there are some restrictions on the types of statements that can appear in a trace assertion. Apart from control-flow constructs, a trace assertion may contain only simple send and receive operations. It cannot contain variations such as random receive, sorted send, or channel poll operations. No data objects can be declared or referred to inside a trace assertion.

If a message field must be matched in a send or receive operation that appears inside a trace assertion, it must be specified with a standard mtype name or with a constant value. Don't care values for specific message fields can be specified with the predefined write-only variable _ (i.e., the underscore symbol).

Sends and receives that appear in an event trace are called monitored events. These events do not generate new behavior, but they are required to match send or receive events on the same channels in the model, with matching message parameters. A send or receive event occurs when a send or a receive statement is executed in the system, that is, an event that occurs during a state transition.

On rendezvous channels, a rendezvous handshake consists of an offer (the send half of the handshake) and an accept (the receive half of the handshake). Even traces can only capture the occurrence of the receive part of a handshake, not of the send part. The reason is that the send (the offer) can be made many times before it results in a successful accept.

A trace assertion can contain end-state, progress-state, and accept-state labels with the usual interpretation. There are, however, a few important differences between trace assertions and never claims:

- Unlike never claims, trace assertions must always be deterministic.
- A trace assertion can match event occurrences that occur in the transitions between system states, whereas a never claim matches propositional values on system states only.
- A trace assertion monitors only a subset of the events in a system: only those of the types that are mentioned in the trace (i.e., the monitored events). A never claim, on the other hand, looks at all global system states that are reached, and must be able to match the state assignments in the system for every state reached.

A trace assertion, just like a never claim, has a current state, but it only executes transitions if a monitored event occurs in the system. Unlike never claims, trace assertions do not execute synchronously with the system; they only execute when events of interest occur.

Note that receive events on rendezvous channels can be monitored with trace assertions, but not with never claims.
Notrace

Sometimes it is desirable to specify precisely the opposite of a trace assertion: a sequence of events that should not occur in an execution. For this purpose the keyword notrace is also supported, though it is only rarely used. A notrace assertion is violated if the event sequence that is specified, subject to the same rules as trace assertions, is matched completely. The assertion is considered to be matched completely when either an end-state label is reached inside the notrace sequence, or the closing curly brace of that sequence is reached.
Predefined Variables and Functions

Some predefined variables and functions can be especially useful in trace assertions and never claims.

There are only four predefined variables in PROMELA. They are:

- `np_`
- `_pid`
- `_last`

We have discussed the `_pid` variable before (p. 16, 36), as well as the global write-only variable `_` (p. 92). These two variables can be used freely in any proctype declaration.

But we have not encountered the two variables `np_` and `_last` before. These two variables are meant to be used only inside trace assertions or never claims.

The predefined variable `np_` holds the boolean value false in all system states where at least one running process is currently at a control-flow state that was marked with a progress label. That is, the value of variable `np_` tells whether the system is currently in a progress or a non-progress state. We can use this variable easily to build a never claim that can detect the existence of non-progress cycles, for instance, as follows:

```pml
never { /* non-progress cycle detector */
  do
    :: true
    :: np_ -> break
  od;
  accept:
    do
      :: np_  
    od
}
```

After a finite prefix of arbitrary length, optionally passing through any finite number of non-progress states, the claim automaton moves from its initial state to the final accepting state, where it can only remain if there exists at least one infinitely long execution sequence that never traverses any more progress states.

The true purpose of the `np_` variable is not in the definition of this claim, since this precise claim is used automatically when SPIN’s default search for non-progress cycles is invoked. The availability of the variable makes it possible to include the non-progress property into other more complex types of temporal properties. A standard application, for instance, would be to search for non-progress cycles while at the same time enforcing non-standard fairness constraints.

The predefined global variable `_last` holds the instantiation number of the process that performed the last step in a system execution sequence. Its value is not part of the system state unless it is explicitly used in a specification. Its initial value is zero.

The use of the following three predefined functions is restricted to never claims:

```pml
pc_value(pid)
enabled(pid)
procname[pid]@label
```
Remote Referencing

In SPIN version 4.0 and higher (cf. Chapters 10 and 17), another type of reference is also supported. The additional type of reference bypasses the standard scope rules of PROMELA by making it possible for any process, and also the never claim, to refer to the current value of local variables from other processes. This capability should be used with caution, since it conflicts with the assumptions about scope rules that are made in SPIN's partial order reduction strategy (see Chapter 9).

The syntax is the same as for remote label references, with the replacement of the "@" symbol for a single colon ":".

For instance, if we wanted to refer to the variable count in the process of type Dijkstra in the example on page 77, we could do so with the syntax

\[ \text{Dijkstra}[0]:\text{count} \]

If there is only one instantiation of proctype Dijkstra, we can again use the shorter version

\[ \text{Dijkstra}:\text{count} \]

following the same rules as before.
Path Quantification

We will discuss the verification algorithms used in SPIN in more detail in later chapters, but we can already note a few important features of the approach taken. All correctness properties that can be verified with the SPIN system can be interpreted as formal claims that certain types of behavior are, or are not, possible.

- An assertion statement formalizes the claim that it is impossible for the given expression to evaluate to false.
- An end label states that it is impossible for the system to terminate without all active processes having either terminated or stopped at one of the specially labeled end states.
- A progress label states that it is impossible for the system to execute forever without also passing through at least one of the specially labeled progress states infinitely often.
- An accept label states that it is impossible for the system to execute forever while also passing through at least one of the specially labeled accept states infinitely often.
- A never claim states that it is impossible for the system to exhibit, either infinite or finite, behavior that completely matches the behavior that is formalized by the claim.
- A trace assertion, finally, states that it is impossible for the system to deviate from the behavior that is formalized.

In all cases, the verification performed by SPIN is designed to prove the user wrong: SPIN will try its best to find a counterexample to at least one of the formal claims that is stated. So, in a way SPIN never tries to prove the correctness of a specification. It tries to do the opposite.

Hunting for counterexamples, rather than direct proof, has advantages. Specifically, it can allow the verifier to employ a more efficient search procedure. If, for instance, the error behavior is formalized in a never claim, SPIN can restrict its search for counterexamples to the behaviors that match the claim. never claims, then, in a way act as a restriction on the search space. If the error behavior is indeed impossible, as the user claims, the verifier may have very little work to do. If the error behavior is almost impossible, it may have to do a little more work, but still not necessarily as much as when it has to search the entire space of all possible behaviors. This only happens in the worst case.
Formalities

Let E be the complete set of all possible $\omega$-runs of the system. Given a correctness property $\phi$ formalized as an LTL property, we say that the system satisfies $\phi$ if and only if all runs in E do. We can express this as

**Equation 4.1**

$$ (E \models \phi) \iff \forall \sigma, (\sigma \in E \rightarrow \sigma \models \phi) . $$

SPIN, however, does not attempt to prove this directly. We can only use SPIN in an attempt to disprove the claim by trying to find a counterexample that shows that $\neg \phi$ is satisfied for at least one run. That is, instead of proving [4.1] directly, SPIN tries to show the opposite

**Equation 4.2**

$$ \neg (E \models \phi) \iff \exists \sigma, (\sigma \in E \land \neg (\sigma \models \phi)) $$

where of course $\neg (\sigma \models \phi)$ means that $(\sigma \models \neg \phi)$.

If the attempt to show that the right-hand side of [4.2] holds succeeds, we have shown that $\neg (E \models \phi)$, and therefore that the left-hand side of [4.1] does not hold: the system does not satisfy the property.

If the attempt to find a counterexample fails, we have shown that the left-hand side of [4.2] does not hold, and therefore that the left-hand side of [4.1] must hold: the system satisfies the property.

This all looks fairly straightforward, but note carefully that the step from [4.1] to [4.2] cannot be achieved by the mere negation of property $\phi$. If, for instance, instead of property $\phi$ we try to prove with the same procedure that $\neg \phi$ is satisfied, then [4.1] becomes

**Equation 4.3**

$$ (E \models \neg \phi) \iff \forall \sigma, (\sigma \in E \rightarrow (\sigma \models \neg \phi)) . $$

which is the same as

**Equation 4.4**

$$ (E \models \neg \phi) \iff \forall \sigma, (\sigma \in E \rightarrow \neg (\sigma \models \phi)) . $$

Note that the right-hand sides of [4.2] and [4.4] differ. The logical negation of the right-hand side of [4.1] is the right-hand side of [4.2], and not the right-hand side of [4.4]. In other words, $(E \models \neg \phi)$ is not the same as $\neg (E \models \phi)$. The first equation does logically imply the second, but the reverse is not necessarily true:

**Equation 4.5**

$$ (E \models \neg \phi) \rightarrow \neg (E \models \phi) . $$

It is not too hard to come up with examples where we have simultaneously:

**Equation 4.6**

```
byte x = 1;
init {
    do :: x = 0 :: x = 2 od
}
#define p      (x != 0)
#ifdef PHI
    never {    /* \[\]p */
        accept:
        do :: (p) od
    }
#else
    never {     /* !\[\]p */
        do :: !p -> break :: true od
    }
#endif
```
Finding Out More

This concludes our overview of the various ways for expressing correctness requirements that are supported in PROMELA. More information about the derivation of never claims from Linear Temporal Logic formulae can be found in Chapter 6. More about the specification of requirements for a SPIN verification in a more intuitive, graphical format can be found in Chapter 13 where we discuss the timeline editing tool.

We have seen in this chapter that there are many different ways in which correctness requirements can be expressed. Be reassured, though, that the most easily understood mechanism for this purpose is also the most commonly used: the simple use of assertions.

The terms safety and liveness were first systematically discussed by Leslie Lamport, cf. Lamport [1983], and see also Alpern and Schneider [1985,1987]. An excellent introduction to the formalization of correctness properties for distributed systems can be found in Manna and Pnueli [1995]. Many other textbooks contain excellent introductions to this material; see, for instance, Berard et al. [2001], Clarke et al. [2000], or Huth and Ryan [2000].

A more detailed treatment of the differences between various ways of specifying, for instance, system invariants in PROMELA can be found in Ruys [2001].
Chapter 5. Using Design Abstraction

"Seek simplicity, and distrust it."

—(Alfred North Whitehead, 1861–1947)

System design is a process of discovery. By exploring possible solutions, a designer discovers the initially unknown constraints, and weeds out the designs that seemed plausible at first, but that do not survive closer scrutiny. In the process, the designer determines not only what is right and what is wrong, but also what is relevant and what is irrelevant to the basic design premises.

For a design tool to be effective in this context, it needs to be able to assist the designer in the creation and the analysis of intuitive high-level abstractions without requiring the resolution of implementation-level detail. The tool should be able to warn when the design premises are logically flawed, for instance, when the design is ambiguous, incomplete, or inconsistent, or when it does not exhibit the properties it was designed to have. To use such a tool well, the designer should be comfortable building and checking design abstractions. This task is sufficiently different from the task of building design implementations that it is worth a closer look.
What Makes a Good Design Abstraction?

The purpose of a design model is to free a designer from having to resolve implementation-level details before the main design premises can be checked. SPIN not only supports design abstractions, it requires them. At first sight, SPIN’s input language may look like an imperative programming language, but it intentionally excludes a number of features that would be critical to an implementation language. It is not directly possible, for instance, to express floating point arithmetic, process scheduling, or memory management operations. Although all of these things can be important in an implementation, they can and should be abstracted from a high-level design model. Note that in much the same vein, most of today’s higher-level programming languages make it impossible to express decisions on register allocation, or the management of instruction caches. These issues, though important, are best resolved and checked at a different level of abstraction.

So, what makes a good design abstraction in concurrent systems design? The focus on concurrent systems has important implications. In a sequential application, the best abstraction is typically data-oriented. In a concurrent application the preferred abstraction is control-oriented.
Data and Control

A large sequential program is typically divided into smaller modules, each performing a well-defined computational function. The interfaces between these modules are kept as small as possible, reducing the number of assumptions that one module must make about the others. The interface definitions in this case are data-oriented, not control-oriented. The modules in a sequential application typically do not maintain internal state information independently from the rest of the program.

This is different in distributed systems design. In a distributed system, the module structure is typically determined by an externally imposed system architecture (e.g., determined by a physical separation of the main components of the system). Each module then has its own independent thread of control, which necessarily carries state information. In this case control, not data, is the primary concern in the definition of module interfaces.

In a SPIN verification model the focus is on the control aspects of a distributed application, not on the computational aspects. PROMELA allows us to express the assumptions that are made within each module about the interactions with other modules. The language discourages the specification of detailed assumptions about process-internal computations.

To make sure that the models we can specify in PROMELA always have effectively verifiable properties, we impose two requirements:

- the model can only specify finite systems, even if the underlying application is potentially infinite, and
- the model must be fully specified, that is, it must be closed to its environment.

The second requirement says that the behavior that is defined in a verification model may not depend on any hidden assumptions or components. All input sources must be part of the model, at least in abstract form.

For arbitrary software applications these two requirements are not automatically satisfied. To achieve verifiability, we have to apply abstraction.

A program that allows unrestricted recursion, or that contains unbounded buffers, for instance, is not finite-state. A program that reads input from a file-descriptor or an input-stream, similarly, is not closed to its environment. These programs cannot be verified with automatic techniques unless some abstractions are made.

The need for abstraction, or modeling, is often seen as a hurdle instead of a feature in model checking applications. Choosing the right level of abstraction, though, can mean the difference between a tractable model with provable properties and an intractable model that is only amenable to simulation, testing, or manual review. Sometimes we have to choose between proving simple properties of a complex model, formalized at a low-level abstraction, and proving more complex properties of a simpler model, formalized at a higher-level abstraction.

The importance of abstraction places demands on the design of the input language of a model checking tool. If the input language is too detailed, it discourages abstractions, which in the end obstructs the verification process. We have to be careful, therefore, in choosing which features are supported in a verification system. In SPIN, for instance, a number of otherwise desirable language features have been left out of the specification language. Among them are support for memory management, floating point calculations, and numerical analysis. Other verification systems are even more restrictive, and exclude also structured data types, message passing, and process creation. Still other systems are more permissive, and, at the price of increased complexity, include support for: real-time verification, probabilities, and procedures. All other things being equal, we should expect the most permissive system to be the easiest to build models for, but the least efficient to verify them. SPIN attempts to find a balance between ease of use and model checking efficiency.

The recommended way to develop a verification model is as follows:

-
The Smallest Sufficient Model

It is sometimes easy to lose sight of the one real purpose of using a model checking system: it is to verify system properties that cannot be verified adequately by other means. If verification is our objective, computational complexity is our foe. The effort of finding a suitable design abstraction is therefore the effort of finding the smallest model that is sufficient to verify the properties that we are interested in. No more, and no less. A one-to-one translation of an implementation into a verification modeling language such as PROMELA may pass the standard of sufficiency, but it is certainly not the smallest such model and may cause unnecessary complexity in verification, or even render the verification intractable. To reduce verification complexity we may sometimes choose to generalize a problem, and sometimes we may choose to specialize it.

As the difference between a verification model and an implementation artifact becomes larger, one may well question if the facts that we are proving still have relevance. We take a very pragmatic view of this here. For our purposes, two models are equivalent if they have the same properties. This means that we can always simplify a verification model if its properties of interest are unaffected by the simplifications. A verification system, for that matter, is effective if it can be used to uncover real defects in real systems. There is little doubt that the verification methodology we are discussing here can do precisely that.
Avoiding Redundancy

The success of the model checking process for larger applications relies on our skill in finding and applying abstractions. For smaller applications this skill amounts mostly to avoiding simple cases of redundancy. It should be noted, for instance, that paradigms that are commonly used in simulation or testing can be counterproductive when used in verification. A few examples will suffice to make this point.
Counters

In the construction of a simulation model it is often convenient to add counters, for instance, to keep track of the number of steps performed. The counter is basically a write-only variable, used only in print statements.

The example in Figure 5.1 illustrates a typical use. The variable cnt is used here as if it were a natural number with infinite range. No check for overflow, which will inevitably occur, is made. The implicit assumption that in practical cases overflow is not likely to be a concern may be valid in program testing or simulation; it is false in verifications where all possible behaviors must be taken into account.

Figure 5.1 Counter Example

```
active proctype counter ()
{   int cnt = 1;

   do
    :: can_proceed ->
    /* perform a step */
    cnt++;
    printf("step: %d\n", cnt)
   od
}
```

It should be noted carefully that it is not necessarily a problem that the variable cnt may take up to 32 bits of storage to maintain its value. The real problem is that this variable can reach 232 distinct values (over four billion). The complexity of the verification problem may be increased by that same amount. Phrased differently: Removing a redundant counter can reduce the complexity of a naive verification model by about nine orders of magnitude.
Sinks, Sources, and Filters

Another avoidable source of complexity is the definition of processes that act solely as a source, a filter, or a sink for a message stream. Such processes often add no refutation power to a verification model, and are almost always better avoided.[1]

[1] The exception would be if a given correctness property directly depends on the process being present in the model. This should be rare.

- A sink process, for instance, merely receives and then discards messages. Since the messages are discarded in the model, they should probably not even be sent within the model. Having them sent but not processed would indicate an incomplete abstraction.

- A source process generates a set of possible messages that is then forwarded to a given destination. If the sole function of the source process is to provide the choice of messages, this choice can possibly be moved beneficially into the destination process, avoiding the sending of these messages altogether.

- A filter process passes messages from one process to another, possibly making small changes in the stream by dropping, duplicating, inserting, or altering messages. Again, if the desired effect is to generate a stream with a particular mix of messages, it is often possible to generate just such a stream directly.

Figure 5.2 shows a simple example of each of these three types of processes. To see how much can be saved by removing the sink process, for instance, consider the number of reachable states that is contributed by the storage of messages in the channel named q. The channel can hold between zero and eight distinct messages, and each of these is one of three possible types. This gives a total number of states equal to:

\[ \sum_{i=0}^{8} 3^i = 9.84 \]

**Figure 5.2 A Sink, a Source, and a Filter Process**

```plaintext
mtype = { one, two, three };
chan q = [8] of { mtype };
chan c = [8] of { mtype };

active proctype sink()
{
    do
    :: q?one
    :: q?two
    :: q?three
    od
}

active proctype filter()
{
    mtype m;
    do
    :: c?m -> q!m
    od
}

active proctype source()
{
    do
    :: c!one
```
Simple Refutation Models

Is it realistic to expect that we can build models that are of practical significance and that remain computationally tractable? To answer this, we discuss two remarkably simple models that have this property. The first model counts just twelve reachable states, which could be sketched on a napkin. The second model is not much larger, with fifty-one reachable states, yet it too has undeniable practical significance. A naïve model for either of these examples could easily defeat the capabilities of the most powerful model checking system. By finding the right abstraction, though, we can demonstrate that the design represented by the first model contains a design flaw, and we can prove the other to be a reliable template for the implementation of device drivers in an operating systems kernel.

The two abstractions discussed here require less computational power to be verified than what is available on an average wristwatch today. To be sure, it is often harder to find a simple model than it is to build a complex one, but the effort to find the simplest possible expression of a design idea can provide considerably greater benefits.
Pathfinder

NASA’s Pathfinder landed on the surface of Mars on July 4th, 1997, releasing a small rover to roam the surface. The mechanical and physical problems that had to be overcome to make this mission possible are phenomenal. Designing the software to control the craft may in this context seem to have been one of the simpler tasks, but designing any system that involves concurrency is challenging and requires the best minds and tools. Specifically, in this case, it was no easier to design the software than the rest of the spacecraft. And, as it turned out, it was only the control software that occasionally failed during the Pathfinder mission. A design fault caused the craft to lose contact with earth at unpredictable moments, causing valuable time to be lost in the transfer of data.

It took the designers a few days to identify the origin of the bug. To do so required an attempt to reproduce an unknown, non-deterministic execution sequence with only the tools from a standard system test environment, which can be very time-consuming.

The flaw turned out to be a conflict between a mutual exclusion rule and a priority rule used in the real-time task scheduling algorithm. The essence of the problem can be modeled in a SPIN verification model in just a few lines of code, as illustrated in Figure 5.3.

**Figure 5.3 Small Model for the Pathfinder Problem**

```c
mtype = { free, busy, idle, waiting, running };

mtype H.state = idle;
mtype L.state = idle;
mtype mutex = free;

active proctype high_priority()
{
    end:
    do
        : H.state = waiting;
        atomic { mutex == free -> mutex = busy };
        H.state = running;
        /* produce data */
        atomic { H.state = idle; mutex = free }
    od
}

active proctype low_priority() provided (H.state == idle)
{
    end:
    do
        : L.state = waiting;
        atomic { mutex == free -> mutex = busy };
        L.state = running;
        /* consume data */
        atomic { L.state = idle; mutex = free }
    od
}
```

Two priority levels are modeled here as active proctypes. Both processes need access to a critical region for transferring data from one process to the other, which is protected by a mutual exclusion lock. If by chance the high priority process starts running while the low priority process holds the lock, neither process can proceed: the high priority process is locked out by the mutex rule, and the low priority process is locked out by the priority rule, which is modeled by a provided clause on the low priority process.

The model shown here captures the essence of this problem in as few lines as possible. A verification of this model is performed in the next section.
A Disk-Head Scheduler

The next example illustrates how an abstract model can be constructed, again in just a few lines of high-level code, to confirm that a design has the properties it is intended to have. The example is a standard problem in operating system design: scheduling access of multiple client processes to a single server, which in this case is a disk scheduler. Only one client request is served by the disk-scheduler at a time. If multiple requests arrive, they are to be queued and served in order of arrival.

In a first attempt to build a verification model for this problem, it is natural to introduce separate processes to model the disk scheduler, the disk controller, the disk device driver, and the individual client processes that submit requests. To initiate a disk operation, a client process submits a request to the scheduler, where it may get queued. When it is ready to be serviced, the scheduler sends a start command to the controller, which then initiates the requested operation through the device driver. Completion of the operation is signaled by a hardware interrupt, which is intercepted by the scheduler. This basic architecture is illustrated in Figure 5.5.

**Figure 5.5. Disk Scheduler Context**

![Diagram showing the disk scheduler context](image)

Our objective is to check the basic design of the interaction between the disk scheduler and its clients. This means that the internal details of the device driver (e.g., mapping disk blocks to cylinders, sending commands to move the disk heads, etc.) are not directly relevant to this aspect of the design. To focus the verification model on the area of primary interest, we can and should abstract from the internals of the device driver process and the physical disk. The possible interactions between the device driver and the scheduler are, for instance, already captured in the device driver model from Figure 5.6.

**Figure 5.6 Minimal Device Driver Interface Model**

```c
proctype Contr(chan req, signal) {
  do
    :: req?IO ->
      /* perform IO operations */
      signal!Interrupt
    od
}
```

The only assumption we are making here about the behavior of the device driver is that it will respond to every IO request with an interrupt signal within a finite, but otherwise arbitrary, amount of time. The relevant behavior of a client process can be modeled very similarly. It suffices to assume that each client can submit one request at a time, and that it will then wait for the matching response from the scheduler.

Before looking at the remainder of the verification model, though, we can already see that these initial models for the device driver and the client have all the characteristics of filter processes. The same is true for a minimal model of the disk controller. This is not too surprising, since we deliberately placed the focus on the verification of request queuing at the disk scheduler, not on the surrounding processes.
Controlling Complexity

We will see in Chapter 8 that the worst-case computational expense of verifying any type of correctness property with a model checker increases with the number of reachable system states $R$ of a model. By reducing the size of $R$, therefore, we can try to reduce the complexity of a verification. Abstraction is the key tool we can use to keep the size of $R$ small, but there are also other factors that we could exploit in model building.

Let $n$ be the number of concurrent components, and let $m$ be the total number of data objects they access. If we represent the number of control states of the $i$-th component by $T_i$, and the number of possible values for the $j$-th data object by $D_j$, then in the worst case the size of $R$ could be the product of all values $T_1$ to $T_n$ and all values $D_1$ to $x \ D_m$. That is, the value of $R$ itself may well be exponential in the number of concurrent components and the number of data objects. As a general rule, therefore, it is always good to search for a model with the fewest number of components (processes, channels, data objects), that is, to construct the smallest sufficient model.
Example

Let us consider the complexity that can be introduced by a single useful type of abstract data object that is commonly used in distributed systems: a message channel or buffer. Let $q$ be the number of buffers we have, let $s$ be the maximum number of messages we can store in each buffer, and let $m$ be the number of different message types that can be used. In how many different states can this set of data objects be? Each buffer can hold between zero and $s$ messages, with each message being a choice of one out of $m$, therefore, the number of states $R_Q$ is:

$$R_Q = \left( \sum_{i=0}^{s} m^i \right)^q.$$

Figure 5.8 shows how the number of states varies for different choices of the parameters $q$, $s$, and $m$. In the top-left graph of Figure 5.8, the parameters $s$ and $q$ are fixed to a value of 2, and the number of message types is varied from 1 to 10. There is a geometric increase in the number of states, but clearly not an exponential one. In the top-right graph, the parameters $m$ and $q$ are fixed to a value of 2, and the number of queue slots $s$ is varied. This time there is an exponential increase in the number of states. Similarly, in the bottom-left graph, the parameters $m$ and $s$ are fixed, and the number of queues is varied. Again, we see an exponential increase in the number of states. Similarly, in the bottom-right graph of the figure, only the number of message types is fixed and the parameters $s$ and $q$ are equal and varied from 1 to 10. As can be expected, the increase is now doubly exponential. The number of possible states quickly reaches astronomical values.

Figure 5.8. Number of Possible States for $q$ Message Buffers with $s$ Buffer Slots and $m$ Message Types

Exponential effects work both ways. They can quickly make simple correctness properties of an uncarefully constructed model computationally intractable, but they can also help the model builder to prove subtle properties of complex systems by controlling just a few carefully chosen parameters.

The size of the available memory on a computer unavoidably restricts the size of the largest problems we can verify. We can try clever encoding and storage options for state space information, but at some point either the machine will run out of available memory or the user will run out of time, waiting for a verification run to complete. If the system is too complex to be analyzed exhaustively, we have no choice but to model it with a system that has fewer states. The tools that are used to accomplish this are: reduction, abstraction, modularity, and structure.

The existence of the state explosion phenomenon we have sketched above should never be used to excuse a designer from proving that a concurrent system fulfills its correctness requirements. It may well be considered to be the very objective of design verification to construct a tractable model and to formalize its properties. After all, since
A Formal Basis for Reduction

The SPIN verification algorithms work by detecting the presence of a counterexample to a correctness claim. If we want to prove that \( p \) holds, we can use SPIN to try to find a counterexample where the negation of \( p \) holds. For temporal logic formulae the same principle is applied. Instead of proving that there exist behaviors for which a given temporal logic formula is valid, SPIN tries to do the opposite: it attempts to find at least one behavior for which the negation of the formula is satisfied. If no counterexample can be found in an exhaustive verification, the formula is proven valid for all possible behaviors.

Call \( E \) the set of all possible runs of a system. The verification algorithms we have discussed demonstrate that either \( E \) does not contain any runs that violate a correctness requirement, or they provide positive proof that at least one such run exists. The verifier need not search for all possible runs in which the correctness requirement is satisfied, and indeed it often cannot do so.

This means that it is possible to add runs to \( E \) without affecting the validity of the proof, provided of course that we do not remove or alter any of the existing runs in \( E \). We will use an example to demonstrate a number of strategies that can be used to reduce the complexity of a verification task by adding runs to \( E \), such that in all cases \( E \subseteq E' \). This principle is formalized in the following property.[2]


**Property 5.1 (Reduction Property)**

Given two finite state automata \( T \) and \( T' \), with sets of runs \( E \) and \( E' \), respectively. If \( E \subseteq E' \) then any correctness property proven for \( T' \) necessarily also holds for \( T \).

Proof: The violation of a correctness property for \( T \) is not possible without the existence of a run in \( E \) that demonstrates it. If no such run exists in \( E' \) then no such run can exist in \( E \) either, since \( E' \) includes \( E \).

We will see that abstractions of this type can dramatically reduce the number of reachable states of a system. Note that we can generalize a problem by removing constraints from it. The behavior of a model that is less specific often can be represented with fewer states. The least specific model would be one that imposes no constraints whatsoever on, for instance, the messages it can send. It can be represented by a one-state demon that randomly generates messages within its vocabulary, one by one, in an infinite sequence.
Example – A File Server

Assume our task is to verify the correctness of a transfer protocol that is used to access a remote file server. Our first obligation is to determine precisely which correctness properties the transfer protocol must have, and what may be assumed about the behavior of the file server and of the transmission channel.

Consider first the transmission channel. Assume the channel is an optical fiber link. The protocol verifier’s job is not to reproduce the behavior of the fiber link at the finest level of detail. The quality of a verification does not improve with a more detailed model of the link. Just the opposite is the case. This is worth stating explicitly:

A less detailed verification model is often more tractable, and allows for more general, and thus stronger, proofs.

A verification model should represent only those behaviors that are relevant to the verification task at hand. It need not contain information about the causes of those behaviors. If, in the file server example, the fiber link has a non-zero probability of errors, then the possibility of errors must be present in our model, but little more. The types of errors modeled could include disconnection, message-loss, duplication, insertion, or distortion. If all these types of errors are present, and relevant to the verification task at hand, it should suffice to model the link as a one-state demon that can randomly disconnect, lose, duplicate, insert, or distort messages.

A fully detailed model of the link could require several thousand states, representing, for instance, the clustering of errors, or the nature of distortions. For a design verification of the transfer protocol, however, it not only suffices to represent the link by a one-state demon: doing so guarantees a stronger verification result that is independent of clustering or distortion effects. Clearly, a model that randomly produces all relevant events that can be part of the real link behavior satisfies the requirements of Property 5.1. Of course, the random model of a link can contribute artificial behaviors where specific types of errors are repeated without bound. Our verification algorithms, however, provide the means to prune out the uninteresting subsets of these behaviors. If, for instance, we mark message loss as a pseudo progress event and start a search for non-progress cycles, we can secure that every cyclic execution that is reported by the verifier contains only finitely many message loss events.

Next, consider the file server. It can receive requests to create and delete, open and close, or read and write distinct files. Each such request can either succeed or fail. A read request on a closed file, for instance, will fail. Similarly, a create or write request will fail if the file server runs out of space. Again, for the verification of the interactions with the file server, we need not model in detail under what circumstances each request may succeed or fail. Our model of the server could again be a simple one-state demon that randomly accepts or rejects requests for service, without even looking at the specifics of the request.

Our one-state server would be able to exhibit behaviors that the real system would not allow, for instance, by rejecting valid requests. All behaviors of the real server, however, are represented in the abstract model. If the transfer protocol can be proven correct, despite the fact that our model server may behave worse than the real one, the result is stronger than it would have been if we had represented the server in more detail. By generalizing the model of the file server, we separate, or shield, the correctness of the transfer protocol from the correctness requirements of the server. Again, the model that randomly produces all relevant events satisfies the requirements of Property 5.1.

[3] Remember that it is not the file server’s behavior we are verifying, but the behavior of the transfer protocol. If the file server would have been the target of our verification, we would try to model it in more detail and generalize the transfer protocol that accesses it.

Finally, let us consider the number of message types and message buffers that are needed to represent the interaction of user processes with the remote file server. If no single user can ever have more than one request outstanding, we need minimally three distinct types of messages, independent of how many distinct services the remote system actually offers. The three message types are request, accept, and reject.

If there are q users and only one server, the server must of course know which response corresponds to which request. Suppose that we use a single buffer for incoming requests at the server, and mark each request with a
In Summary

The goal of this chapter is to show that applying model checking tools in a focused and targeted manner can be far more effective than blindly applying them as brute force reachability analyzers.

In a nutshell, the application of model checking in a design project typically consists of the following four steps:

- First, the designer chooses the properties (the correctness requirements) that are critical to the design.

- Second, the correctness properties are used as a guideline in the construction of a verification model. Following the principle of the smallest sufficient model, the verification model is designed to capture everything that is relevant to the properties to be verified, and little else. The power of the model checking approach comes in large part from our ability to define and use abstractions. Much of that power may be lost if we allow the verification model to come too close to the specifics of an implementation.

- Third, the model and the properties are used to select the appropriate verification method. If the model is very large, this could mean the choice between a precise verification of basic system properties (such as a check for absence of deadlock and the correctness of all process and system assertions), or a more approximate check of more complex logical and temporal properties.

- Fourth, the result of the verification is used to refine the verification model and the correctness requirements until all correctness concerns are adequately satisfied.

In the construction of a verifiable model it is good to be aware of the main causes of combinatorial complexity: the number and size of buffered channels, and the number of asynchronously executing processes. We can often bring the complexity of a verification task under control by carefully monitoring and adjusting these few parameters.

We return to the topic of abstraction in Chapter 10, where we consider it in the context of automated model extraction methods from implementation level code.
Bibliographic Notes

The solution to the disk scheduler problem discussed in this chapter is based on Villiers [1979].

The importance of abstraction in verification is generally recognized and features prominently in many papers in this area. Foundational work goes back to the early work of Patrick and Radhia Cousot on abstract interpretation, e.g., Cousot and Cousot [1976].

A detailed discussion of the theoretical background for abstraction is well beyond the scope of this book, but a good starting point for such a discussion can be found in, for instance, the work of Abadi and Lamport [1991], Kurshan [1993], Clarke, Grumberg, and Long [1994], Graf and Saiti [1997], Dams [1996], Dams, Gerth, and Grumberg [1997], Kesten and Pnueli [1998], Das, Dill, and Park [1999], and in Chechik and Ding [2002]. A good overview can also be found in Shankar [2002]. A general discussion of the role of abstraction in applications of SPIN is also given in Holzmann [1998b], from which we have also derived some of the examples that were used in this chapter.

An interesting discussion of the use of abstraction techniques that exploit symmetry in systems models to achieve a reduction in the complexity of verifications can be found in Ip and Dill [1996].
Chapter 6. Automata and Logic

"Obstacles are those frightful things you see when you take your eyes off your goal."

—(Henry Ford, 1863–1947)

The model checking method that we will describe in the next few chapters is based on a variation of the classic theory of finite automata. This variation is known as the theory of $\omega$-automata. The main difference with standard finite automata theory is that the acceptance conditions for $\omega$-automata cover not just finite but also infinite executions.

Logical correctness properties are formalized in this theory as $\omega$-regular properties. We will see shortly that $\omega$-automata have just the right type of expressive power to model both process behavior in distributed systems and a broad range of correctness properties that we may be interested in proving about such systems.
Automata

To develop the theory, we begin with a few basic definitions.

**Definition 6.1 (FSA)**

A finite state automaton is a tuple \((S, s_0, L, T, F)\), where

- \(S\) is a finite set of states,
- \(s_0\) is a distinguished initial state, \(s_0 \in S\),
- \(L\) is a finite set of labels,
- \(T\) is a set of transitions, \(T \subseteq (S \times L \times S)\), and
- \(F\) is a set of final states, \(F \subseteq S\).

We will refer to state set \(S\) of finite state automaton \(A\) with a dot notation: \(A. S\). Similarly, the initial state of \(A\) is referred to as \(A. s_0\), etc.

In the simplest case, an automaton is deterministic, with the successor state of each transition uniquely defined by the source state and the transition label. Determinism is defined more formally as follows.

**Definition 6.2 (Determinism)**

A finite state automaton \((S, s_0, L, T, F)\) is deterministic if, and only if,

\[
\forall s \forall l, ((s, l, s') \in T \land (s, l, s'') \in T) \rightarrow s' \equiv s''.
\]

Many of the automata we will use do not have this property, that is, they will be used to specify non-deterministic behaviors. As we shall see, there is nothing in the theory that would make the handling of non-deterministic automata particularly troublesome.

**Definition 6.3 (Runs)**

A run of a finite state automaton \((S, s_0, L, T, F)\) is an ordered, possibly infinite, set of transitions (a sequence)

\[
\{(s_0, l_0, s_1), (s_1, l_1, s_2), (s_2, l_2, s_3), \ldots\}
\]

such that

\[
\forall i, (i \geq 0) \rightarrow (s_i, l_i, s_{i+1}) \in T.
\]

Occasionally we will want to talk about specific aspects of a given run, such as the sequence of states that is traversed, or the sequence of transition labels that it defines. Note that for non-deterministic automata the sequence of
Omega Acceptance

With the definition of a finite state automaton given here, we can model terminating executions, but we still cannot decide on acceptance or non-acceptance of ongoing, potentially infinite, executions. Looking at Figure 6.2, for instance, if we were to model the underlying scheduler, rather than the processes being scheduled, the termination of the scheduler itself would not necessarily be a desirable result. The same is true for many other interesting systems, such as the control software for a nuclear power plant, a telephone switch, an ATM machine, or a traffic light.

An infinite run is often called an \( \omega \)-run (pronounced: "omega run"). Acceptance properties for \( \omega \)-runs can be defined in a number of different ways. The one we will adopt here was introduced by J.R. Büchi [1960].

If \( \sigma \) is an infinite run, let the symbol \( \sigma_\omega \) represent the set of states that appear infinitely often within \( \sigma \)'s set of transitions, and \( \sigma^+ \) the set of states that appear only finitely many times. The notion of Büchi acceptance is defined as follows.

**Definition 6.5 (Büchi acceptance)**

An accepting \( \omega \)-run of finite state automaton \((S, s_0, L, T, F)\) is any infinite run \( \sigma \) such that \( \exists s_f \in F \land s \in \sigma_\omega \).

That is, an infinite run is accepted if and only if some state in \( F \) is visited infinitely often in the run. Without further precautions then, in the automaton from Figure 6.1 we could only see an accepting run under the definition of Büchi acceptance if at least one of the states \( s_1, s_2, \) or \( s_3 \) were members of final set \( F \), since only these states can be visited infinitely often in a run.

With these definitions it is also easy to formalize the notion of non-progress that we discussed before. Let \( P \subseteq S \) be the set of progress states. An \( \omega \)-run \( \sigma \) then corresponds to a non-progress cycle if: \( \forall s_f, s \in \sigma_\omega \Rightarrow s \notin P \).
The Stutter Extension Rule

The given formalization of acceptance applies only to infinite runs. It would clearly be convenient if we could somehow find a way to extend it so that the classic notion of acceptance for finite runs (cf. Definition 6.4) would be included as a special case. This can be done with the adoption of a stuttering rule. To apply the rule, we must extend our label sets with a fixed predefined null-label $\varepsilon$, representing a no-op operation that is always executable and has no effect (much like PROMELA’s skip statement). The stutter extension of a finite run can now be defined as follows.

**Definition 6.6 (Stutter Extension)**

The stutter extension of finite run $\sigma$ with final state $s_n$ is the $\omega$-run $\sigma, (s_n, \varepsilon, s_n)\omega$.

The final state of the run, then, is thought to persist forever by infinitely repeating the null action $\varepsilon$. It follows that such a run would satisfy the rules for Büchi acceptance if, and only if, the original final state $s_n$ is in the set of accepting states $F$, which means that it indeed generalizes the classical definition of finite acceptance.

A couple of abbreviations are so frequently used that it is good to summarize them here. The set of runs that is accepted by an automaton is often referred to as the language of the automaton. An automaton with acceptance conditions that are defined over infinite runs is often called an $\omega$-automaton.

Accepting $\omega$-runs of a finite state automaton can always be written in the form of an expression, using a dot to represent concatenation and the superfix $\omega$ to represent infinite repetition:

$$\bigcup_{i=1}^{N} U_i \cdot V_i^\omega$$

with $U_i$ and $V_i$ regular expressions over transitions in the automaton. That is, each such run consists of a finite prefix $U$, corresponding to an initial part of the run that is executed just once, and a finite suffix $V$, corresponding to a part of the run that is repeated ad infinitum. These expressions are called $\omega$-regular expressions, and the class of properties that they express are called $\omega$-regular properties. As a final bit of terminology, it is common to refer to automata with Büchi acceptance conditions simply as Büchi Automata.
Finite States, Infinite Runs

It is clear that also an automaton with only finitely many states can have runs that are infinitely long, as already illustrated by Figure 6.1. With some reflection, it will also be clear that a finite automaton can have infinitely many distinct infinite runs.

To see this, imagine a simple automaton with eleven states, ten states named s0 to s9, and one final (accepting) state s10. Define a transition relation for this automaton that connects every state to every other state, and also include a transition from each state back to itself (a self-loop). Label the transition from state si to sj with the PROMELA print statement printf("%d\n", i). Use this labeling rule for all transitions except the self-loop on the one final state s10, which is labeled skip. That is, if the transition from si to sj is taken, the index number of the source transition will be printed, with as the single exception the transition from s10 back to s10, which produces no output.

Every accepting run of this automaton will cause a number to be printed. This automaton has precisely one accepting run for every imaginable non-negative integer number, and there are infinitely many distinct numbers of this type.
Other Types of Acceptance

There are of course many other ways to formalize the acceptance conditions of $\omega$-automata. Most of these methods are named after the authors that first proposed them.

- Define $F$ to be a set of subsets from state set $S$, that is, $F \subseteq 2^S$. We can require that the set of all states that are visited infinitely often in run $\sigma$ equals one of the subsets in $F$:

$$\exists f \in F \land \sigma^n = f.$$

This notion of acceptance is called Muller acceptance, and the corresponding automata are called Muller Automata.

- We can also define a finite set of $n$ pairs, where for each pair $(L_i, U_i)$ we have $L_i \subseteq S$ and $U_i \subseteq S$. We can now require that there is at least one pair $i$ in the set for which none of the states in $L_i$ appear infinitely often in $\sigma$, but at least one state in $U_i$ does:

$$\exists i, (1 \leq i \leq n), \forall s, (s \in L_i \rightarrow s \notin \sigma^n) \land \exists t, (t \in U_i \land t \in \sigma^n).$$

This notion of acceptance is called Rabin acceptance, and the corresponding automata are called Rabin Automata.

- Using the same definition of pairs of sets states, we can also define the opposite condition that for all pairs in the set either none of the states in $U_i$ appear infinitely often in $\sigma$, or at least one state in $L_i$ does:

$$\forall i, (1 \leq i \leq n), \exists s, (s \in L_i \land s \notin \sigma^n) \lor \forall t, (t \in U_i \rightarrow t \notin \sigma^n).$$

This notion of acceptance is called Streett acceptance, and the corresponding automata are called Streett Automata.

All these types of acceptance are equally expressive and define the same class of $\omega$-regular properties as Büchi Automata.

Many interesting properties of Büchi automata have been shown to be decidable. Most importantly, this applies to checks for language emptiness (i.e., deciding whether the set of accepting runs of a given Büchi automaton is empty), and language intersection (i.e., generating a single Büchi automaton that accepts precisely those $\omega$-runs that are accepted by all members of a given set of Büchi automata). We shall see in Chapter 8 that the verification problem for SPIN models is equivalent to an emptiness test for an intersection product of Büchi automata.
Automata models offer a good formalism for the analysis of distributed system models. As noted in earlier chapters, though, a complete verification model contains not just the specification of system behavior but also a formalization of the correctness requirements that apply to the system. We will now show how higher-level requirements can be expressed in a special type of logic that has a direct connection to the formalism of Büchi Automata.

A run of an automaton captures the notion of system execution. Through the definition of acceptance conditions we can already distinguish the runs that satisfy a given set of requirements from those that violate it. It can be a daunting task, though, to express correctness requirements at this relatively low level of abstraction. We need a more convenient method.

Consider the automaton from Figure 6.3 with initial and final state s0. The formulation of a correctness property for this automaton requires the ability to interpret its runs, minimally to distinguish the good runs from the bad ones. To do so, we can define a semantics on the labels that are used. We will use the semantics interpretation of PROMELA. An integer variable named x is assigned values, and is tested in conditionals.

Figure 6.3. Model of a Simple Computation

The sequence of states traversed during a run of this (deterministic) automaton is:

s0, s1, s2, s3, s2, s3, s2, s3, s2, s0, ....

Of course, not every accepting run of the automaton will automatically be consistent with our chosen semantics interpretation of the labels. Given an initial value for x, we can write down the new value for x that is consistent with the PROMELA assignment statements from the labels. A run is only consistent with the semantics interpretation if all condition labels that appear in the run, such as x > 0 and x \leq 0, evaluate to true.

Given the initial value zero of x, we can annotate each state in the run above with the corresponding value for x, as follows:

(s0, 0), (s1, 13), (s2, 7), (s3, 7), (s2, 3), (s3, 3), (s2, 1), (s3, 1), (s2, 0), (s0, 0), ....

Jointly, the state number si and the value of variable x define an extended system state. We can derive a pure (non-extended) finite state automaton from the one that is specified in Figure 6.3 by expanding the set of states. State s2, for instance, would generate four copies in such an unfolding. For values 7, 3, 1, and 0 of x, and state s3 would generate three copies, one for each of the values 7, 3, and 1. The resulting expanded finite state automaton has nine states, all of which appear in the annotated state sequence.

We can formulate properties of runs of the expanded automaton. The most interesting properties would deal with the achievable and non-achievable values of x during a run. Consider, for instance, the properties

p: "the value of x is odd"

q: "the value of x is 13"
Temporal Logic

The branch of logic that allows one to reason about both causal and temporal relations of properties is called temporal logic. Temporal logic was first studied in the late sixties and early seventies, but primarily as a tool in philosophical arguments that involved the passage of time. A first paper proposing the application of this type of logic for the analysis of distributed system was authored by Amir Pnueli in 1977. It took more than a decade, though, for the fundamental importance of these ideas to be more generally accepted.

Temporal logic allows us to formalize the properties of a run unambiguously and concisely with the help of a small number of special temporal operators. Most relevant to the verification of asynchronous process systems is a specific branch of temporal logic that is known as linear temporal logic, commonly abbreviated as LTL. The semantics of LTL is defined over infinite runs. With the help of the stutter extension rule, however, it applies equally to finite runs, as we shall see in more detail shortly.

A well-formed temporal formula is built from state formulae and temporal operators, using the following two basic rules:

**Definition 6.7 (Well-Formed Temporal Formulae)**

- All state formulae, including true and false, are well-formed temporal formulae.
- If $\alpha$ is a unary temporal operator, $\beta$ is a binary temporal operator, and $p$ and $q$ are well-formed temporal formulae, than so are $\alpha p$, $p \beta q$, $(p)$, and $!p$ ($\neg p$).

The first temporal operator we will discuss is the binary operator until, which we will represent by the symbol $\mathcal{U}$. The truth of a formula such as $p \mathcal{U} q$ can be evaluated for any given $\omega$-run $\sigma$. The symbols $p$ and $q$ can be replaced with arbitrary state formulae or with temporal sub-formulae. If a temporal formula $f$ holds for $\omega$-run $\sigma$, we write:

$\sigma \models f$.

In the definitions that follow, we use the notational convention that $\sigma_i$ represents the $i$-th element of the run $\sigma$, and $\sigma[i]$ represents the suffix of $\sigma$ that starts at the $i$-th element. Trivially $\sigma \equiv \sigma[1] \equiv \sigma[1]$.

There are two variations of the until operator that are distinguished by the adjective weak and strong. The definition of the weak until operator is:

**Definition 6.8 (Weak Until)**

$\sigma[i] \models (p \mathcal{U} q) \iff \sigma[i] \models q \lor (\sigma[i] \models p \land \sigma[i+1] \models (p \mathcal{U} q))$.

Notice that this definition does not require that the sub-formula $q$ ever become true. The second variant of the operator, called strong until and written $\mathcal{U}$, adds that requirement.

**Definition 6.9 (Strong Until)**

$\sigma[i] \models (p \mathcal{U} q) \iff \sigma[i] \models (p \mathcal{U} q) \land \exists j \geq i, \sigma[i] \models q$.

There are two special cases of these two definitions that prove to be especially useful in practice. The first is a formula of the type $p \mathcal{U}$ false. Note that the truth of this formula only depends on the value of sub-formula $p$. We introduce a special operator to capture this:
Recurrence and Stability

There are many standard types of correctness properties that can be expressed with the temporal operators we have defined. Two important types are defined next.

**Definition 6.13**

A recurrence property is any temporal formula that can be written in the form $\square \diamond p$, where $p$ is a state formula.

The recurrence property $\square \diamond p$ states that if $p$ happens to be false at any given point in a run, it is always guaranteed to become true again if the run is continued.

**Table 6.1. Frequently Used LTL Formulae**

<table>
<thead>
<tr>
<th>Formula</th>
<th>Pronounced</th>
<th>Type/Template</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\square p$</td>
<td>always $p$</td>
<td>invariance</td>
</tr>
<tr>
<td>$\diamond p$</td>
<td>eventually $p$</td>
<td>guarantee</td>
</tr>
<tr>
<td>$p \rightarrow \diamond q$</td>
<td>$p$ implies eventually $q$</td>
<td>response</td>
</tr>
<tr>
<td>$p \rightarrow q \cup r$</td>
<td>$p$ implies $q$ until $r$</td>
<td>precedence</td>
</tr>
<tr>
<td>$\square \diamond p$</td>
<td>always eventually $p$</td>
<td>recurrence (progress)</td>
</tr>
<tr>
<td>$\diamond \square p$</td>
<td>eventually always $p$</td>
<td>stability (non-progress)</td>
</tr>
<tr>
<td>$\diamond p \rightarrow \diamond q$</td>
<td>eventually $p$ implies eventually $q$</td>
<td>correlation</td>
</tr>
</tbody>
</table>

**Definition 6.14**

A stability property is any temporal formula that can be written in the form $\diamond \square p$, where $p$ is a state formula.

The stability property $\diamond \square p$ states that there is always a point in a run where $p$ will become invariably true for the remainder of the run.

Recurrence and stability are in many ways dual properties that reflect a similar duality between the two earlier canonical correctness requirements we discussed: absence of non-progress cycles and absence of acceptance cycles.

There are other interesting types of duality. For instance, if "!" denotes logical negation, it is not hard to prove that in any context:

**Equation 1**

$\neg \square p \iff \diamond \neg p$

**Equation 2**

$\neg \square p \iff \diamond \neg p$
Using Temporal Logic

The logic looks straightforward enough, and it is not difficult to develop an intuition for the meaning of the operators. Still, it can sometimes be difficult to find the right formalization in temporal logic of informally stated requirements. As an example, consider the informal system requirement that \( \mathit{p} \) implies \( \mathit{q} \). The formalization that first comes to mind is

\[ \mathit{p} \rightarrow \mathit{q} \]

which is almost certainly wrong. Note that as a formula in temporal logic this property must hold for every run of the system. There are no temporal operators used here, just logical implication. This means that it holds if and only if

\[ \pi \models (\neg \pi) \lor \mathit{q} \]

which holds if in the first state of the run either \( \mathit{p} \) is false or \( \mathit{q} \) is true. It says nothing about the remaining steps in \( \pi \)[2]. To make the property apply to all steps in the run we would have to change it into

\[ \Box (\mathit{p} \rightarrow \mathit{q}) \]

but also that is most likely not what is meant, because this expresses merely a logical implication between \( \mathit{p} \) and \( \mathit{q} \), not a temporal implication. If a temporal implication was meant, the formula should be written as follows:

\[ \Box (\mathit{p} \rightarrow \Diamond \mathit{q}) \]

This still leaves some room for doubt, since it allows for the case where \( \mathit{q} \) becomes true in precisely the same state as where \( \mathit{p} \) becomes true. It would be hard to argue that this accurately captures the notion that the truth of \( \mathit{q} \) is somehow caused by the truth of \( \mathit{p} \). To capture this, we need to modify the formula again, for instance, by adding a next operator.

\[ \Box (\mathit{p} \rightarrow X (\Diamond \mathit{q})) \]

After all this work, this formula may still prove to be misleading. If the antecedent \( \mathit{p} \) is invariantly false throughout each run, for instance, the property will be satisfied. In this case, we call the property vacuously true. It is almost surely not what we meant when we formalized the property. This brings us to the final revision of the formula by adding the statement that we expect \( \mathit{p} \) to become true at some point. This produces the final form

\[ \Box (\mathit{p} \rightarrow X (\Diamond \mathit{q})) \land \Diamond \mathit{p} \]

which is quite different from the initial guess of \( (\mathit{p} \rightarrow \mathit{q}) \).
Valuation Sequences

Let $P$ be the set of all state formulae that are used in a given temporal logic formula. Each such state formula is typically represented by a lower-case propositional symbol (say $p$ or $q$). Let, further, $V$ represent the set of all the possible boolean truth assignments to the propositional symbols in $P$ (i.e., set $V$ has $2^{|P|}$ elements, where $|P|$ is the number of elements of set $P$). We call $V$ the set of valuations of $P$. With each run $\sigma$ of a system we can now associate a sequence of valuations from $V$, denoting the specific boolean values that all propositional symbols take, as we illustrated earlier for the system in Figure 6.3. We will refer to that sequence as $V(\sigma)$. 
Stutter Invariance

The next operator, X, can be useful to express complex system requirements, but it should be used with caution. Note first that in a distributed system the very notion of a "next" state is somewhat ambiguous. It is usually unknown and unknowable how the executions of asynchronously execution processes are going to be interleaved in time. It can therefore usually not be determined with certainty how a given current system state relates to the one that happens to follow it after one more step in a run. We can assume that every process will make finite progress, unless it becomes permanently blocked, but it is usually not justified to make more specific assumptions about the precise rate of progress, relative to other processes, since this may depend on uncontrollable and often unobservable aspects of a distributed system, such as the relative speeds of processors or subtle details of process scheduling.

These somewhat vague notions about what can and what cannot safely be stated about the runs of a distributed system can be made more precise with the help of the notion of stutter invariance.

Consider a run $\sigma$ and its valuation $\phi = V(\sigma)$. Remember that $\phi$ is a sequence of truth assignments to the elements of a finite set of boolean propositions $P$ used in a given temporal formula. Two subsequent elements of this sequence are either equal or they differ. We will replace series of equal consecutive elements in a valuation with a single symbol with the number of repetitions recorded in a superfix.

Let $N$ be a sequence of positive numbers $N_1, N_2, \ldots$. Each valuation $\phi$ of a run can then be written in the form

$$\phi_{N_1}^{N_1}, \phi_{N_2}^{N_2}, \ldots$$

with an appropriate choice for $N$. Given such a sequence $\phi$, we can derive a stutter-free variant of $\phi$ by setting all elements of $N$ to one: $N=1, 1, \ldots$. We can also derive a set of variants of $\phi$ that includes all possible choices for $N$. Such a set is called the stutter extension of $\phi$ and written as $E(\phi)$.

For temporal logic formula $f$ to be satisfied on some run $\sigma$, the valuation $V(\sigma)$ must satisfy the formula, that is, we must have $V(\sigma) \models f$. We are now ready to define stutter invariance.

**Definition 6.17 (Stutter invariance)**

A temporal logic formula $f$ is stutter invariant if and only if

$$V(\sigma) \models f \rightarrow \forall \phi, \phi \in E(\sigma), V(\phi) \models f.$$

This means that the property is stutter invariant if it is insensitive to the number of steps that individual valuations of the boolean propositions remain in effect.

We argued earlier that it would be dangerous for the correctness of a system to depend on execution speed, so this nicely captures our intuition about well-formed formulae in temporal logic: such formulae should be stutter invariant.

It can be shown that if we bar the next operator, X, from temporal logic, the temporal formulae that we write will be guaranteed to be stutter invariant. Moreover, it can also be shown that without the next operator we can precisely express all stutter invariant properties. This does not mean that a temporal logic formula that includes a X operator is necessarily not stutter invariant: it may well be so, but it is not guaranteed.

In a later chapter we will see another reason why we will want to be cautious with the use of X: properties that are known to be stutter invariant can be verified more efficiently than properties that do not have this property.
Fairness

One of the attractive features of LTL is that it can be used to express a fairly broad range of fairness assumptions. SPIN itself supports only a limited notion of fairness that applies only to the specific way in which process-level non-determinism is resolved (i.e., it applies only to process scheduling decisions). In some cases, we may want to express that also non-deterministic choices within a process are resolved conform some user-specified notion a fairness. These types of fairness conditions are readily expressed in LTL. If, for instance, our correctness claim is $\phi$, we can add the fairness constraint that if a process of type P visits a state labeled U infinitely often, it must also visit a state labeled L infinitely often, by adding a conjunct to the property:

$$\phi \land (\square (P@U) \rightarrow (\square (P@L))).$$
From Logic To Automata

It was shown in the mid eighties that for every temporal logic formula there exists a Büchi automaton that accepts precisely those runs that satisfy the formula. There are algorithms that can mechanically convert any temporal logic formulae into the equivalent Büchi automaton. One such algorithm is built into SPIN.

Strictly speaking, the system description language PROMELA does not include syntax for the specification of temporal logic formulae, but SPIN does have a separate parser for such formulae and it can mechanically translate them into PROMELA syntax, so that LTL can effectively become part of the language that is accepted by SPIN. LTL, however, can only be used for specifying correctness requirements on PROMELA verification models. The models themselves cannot be specified in LTL. SPIN's conversion algorithm translates LTL formulae into never claims, and it automatically places accept labels within the claim to capture the semantics of the ω-regular property that is expressed in LTL.

To make it easier to type LTL formulae, the box (always) operator is written as a combination of the two symbols [], and the diamond operator (eventually) is written as the two symbols <> . SPIN only supports the strong version of the until operator, represented by the capital letter U. To avoid confusion, state properties are always written with lower-case symbols such as p and q.

We can, for instance, invoke SPIN as follows:

```
$ spin -f '<>[] p'
never { /* <>[]p */
T0_init:
  if
    : (p) -> goto accept_S4
    : (1) -> goto T0_init
  fi;
accept_S4:
  if
    : (p) -> goto accept_S4
  fi
}
```

Note carefully that in a UNIX environment the temporal logic formula must be quoted to avoid misinterpretation of the angle symbols by the command interpreter, and to secure that the formula is seen as a single argument even if it contains spaces. [1] SPIN places braces around all expressions to make sure that there can be no surprises in the enforcement of precedence rules in their evaluation. Note also that the guard condition (1) is equivalent to the boolean value true.

[1] On some, but not all, UNIX systems, the argument with the formula can also be enclosed in double quotes.

A note on syntax: SPIN accepts LTL formulae that consist of propositional symbols (including the predefined terms true and false), unary and binary temporal operators, and the three logical operators ! (logical negation), ∧ (logical and), and ∨ (logical or). The logical and operator can also be written in C style as &&, and the logical or operator can also be written as ||. Also supported are the abbreviations -> for logical implication and <-> for logical equivalence (see Definitions 6.15 and 6.16). Arithmetic operators (e.g., +, -, *, /) and relational operators (e.g., >, ≥, <, <=, ==, !=) cannot appear directly in LTL formulae.

For example, the following attempt to convert a formula fails:

```
$ spin -f '(([] p -> <> (a+b <= c)))'
```
An Example

Consider the following model:

```c
int x = 100;

active proctype A()
{
    do
        :: x%2 -> x = 3*x+1
    od
}

active proctype B()
{
    do
        :: !(x%2) -> x = x/2
    od
}
```

What can the range of values of x be? We may want to prove that x can never become negative or, more interestingly, that it can never exceed its initial value of one hundred. We can try to express this in the following formula:

```
$ spin -f ' [] (x > 0 && x <= 100)'     # wrong
```

But this is not right for two reasons. The first is indicated by the syntax error that SPIN flags. For SPIN to be able to translate a temporal formula it may contain only logical and temporal operators and propositional symbols: it cannot directly include arithmetic or relational expressions. We therefore have to introduce a propositional symbol to represent the expression (x > 0 && x <= 100), and write

```
$ spin -f '[] p'               # better, but still wrong
```

Elsewhere in the model itself we can now define p as:

```c
#define p      (x > 0 && x <= 100)
```

To see that this is still incorrect, notice that we have used SPIN to generate a never claim: expressing behavior that should never happen. We can use SPIN only to check for violations of requirements. So what we really meant to state was that the following property, the violation of the first, cannot be satisfied:

```
$ spin -f '[] p'      # correct
```

This automaton exits, signifying a violation, when the condition p ever becomes false, which is what we intended to express. SPIN can readily prove that violations are not possible, proving that with the given initialization the value of x is indeed bounded.

Another property we can try to prove is that the value of x eventually always returns to one. Again, to check that this is true we must check that the opposite cannot happen. First we introduce a new propositional symbol q.

```c
#define q      (x == 1)
```

Using q, the negated property is written as follows:

```
$ spin -f '[]<>q'      # correct
```

Also in this case SPIN readily proves the truth of the property.

Note also that to make these claims about the possible values of the integer variable x, the scope of the variable must include the never claim. This means that we can only make these claims about global variables. A local variable is never within the scope of a PROMELA never claim.
Omega-Regular Properties

PROMELA never claims can express a broader range of properties that can be expressed in temporal logic, even when the next operator is allowed. Formally, a never claim can express any $\omega$-regular property. To capture a property that is not expressible in temporal logic we can try to encode it directly into a never claim, but this is an error-prone process. There is an alternative, first proposed by Kousha Etessami. The alternative is to extend the formalism of temporal logic. A sufficient extension is to allow each temporal logic formula to be prefixed by an existential quantifier that is applied to one of the propositional symbols in the formula. Etessami proved that this single extension suffices to extend the power of temporal logic to cover all $\omega$-regular properties.

Consider the case where we want to prove that it is impossible for $p$ to hold only in even steps in a run, but never at odd steps. The temporal logic property $[\square] X p$ would be too strong for this, since it would require $p$ to hold on all even steps. This property can be expressed with existential quantification over some pseudo variable $t$ as follows.

$$\{E \ t\} \ t \land [\square](t \rightarrow X \neg t) \land [\square](\neg t \rightarrow X \ t) \land [\square](p \rightarrow \neg t)$$

This property states that there exists a propositional symbol $t$ that is initially true and forever alternates between true and false, much like a clock. The formula further states that the truth of the $p$ that we are interested in always logically implies the falseness of the alternating $t$. The automaton that corresponds to this formula is as follows.

```
$ eqltl -f '{E \ t} \ t \land [\square](t \rightarrow X \neg t) \land \\
 [\square](\neg t \rightarrow X \ t) \land [\square](p \rightarrow \neg t)'

never {
  accept0:
    if
        :: (!p) -> goto accept1
    fi;
  accept1:
    if
        :: (1) -> goto accept0
    fi
}
```

In the first step, and every subsequent odd step in the run, $p$ is not allowed to be true. No check on the value of $p$ is in effect during the even steps.

The eqltl program was developed by Kousha Etessami.
Other Logics

The branch of temporal logic that we have described here, and that is supported by the SPIN system, is known as linear time temporal logic. The prefix linear is due to the fact that these formulae are evaluated over single sequential runs of the system. With the exception of the small extension that we discussed in the previous section, no quantifiers are used. Linear temporal logic is the dominant formalism in software verification. In applications of model checking to hardware verification another version of temporal logic is frequently used. This logic is known as branching time temporal logic, with as the best known example CTL (an acronym for computation tree logic), which was developed at Carnegie Mellon University. CTL includes both universal and existential quantification, and this additional power means that CTL formulae are evaluated over sets of executions (trees), rather than over individual linear execution paths. There has been much debate in the literature about the relative merits of branching and linear time logics, a debate that has never culminated in any clear conclusions. Despite many claims to the contrary, there is no definitive advantage to the use of either formalism with regard to the complexity of verification. This complexity is dominated by the size of the verification model itself, not by the type of logic used to verify it. This issue, and some other frequently debated issues in model checking, is explored in greater detail in Appendix B.
Bibliographic Notes

The basic theory of finite automata was developed in the fifties. A good summary of the early work can be found in Perrin [1990]. The theory of \(\omega\)-automata dates back almost as far, starting with the work of Büchi [1960]. An excellent survey of this work, including definitions of the various types of acceptance conditions, can be found in Thomas [1990].

Amir Pnueli's influential paper, first proposing the use of temporal logic in the analysis of distributed systems, is Pnueli [1977]. The main notions used in the definition of temporal logic were derived from earlier work on tense logics. Curiously, this work, including the definition of some of the key operators from temporal logic, did not originate in computer science but in philosophy, see, for instance, Prior [1957,1967], and Rescher and Urquhart [1971]. An excellent overview of temporal logic can be found in Emerson [1990].

The correspondence between linear temporal logic formulae and Büchi automata was first described in Wolper, Vardi, and Sistla [1983]. An efficient conversion procedure, which forms the basis for the implementation used in SPIN, was given in Gerth, Peled, Vardi, and Wolper [1995]. The SPIN implementation uses some further optimizations of this basic procedure that are described in Etessami and Holzmann [2000].

There are several other implementations of the LTL conversion procedure, many of which can outperform the procedure that is currently built into SPIN. A good example is the procedure outlined in Gastin and Oddoux [2001]. Their converter, called ltl2ba, is available as part of the SPIN distribution.

The notion of stuttering is due to Lamport [1983], see also Peled, Wilke, and Wolper [1996] and Peled and Wilke [1997]. Etessami's conversion routine for handling LTL formulae with existential quantification is described in Etessami, Wilke, and Schuller [2001].
Chapter 7. PROMELA Semantics

"The whole is often more than the sum of its parts."

—(Aristotle, Metaphysica, 10f–1045a, ca. 330 B.C.)

As we have seen in the earlier chapters, a SPIN model can be used to specify the behavior of collections of asynchronously executing processes in a distributed system. By simulating the execution of a SPIN model we can in principle generate a large directed graph of all reachable system states. Each node in that graph represents a possible state of the model, and each edge represents a single possible execution step by one of the processes. PROMELA is defined in such a way that we know up-front that this graph will always be finite. There can, for instance, be no more than a finite number of processes and message channels, there is a preset bound on the number of messages that can be stored in each channel, and each variable has a preset and finite range of possible values that it can attain during an execution. So, in principle, the complete graph can always be built and analyzed in a finite amount of time.

Basic correctness claims in PROMELA can be interpreted as statements about the presence or absence of specific types of nodes or edges in the global reachability graph. More sophisticated temporal logic properties can be interpreted to express claims about the presence or absence of certain types of subgraphs, or paths, in the reachability graph. The global reachability graph can itself also be interpreted as a formal object: a finite automaton, as defined in Appendix A (p. 553).

The structure of the reachability graph is determined by the semantics of PROMELA. In effect, the PROMELA semantics rules define how the global reachability graph for any given PROMELA model is to be generated. In this chapter we give operational semantics of PROMELA in precisely those terms. The operational semantics definitions should allow us to derive in detail what the structure of the global reachability graph is for any given SPIN model.
Transition Relation

Every PROMELA proctype defines a finite state automaton, \((S, s_0, L, T, F)\), as defined in Chapter 6. The set of states of this automaton \(S\) corresponds to the possible points of control within the proctype. Transition relation \(T\) defines the flow of control. The transition label set \(L\) links each transition in \(T\) with a specific basic statement that defines the executability and the effect of that transition. The set of final states \(F\), finally, is defined with the help of PROMELA end-state, accept-state, and progress-state labels. A precise description of how set \(F\) is defined for safety and for liveness properties can be found in Appendix A.

Conveniently, the set of basic statements in PROMELA is very small. It contains just six elements: assignments, assertions, print statements, send or receive statements, and PROMELA's expression statement (cf. p. 51). All other language elements of PROMELA serve only to specify the possible flow of control in a process execution, that is, they help to specify the details of transition relation \(T\). As one small example, note that goto is not a basic statement in PROMELA. The goto statement, much like the semicolon, merely defines control-flow.

As a small example of how PROMELA definitions translate into automata structures, consider the PROMELA model shown in Figure 7.1, which corresponds to the automaton structure shown in Figure 7.2. The presence of the goto achieves that the execution of the assertion statement leads to control state \(s_2\), instead of \(s_4\). Thereby it changes the target state of a transition, but it does not in itself add any transitions. In other words, the goto effects a change in transition relation \(T\), but it does not, and cannot, appear in label set \(L\).

**Figure 7.1 Sample PROMELA Model**

```plaintext
active proctype not_euclid(int x, y)
{
   if
     :: (x >  y) \rightarrow L: x = x - y
     :: (x <  y) \rightarrow y = y - x
     :: (x == y) \rightarrow assert(x!=y); goto L
   fi;
   printf(";\d\n", x)
}
```

**Figure 7.2. Transition Relation for the Model in Figure 7.1**

Two points are especially worth noting here. First, language elements such as if, goto, the statement separators semicolon and arrow, and similarly also do, break, unless, atomic, and d_step, cannot appear as labels on transitions: only the six basic types of statements in PROMELA can appear in set \(L\).

Second, note that expression statements do appear as first-class transition labels in the automaton, and they are from
Operational Model

Our operation model centers on the specification of a semantics engine which determines how a given PROMELA model defines system executions, including the rules that apply to the interleaved execution of process actions. The semantics engine operates on abstract objects that correspond to asynchronous processes, variables, and message channels. We give formal definitions of these abstract objects first. We also define the concept of a global system state and a state transition, corresponding, respectively, to nodes and edges in a global reachability graph. We skip the definition of more basic terms, such as sets, identifiers, integers, and booleans.

Definition 7.1 (Variable)

A variable is a tuple (name, scope, domain, inival, curval) where

- name is an identifier that is unique within the given scope,
- scope is either global or local to a specific process,
- domain is a finite set of integers,
- inival, the initial value, is an integer from the given domain, and
- curval, the current value, is also an integer from the given domain.

We will refer to the elements of a tuple with a dot notation. For instance, if v is a variable, then v.scope is its scope.

The scope of a variable is either global, including all processes, or it is restricted to one specific process (to be defined below). The type of a variable trivially determines its domain. For instance, a variable of type bit has domain \{0,1\}.

Definition 7.2 (Message)

A message is an ordered set of variables (Def. 7.1).

Definition 7.3 (Message Channel)

A channel is a tuple (ch_id, nslots, contents) where

- ch_id is a positive integer that uniquely identifies the channel,
- nslots is an integer, and
- contents is an ordered set of messages (Def. 7.2) with maximum cardinality nslots.

Note that the definition of a channel does not contain a scope, like the definition of a variable. A PROMELA channel does not know which process sent it a message, or which process it accepted a message from. The definition of a channel is similar to the definition of an integer variable, which follows. The main difference is the addition of the cardinality of contents in the case of a channel.
Operational Model, Semantics Engine

The semantics engine executes a SPIN model in a step by step manner. In each step, one executable basic statement is selected. To determine if a statement is executable or not, one of the conditions that must be evaluated is the corresponding executability clause, as described in the PROMELA manual pages that start on p. 363. If more than one statement is executable, any one of them can be selected. The semantics definitions deliberately do not specify (or restrict) how the selection of a statement from a set of simultaneously executable statements should be done. The selection could, for instance, be random. By leaving this decision open, we in effect specify that the correctness of every SPIN model should be independent of the selection criterion that is used.

For the selected statement, the effect clause from the statement is applied, as described in the PROMELA manual pages for that statement, and the control state of the process that executes the statement is updated. The semantics engine continues executing statements until no executable statements remain, which happens if either the number of processes drops to zero, or when the remaining processes reach a system deadlock state.

The semantics engine executes the system, at least conceptually, in a stepwise manner: selecting and executing one basic statement at a time. At the highest level of abstraction, the behavior of this engine can be defined as follows:

Let E be a set of pairs (p, t), with p a process, and t a transition. Let executable(s) be a function, yet to be defined, that returns a set of such pairs, one for each executable transition in system state s. The semantics engine then performs as shown in Figure 7.3.

Figure 7.3 PROMELA Semantics Engine

```plaintext
1  while (\{(E = executable(s)) != {}\})
2  {  
3     for some (p, t) from E  
4     {  
5         s' = apply(t.effect, s)  
6         if (handshake == 0)
7         {  
8             p.curstate = t.target  
9         } else
10         {  /* try to complete rv handshake */
11             E' = executable(s')
12             /* if E' is {}, s is unchanged */
13             for some (p', t') from E'
14             {  
15                 s = apply(t'.effect, s')
16                 p.curstate = t.target  
17                 p'.curstate = t'.target
18             }
19         }  
20     }  
21 } while (stutter) { s = s } /* 'stutter' extension */
```

As long as there are executable transitions (corresponding to the basic statements of PROMELA), the semantics engine repeatedly selects one of them at random and executes it.

The function apply() applies the effect of the selected transition to the system state, possibly modifying system and local variables, the contents of channels, or even the values of the reserved variables exclusive and handshake, as defined in the effect clauses from atomic or rendezvous send operations, respectively. If no rendezvous offer was made (line 6), the global state change takes effect by an update of the system state (line 7), and the current state of the process that executed the transition is updated (line 8).

If a rendezvous offer was made in the last transition, it cannot result in a global state change unless the offer can also be accepted. On line 11 the transitions that have now become executable are selected. The definition of the function executable() below guarantees that this set can only contain consecutive transitions for the given offer. If there are none such transitions, then the function returns the empty set, and the semantics engine continues in the manner described above.

```plaintext
as long as there are executable transitions (corresponding to the basic statements of PROMELA), the semantics engine repeatedly selects one of them at random and executes it.

The function apply() applies the effect of the selected transition to the system state, possibly modifying system and local variables, the contents of channels, or even the values of the reserved variables exclusive and handshake, as defined in the effect clauses from atomic or rendezvous send operations, respectively. If no rendezvous offer was made (line 6), the global state change takes effect by an update of the system state (line 7), and the current state of the process that executed the transition is updated (line 8).

If a rendezvous offer was made in the last transition, it cannot result in a global state change unless the offer can also be accepted. On line 11 the transitions that have now become executable are selected. The definition of the function executable() below guarantees that this set can only contain consecutive transitions for the given offer. If there are none such transitions, then the function returns the empty set, and the semantics engine continues in the manner described above.

```
Interpreting PROMELA Models

The basic objects that are manipulated by the semantics engine are, of course, intended to correspond to the basic objects of a PROMELA model. Much of the language merely provides a convenient mechanism for dealing with the underlying objects. In the PROMELA reference manual in Chapter 16, some language constructs are defined as meta-terms, syntactic sugar that is translated into PROMELA proper by SPIN's preprocessor. Other language elements deal with the mechanism for declaring and instantiating variables, processes, and message channels. The control-flow constructs, finally, provide a convenient high-level means for defining transition relations on processes. An if statement, for instance, defines how multiple transitions can exit from the same local process state. The semantics engine does not have to know anything about control-flow constructs such as if, do, break, and goto; as shown, it merely deals with local states and transitions.

Some PROMELA constructs, such as assignments and message passing operations, cannot be translated away. The semantics model is defined in such a way that these primitive constructs correspond directly to the transitions of the underlying state machines. We call these PROMELA constructs basic statements, and there are surprisingly few of them in the language. The language reference manual defines the transition elements for each basic statement that is part of the language.
Three Examples

Consider the following PROMELA model.

chan x = [0] of { bit };
chan y = [0] of { bit };
active proctype A() { x?0 unless y!0 }
active proctype B() { y?0 unless x!0 }

Only one of two possible rendezvous handshakes can take place. Do the semantics rules tell us which one? If so, can the same rules also resolve the following, very similar, situation?

chan x = [0] of { bit };
chan y = [0] of { bit };
active proctype A() { x!0 unless y!0 }
active proctype B() { y?0 unless x?0 }

And, finally, what should we expect to happen in the following case?

chan x = [0] of { bit };
chan y = [0] of { bit };
active proctype A() { x!0 unless y?0 }
active proctype B() { y!0 unless x?0 }

Each of these cases can be hard to resolve without guidance from a semantics definition. The semantics rules for handling rendezvous communication and for handling unless statements seem to conflict here. This is what we know.

- The definition of unless states that the statement that precedes the unless keyword has a lower execution priority than the statement that follows it. These priorities must be used to resolve executability conflicts between the two transitions within each process.

- Rendezvous handshakes occur in two parts: the send statement constitutes a rendezvous offer, which can succeed if it is matched by a receive operation on the same channel in the immediately following execution step by the other process. To make the offer, the send statement must be executable by the rules of the semantics engine, and to accept the offer the matching receive operation must be executable.

- The effect clause of the rendezvous send operation states that the value of reserved variable handshake is set to the value of the channel instantiation number ch_id for the channel used. Lines 17-18 in Figure 7.4 then imply that no statement can now be executed, unless it has the rv parameter on that transition set to the same value, which is only the case for receive operations that target the same channel. A global state transition in the main execution loop of the semantics engine can only take place for rendezvous operations if the offer can be accepted.

We are now ready to resolve the semantics questions.

In the first example, according to the priority rule enforced by the unless operator, two statements are executable in the initial state: x!0 and y!0. Either one could be selected for execution. If the first is executed, we enter a rendezvous offer, with handshake set to the ch_id of channel x. In the intermediate global state s' then reached, only one statement can be added to set E', namely x?0. The final successor state has handshake == 0 with both processes in their final state. Alternatively, y!0 could be selected for execution, with an analogous result. The resulting state space structure is illustrated in Figure 7.5. For convenience, we have included the intermediate states where rendezvous offers are in progress. If a rendezvous offer cannot be accepted, the search algorithm will not actually store the intermediate state in the state space. Similarly, if the offer is accepted, the transition from state s0 to s1 is equivalent to an atomic step.

Figure 7.5. State Space Structure for First and Third Example

In the second example, only one statement is executable in the initial system state: y!0, and only the corresponding handshake can take place. The resulting state space structure is illustrated in Figure 7.6.

Figure 7.6. State Space Structure for Second Example

In the third example, the first two statements considered, at the highest priority (line 12, Figure 7.3), are both unexecutable. One priority level lower, though, two statements become executable: x!0 and y!0, and the resulting two system executions are again analogous to those from the first example, as illustrated in Figure 7.5.

A few quick checks with SPIN can confirm that indeed the basic executions we derived here are the only ones that can occur.
Verification

The addition of a verification option does not affect the semantics of a PROMELA model as it is defined here. Note, for instance, that the semantics engine does not include any special mention or interpretation of valid end states, accepting states, non-progress states, or assertions, and it does not include a definition for the semantics of never claims or trace assertions. The reason is that these language elements have no formal semantics within the model; they cannot be used to define any part of the behavior of a model.

Assertion statements, special labels, never claims, and trace assertions are used for making meta statements about the semantics of a model. How such meta statements are to be interpreted is defined in a verifier, as part of the verification algorithm.

When a verifier checks for safety properties it is interested, for instance, in cases where an assert statement can fail, or in the presence of executions that violate the requirements for proper termination (e.g., with all processes in a valid end state, and all message channels empty). In this case, the predefined system variable stutter, used in the definition of the semantics engine on line 22 in Figure 7.3, is set to false, and any mechanism can be in principle used to generate the executions of the system, in search of the violations.

When the verifier checks for liveness properties, it is interested in the presence of infinite executions that either contain finitely many traversals of user-defined progress states, or infinitely many traversals of user-defined accept states. The predefined system variable stutter is set to true in this case, and, again, any mechanism can be used to generate the infinite executions, as long as it conforms to the semantics as defined before. We discuss the algorithms that SPIN uses to solve these problems in Chapters 8 and 9. The definition of final states in product automata is further detailed in Appendix A.
The Never Claim

For purposes of verification, it is not necessary that indeed all finite or infinite executions that comply with the formal semantics are inspected by the verifier. In fact, the verifiers that are generated by SPIN make every effort to avoid inspecting all possible executions. Instead, they try to concentrate their efforts on a small set of executions that suffices to produce possible counterexamples to the correctness properties. The use of never claims plays an important role here. A never claim does not define new semantics, but is used to identify which part of the existing semantics can violate an independently stated correctness criterion.

The interpretation of a never claim by the verifier in the context of the semantics engine is as follows. Note that the purpose of the claim is to suppress the inspection of executions that could not possibly lead to a counterexample. To accomplish this, the verifier tries to reject some valid executions as soon as possible. The decision whether an execution should be rejected or continued can happen in two places: at line 2 of the semantics engine, and at line 22 (Figure 7.3), as illustrated in Figure 7.7.

**Figure 7.7 Claim Stutter**

```plaintext
1 while ((E = executable(s)) != {})
*2 {   if (check_fails()) Stop;
3     for some (p,t) from E
\ldots
21 }
*22 while (stutter) { s = s; if (check_fails()) Stop; }
```

SPIN implements the decision from line 22 by checking at the end of a finite execution if the never claim automaton can execute at least one more transition. Repeated stutter steps can then still lead to a counterexample. When the claim is generated from an LTL formula, all its transitions are condition statements, formalizing atomic propositions on the global system state. Only infinite executions that are consistent with the formal semantics of the model and with the constraint expressed by the never claim can now be generated.

With or without a constraint provided by a never claim, a verifier hunting for violations of liveness properties can check infinite executions for the presence of counterexamples to a correctness property. The method that the verifier uses to find and report those infinite executions is discussed in Chapter 8.
Chapter 8. Search Algorithms

"If I had eight hours to chop down a tree, I'd spend six hours sharpening my axe."

—(Abraham Lincoln, 1809–1865)

In this chapter we will discuss the basic algorithms that SPIN uses to verify correctness properties of PROMELA models. The basic algorithms are fairly simple and can quickly be explained. But, if we are interested in applying a verifier to problems of practical size, the mere basics do not always suffice. There are many ways in which the memory use and the run-time requirements of the basic algorithms can be optimized. Perhaps SPIN’s main strength lies in the range of options it offers to perform such optimizations, so that even very large problem sizes can be handled efficiently. To structure the discussion somewhat, we will discuss the main optimization methods that SPIN uses separately, in the next chapter. In this chapter we restrict ourselves to a discussion of the essential elements of the search method that SPIN employs.

We start with the definition of a depth-first search algorithm, which we can then extend to perform the types of functions we need for systems verification.
Depth-First Search

Consider a finite state automaton \( A = (S, s_0, L, T, F) \) as defined in Chapter 6 (p. 127). This automaton could, for instance, be the type of automaton that is generated by the PROMELA semantics engine from Chapter 7, capturing the joint behavior of a number of asynchronously executing processes. Every state in such an automaton then represents a global system state. For the discussion that follows, though, it is immaterial how the automaton was constructed or what it represents precisely.

The algorithm shown in Figure 8.1 performs a depth-first search to visit every state in set \( A.S \) that is reachable from the initial state \( A.s_0 \). The algorithm uses two data structures: a stack \( D \) and a state space \( V \).

Figure 8.1 Basic Depth-First Search Algorithm

```plaintext
Stack \( D = {} \)
Statespace \( V = {} \)

Start()
{
  Add_Statespace(V, A.s0)
  Push_Stack(D, A.s0)
  Search()
}

Search()
{
  s = Top_Stack(D)
  for each \( (s, l, s') \in A.T \)
    if In_Statespace(V, s') == false
      Add_Statespace(V, s')
      Push_Stack(D, s')
      Search()
  Pop_Stack(D)
}
```

A state space is an unordered set of states. As a side effect of the execution of the algorithm in Figure 8.1, some of the contents of set \( A.S \) is reproduced in state space \( V \), using the definition of initial state \( A.s_0 \) and of transition relation \( A.T \). Not all elements of \( A.S \) will necessarily appear in set \( V \), because not all these elements may effectively be reachable from the given initial state.

The algorithm uses just two routines to update the contents of the state space:

- \( \text{Add}_\text{Statespace}(V, s) \) adds state \( s \) as an element to state space \( V \)
- \( \text{In}_\text{Statespace}(V, s) \) returns true if \( s \) is an element of \( V \), otherwise it returns false

A stack is an ordered set of states. If the symbols < and > indicate the ordering relation, we have for any stack \( D \):

\[
\forall a_1, a_2 \in D: (a_1 \neq a_2 \rightarrow a_1 < a_2 \lor a_1 > a_2)
\]

\[
\forall s_1, s_2, s_3 \in D: (s_1 < s_2 < s_3 \rightarrow s_1 < s_3)
\]

Because of the ordering relation, a stack also has a unique top and bottom element. If the stack is non-empty, the top is the most recently added element and the bottom is the least recently added element.

The algorithm in Figure 8.1 uses three routines to access stack \( D \):

-
Checking Safety Properties

The depth-first search algorithm systematically visits every reachable state, so it is relatively straightforward to extend the algorithm with an evaluation routine that can check arbitrary state or safety properties. The extension of the search algorithm that we will use is shown in Figure 8.2. It uses a generic routine for checking the state properties for any given state \( s \), called Safety(\( s \)).

Figure 8.2 Extension of Figure 8.1 for Checking Safety Properties

```plaintext
Stack D = {}
Statespace V = {}
Start()
{
    Add_Statespace(V, A. s0)
    Push_Stack(D, A. s0)
    Search()
}

Search()
{
    s = Top_Stack(D)
    if !Safety(s)
    {
        Print_Stack(D)
    }
    for each (s, l, s') \( \in \) A.T
        if In_Statespace(V, s') == false
            Add_Statespace(V, s')
            Push_Stack(D, s')
            Search()
    Pop_Stack(D)
}
```

This routine could, for instance, flag the presence of a deadlock state by checking if state \( s \) has any successors, but it can also flag the violation of process assertions or system invariants that should hold at \( s \). Since the algorithm visits all reachable states, it has the desirable property that it can reliably identify all possible deadlocks and assertion violations.

The only real issue to resolve is what precisely the algorithm should do when it finds that a state property is violated. It could, of course, merely print a message, saying, for instance:

dfs: line 322, assertion (a > b) can be violated, aborting.

There are two things wrong with this approach. First and foremost, this solution would leave it to the user to determine just how and why the assertion could be violated. Just knowing that a state property can be violated does not help us to understand how this could happen. Secondly, it is not necessary to abort a verification run after a single violation was found. The search for other violations can continue.

To solve the first problem, we would like our algorithm to provide the user with some more information about the sequence of steps that can lead to the property violation. Fortunately, all the information to do so is readily available. Our algorithm can produce a complete execution trace that demonstrates how the state property was violated. The trace can start in the initial system state, and end at the property violation itself. That information is contained in stack D. For this purpose, the algorithm in Figure 8.2 makes use of a new stack routine Print_Stack(D):
Depth-Limited Search

We can adapt the depth-first search algorithm fairly easily into a depth-limited search that guarantees coverage up to a given depth bound. Such an algorithm is given in Figure 8.4. One change is the addition of an integer variable depth to maintain a running count of the size of stack D. Before growing the stack, the algorithm now checks the value of variable Depth against upper-bound BOUND. If the upper-bound is exceeded, routine Search() does not descend the search tree any further, but returns to the previous expansion step.

This change by itself is not sufficient to guarantee that all safety violations that could occur within BOUND steps will always be found. Assume, for instance, an upper-bound value of three for the size of D. Now consider a state s2 that is reachable from the initial state via two paths: one path of two steps and one path of one step. If s2 has an error state e among its successors (i.e., a state exhibiting a property violation) that error state is reachable via either a path of three steps or via a path of two steps. The first path exceeds our presumed bound of three, but the second does not. If the depth-first search starts by traversing the first path, it will have added states s0, s1, and s2 to state space V when it runs into the depth bound of three. It will then return, first to state s1 and next to state s0 to explore the remaining successor states. One such successor state of s0 is s2. This state, however, is at this point already in V and therefore not reconsidered. (It will not be added to the stack again.) The second path to the error state e will therefore not be explored completely, and the reachability of the error state within three steps will go unreported. The situation is illustrated in Figure 8.3.

Figure 8.3. Example for Depth-Limited Search

![Diagram](image)

We can avoid this type of incompleteness by storing the value of variable Depth together with each state in state space V. The algorithm from Figure 8.4 uses this information in a slightly modified version of the two state space access routines, as follows:

- Add_Statespace(V, s, d) adds the pair (s, d) to state space V, where s is a state and d the value of Depth, that is, the current size of the stack

- In_Statespace(V, s, d) returns true if there exists a pair (s', d') in V such that s' ≡ s and d' < d. Otherwise it returns false

Figure 8.4 Depth-Limited Search

```c
Stack D = {}
Statespace V = {}
int Depth = 0

Start()
{
    Add_Statespace(V, A.s0, 0)
    Push_Seq(D, A.s0)
    Search()
}
```
Trade-Offs

The computational requirements for the depth-first search algorithm are linear in the number of reachable states in A.S. If A.S is itself computed from asynchronous components, which is the typical case in applications of SPIN, the size of this state set is in the worst case equal to the size of the Cartesian product of all component state sets Ai.S (cf. Appendix A). The size of this set can increase exponentially with the number of component systems. Although in practice the number of reachable states is no more than a small fraction of this upper bound, a small fraction of a potentially astronomically large number can still be very large.

One of the advantages of on-the-fly verification is that it allows us to trade memory requirements for run-time requirements when needed. One way to do this would be to randomly erase part of the state space when the algorithm runs out of memory, provided that the part erased contains no states that are still on the stack. Note carefully that the state space access routines (not the stack routines) serve only to prevent the multiple exploration of states. These routines do not affect the actual coverage of the search.

If we omit the call on routine Add_Statespace(), and replace the routine In_Statespace() with a new stack routine In_Stack(), we still have a correct algorithm that is guaranteed to terminate within a finite number of steps. The routine In_Stack(D,s) can be defined to return true if state s is currently contained in stack D, and false in all other cases.

The real purpose of the state space access routines is to improve the efficiency of the search by avoiding the repetition of work. If we completely eliminate the state space routines, as illustrated in Figure 8.5, the efficiency of the search could deteriorate dramatically. This change may cause each state to be revisited once from every other state in the state space, which means a worst-case increase in complexity from $O(R)$ to $O(RR)$ steps, where R is the total number of reachable states.

**Figure 8.5 Stateless Search**

```
Stack D = {}

Start()
{
  Push_Stack(D, A.s0)
  Search()
}

Search()
{
  s = Top_Stack(D)
  if !Safety(s)
  {
    Print_Stack(D)
    if (iterative)
      BOUND = Depth
  }
  for each (s, l, s') in A. T
  {
    if In_Stack(D, s') == false
    {
      Push_Stack(D, s')
      Search()
    }
  }
  Pop_Stack(D)
}
```

Intermediate solutions are possible, for example, by changing the state space V from an exhaustive set into a cache of randomly selected previously visited states, but it is hard to avoid cases of seriously degraded performance. SPIN therefore does not use caching strategies to reduce memory use. The optimization strategies implemented in SPIN are all meant to have a more predictable effect on performance. We discuss these strategies in Chapter 9. 

[ Team LiB ]
Breadth-First Search

The implementation of a breadth-first search discipline looks very similar to that of the depth-first search. Instead of a search stack, though, we now use a standard queue. Successor states are added to the tail of the queue during the search, and they are removed from the head. A queue is just an ordered set of states. We use two new functions to access it.

- Add_Queue(D, s) adds state s to the tail of queue D,
- Del_Queue(D) deletes the element from the head of D and returns it.

This search procedure is illustrated in Figure 8.6.

**Figure 8.6 Breadth-First Search Algorithm**

Queue D = {}
Statespace V = {}

Start()
{
    Add_Statespace(V, A.s0)
    Add_Queue(D, A.s0)
    Search()
}

Search()
{
    s = Del_Queue(D)
    for each (s, l, s') ∈ A. T
    {
        if In_Statespace(V, s') == false
        {
            Add_Statespace(V, s')
            Add_Queue(D, s')
            Search()
        }
    }
}

Despite the similarities of depth-first and breadth-first searches, the two algorithms have quite different properties. For one, the depth-first search can easily be extended to detect cycles in graphs; the breadth-first search cannot. With the depth-first search algorithm, we also saw that it suffices to print out the contents of the stack to reconstruct an error path. If we want to do something similar with a breadth-first search, we have to store more information. One simple method is to store a link at state in state space V that points to one of the predecessors of each state. These links can then be followed to trace a path back from an error state to the initial system state when an error is encountered. It is then easy to use the breadth-first search algorithm for the detection of safety violations, for instance with the following extension that can be placed immediately after the point where a new state s is retrieved from queue D.

if !Safety(s)
{
    Find_Path(s)
}

We have introduced a new procedure Find_Path(s) here that traces back and reproduces the required error path. SPIN has an implementation of this procedure that is enabled by compiling the verifier source text with the optional compiler directive -DBFS. For the example specification, for instance, this gives us the shortest error path immediately.
Checking Liveness Properties

We will show how the basic algorithm from Figure 8.1 can be extended for the detection of liveness properties, as expressible in linear temporal logic. Liveness deals with infinite runs, \( \omega \)-runs. Clearly, we can only have an infinite run in a finite system if the run is cyclic: it reaches at least some of the states in the system infinitely often. We are particularly interested in cases where the set of states that are reached infinitely often contains one or more accepting states, since these runs correspond to \( \omega \)-accepting runs. We have seen in Chapter 6 how we can arrange things in such a way that accepting runs correspond precisely to the violation of linear temporal logic formulae.

An acceptance cycle in the reachability graph of automaton A exists if and only if two conditions are met. First, at least one accepting state is reachable from the initial state of the automaton A.s0. Second, at least one of those accepting states is reachable from itself.

The algorithm that is used in SPIN to detect reachable accepting states that are also reachable from themselves is shown in Figure 8.7. The state space and stack structures now store pairs of elements: a state and a boolean value toggle, for reasons we will see shortly.

Figure 8.7 Nested Depth-First Search for Checking Liveness Properties

Stack D = {}
Statespace V = {}
State seed = nil
Boolean toggle = false

Start()
{
    Add_Statespace(V, A.s0, toggle)
    Push_Stack(D, A.s0, toggle)
    Search()
}

Search()
{
    (s,toggle) = Top_Stack(D)
    for each (s, l, s') \( \in \) A. T
    {
        /* check if seed is reachable from itself */
        if s' == seed V On_Stack(D,s',false)
        {
            PrintStack(D)
            PopStack(D)
            return
        }

        if In_Statespace(V, s', toggle) == false
        {
            Add_Statespace(V, s', toggle)
            Push_Stack(D, s', toggle)
            Search()
        }
    }
    if s \( \in \) A. F & toggle == false
    {
        seed = s /* reachable accepting state */
        toggle = true
        Push_Stack(D, s, toggle)
        Search() /* start 2nd search */
        Pop_Stack(D)
        seed = nil
        toggle = false
    }
}

Pop_Stack(D)
Adding Fairness

LTL is rich enough to express many fairness constraints directly, for example, in properties of the form (□ trigger → ♠ response). Specific types of fairness can also be predefined and built into the search algorithm. Recall that the asynchronous product of finite automata that is the ultimate subject of LTL model checking is built as an interleaving of transitions from smaller automata, A = A1 x A2 ...Ak (cf. Appendix A). Each of the automata A1 x A2 ...Ak contributes transitions to the runs of A. Component automaton Ai is said to be enabled at state s of the global automaton A if’s has at least one valid outgoing transition from Ai. We can now define two standard notions of fairness.

Definition 8.1 (Strong Fairness)

An ω-run σ satisfies the strong fairness requirement if it contains infinitely many transitions from every component automaton that is enabled infinitely often in σ.

Definition 8.2 (Weak Fairness)

An ω-run σ satisfies the weak fairness requirement if it contains infinitely many transitions from every component automaton that is enabled infinitely long in σ.

The two definitions differ just in the use of the terms infinitely often and infinitely long, yet the computational overhead that is required to check these two requirements is vastly different. As we shall see shortly, the check for weak fairness increases the run-time expense of a verification run by a factor that is linear in the number of component automata (i.e., the number of running processes in a SPIN model). To check strong fairness within a system like SPIN, however, would increase the run time of a basic verification by a factor that is quadratic in the number of component automata, which for all practical purposes puts it beyond our reach. Not surprisingly, therefore, SPIN only includes support for weak fairness, and not for strong fairness.

SPIN’s implementation of the weak fairness requirement is based on Choueka’s flag construction method (see the Bibliographic Notes at the end of this chapter). Although the details of the implementation in SPIN are complex, it is not hard to describe the intuition behind the algorithm.

The depth-first search algorithm from Figure 8.1 explores the global reachability graph for an automaton A. Assume again that A itself is computed as the product of k component automata A1, ..., Ak. We will now create (k + 2) copies of the global reachability graph that is computed by the algorithm from Figure 8.1. We preserve the acceptance labels from all accepting states only in the first copy of the state graph, that for convenience we will call the 0-th copy. We remove the accepting labels from all states in the remaining (k + 1) copies. Next, we make some changes in the transition relation to connect all copies of the state graph, without really removing or adding any behavior.

We change the destination states for all outgoing transitions of accepting states in the 0-th copy of the state space, so that they point to the same states in the next copy of the state space, with copy number one.

In the i-th copy of the state graph, with 1 ≤ i ≤ k, we change the destination state of each transition that was contributed by component automaton Ai (i.e., the i-th process) to the same state in the (i + 1)-th copy of the state graph. For the last copy of the state space, numbered (k + 1), we change all transitions such that their destination state is now in the 0-th copy of the state graph.

The unfolding effect is illustrated in Figure 8.8, which is based on a similar figure in Bosnacki [2001].

Figure 8.8. (k+2) Times Unfolded State Space for Weak Fairness

```plaintext
_pid ≠ 1
_pid ≠ 2
```
The SPIN Implementation

(Can be skipped on a first reading.) SPIN's implementation of the weak fairness algorithm differs on minor points from the description we have given. The modifications are meant to reduce the memory and run-time requirements of the search.

A first difference is that the SPIN implementation does not actually store \((k + 2)\) full copies of each reachable state. Doing so would dramatically increase the memory requirements for the weak fairness option. It suffices to store just one copy of each state plus \((k + 2)\) bits of overhead. The additional bits record in which copy of the state graph each state was visited: the \(i\)-th bit is set when the state is encountered in the \(i\)-th copy of the state graph. Creating one extra copy of the state graph now requires just one extra bit per state. If the reachable state space contains \(R\) states, each of \(B\) bits, the memory requirements for the algorithm can thus be reduced from \((R \times B) \times (k + 2)\) to \((R \times B) + (k + 2)\) bits.

Another small difference is that the nested depth-first search for cycles is not initiated from an acceptance state in the 0-th copy of the state graph, but from the last copy of the state graph. Note that whenever this last copy is reached we can be certain of two things:

1. A reachable accepting state exists.
2. A (weakly) fair execution is possible starting from that accepting state.

Each state in the last copy of the state graph now serves as the seed state for a run of the nested depth-first search algorithm, in an effort to find a cycle. As before, all transitions from the last copy of the state graph move the system unconditionally back to the 0-th copy of the state graph, and therefore the only way to revisit the seed state is to pass an accepting state and close the cycle with a fair sequence of transitions.
Complexity Revisited

In the worst case, the algorithm from Figure 8.7 for checking liveness properties uses twice as much run time as the algorithm from Figure 8.2, which sufficed only for checking safety properties. Clearly, in the algorithm from Figure 8.7 each state can now appear in the state space twice: once with the a true toggle and once with a false toggle attribute. The algorithm can, however, be implemented with almost no memory overhead. As we noted earlier in the discussion of weak fairness, each state needs only be stored once, and not twice, with the right bookkeeping information. The bookkeeping information in this case requires just two bits per state. The first bit is set to one when the state is visited with a toggle value false; the second bit is set to one if the state is visited with a toggle value true (i.e., in the nested part of the search). Clearly, the combination (0,0) for these two bits will never be seen in practice, but each of the three remaining combinations can appear and the two bits together suffice to accurately identify all reached states separately in each of the two (virtual) state graphs.

The algorithm from Figure 8.2 incurs a computational expense that is linear in the number of reachable states for a given system model, that is, there is a largely fixed amount of work (computation time and memory space) associated with each reachable system state. Adding cycle detection increases the run-time expenses by a factor of maximally two, but does not impact the memory requirements noticeably. Adding a property automaton (e.g., a never claim generated from an LTL requirement) of N states increases the expense of a straight reachability by another factor of maximally N. The size N of the property automaton itself, though, can increase exponentially with the number of temporal operators used in an LTL formula. This exponential effect, though, is rarely, if ever, seen in practice.

Adding the weak fairness constraint causes an unfolding of the reachable state space by a factor of (k + 2), where k is the number of active processes in the system. In the implementation, the memory cost of the unfolding is reduced significantly by storing each copy of a reachable state not (k + 2) times but once, and annotating it with (k + 2) bits to record in which copies of the state graph the state has been encountered. If we use the nested depth-first search cycle detection method, the memory overhead per reachable state then remains limited to 2(k + 2) bits per reached state. In the worst case, though, the run-time requirements can increase by a factor of 2(k + 2), although in practice it is rare to see an increase greater than two.

Clearly, automated verification can be done most efficiently for pure safety properties: basic assertions, system invariants, absence of deadlock, etc. Next in efficiency is the verification of liveness properties: proving the absence of non-progress cycles or the presence of acceptance cycles. Next in complexity comes the verification of LTL properties. The more complex the temporal formula, the more states there can be in the corresponding property automaton, and the greater the computational expense of the verification can be. This is a worst-case assessment only, though. In many cases, there is a tight coupling between transitions in a property automaton that is generated from an LTL formula and the reachable states of a system, which means that often the computational expense is only modestly affected by the size of the property automaton or the size of the underlying LTL formula.
The best known alternative method to detect acceptance cycles in a finite graph is based on the construction of all the maximal strongly connected components in the graph. If at least one component contains at least one accepting state, then an accepting \( \omega \)-run can be constructed. The strongly connected components in a graph can be constructed with time and space that is linear in the size of the graph with a depth-first search, Tarjan [1972]. Tarjan's procedure requires the use of two integers to annotate each state (the depth-first number and the low-link number), while the nested depth-first search procedure from Figure 8.7 requires the addition of just two bits of information. Tarjan's procedure, though, can identify all accepting \( \omega \)-runs in a graph. The nested depth-first search procedure can always identify at least one such run, but not necessarily all. The nested depth-first search procedure is compatible with all lossless and lossy memory compression algorithms that we will explore in the next chapter, while Tarjan's procedure is not.

State space caching methods were described in Holzmann, Godefroid, and Pirottin [1992], and in Godefroid, Holzmann, and Pirottin [1995].

The nested depth-first search procedure was first described in Courcoubetis, Vardi, Wolper, and Yannakakis [1990], and its application to SPIN is described in Godefroid and Holzmann [1993]. A similar procedure for the detection of non-progress cycles can also be found in Holzmann [1991], and is discussed in more detail in Holzmann [2000]. A modification of the nested depth-first search procedure to secure compatibility with partial order reduction methods is described in Holzmann, Peled, and Yannakakis [1996].

Choueka's flag construction method was first described in Choueka [1974]. Its potential use for the enforcement of fairness with a nested depth-first search was mentioned in Courcoubetis et al. [1990]. An alternative, detailed description of SPIN's implementation of the weak fairness algorithm can be found in Chapters 3 and 7 of Bosnacki [2001].
Chapter 9. Search Optimization

"Don't find fault. Find a remedy."

— (Henry Ford, 1863–1947)

The basic algorithms for performing explicit state verification, as implemented in SPIN, are not very complicated. The hard problem in the construction of a verification system is therefore not so much in the implementation of these algorithms, but in finding effective ways to scale them to handle large to very large verification problems. In this chapter we discuss the methods that were implemented in SPIN to address this issue.

The optimization techniques we will review here have one of two possible aims: to reduce the number of reachable system states that must be searched to verify properties, or to reduce the amount of memory that is needed to store each state.

SPIN's partial order reduction strategy and statement merging technique fall into the first of these two categories. In the second category we find techniques that are based on either lossless or lossy compression methods. The former preserve the capability to perform exhaustive verifications, though often trading reductions in memory use for increases in run time. The lossy compression methods can be more aggressive in saving memory use without incurring run-time penalties, by trading reductions in both memory use and speed for a potential loss of coverage. The bitstate hashing method, for which SPIN is perhaps best known, falls into the latter category. A range of lossless compression methods is also supported in SPIN. We will briefly discuss the principle of operation of the hash-compact method, collapse compression, and the minimized automaton representation. We begin with a discussion of partial order reduction.
Partial Order Reduction

Consider the two finite state automata $T_1$ and $T_2$ shown in Figure 9.1. If we interpret the labels on the transitions, we can see that the execution of each system is meant to have a side effect on three data objects. The automata share access to an integer data object named $g$, and they each have access to a private data object, named $x$ and $y$, respectively. Assume that the initial value of all data objects is zero, and the range of possible values is 0...4.

**Figure 9.1. The Finite State Automata $T_1$ and $T_2$**

![Figure 9.1](image)

The expanded asynchronous product of $T_1$ and $T_2$ (cf. Appendix A) is illustrated in Figure 9.2. We have used the state labels in Figure 9.2 to record the values of the data objects in the order: $x$, $y$, $g$.

**Figure 9.2. Expanded Asynchronous Product of $T_1$ and $T_2**

![Figure 9.2](image)

The paths through the graph from Figure 9.2 represent all possible interleavings of the combined execution of the four statements from automata $T_1$ and $T_2$. Clearly, the two possible interleavings of the statements $x = 1$ and $y = 1$ both lead to the same result, where both $x$ and $y$ have value 1. The two possible interleavings of the statements $g = g + 2$ and $g = g \times 2$, on the other hand, lead to two different values for $g$. The underlying notion of data independence and data dependence can be exploited to define an equivalence relation on runs.

The system is small enough that we can exhaustively write down all finite runs. There are only six:

$\sigma_1 = \{(0, 0, 0), (1, 0, 0), (1, 0, 2), (1, 1, 2), (1, 1, 4)\}$

$\sigma_2 = \{(0, 0, 0), (1, 0, 0), (1, 1, 0), (1, 1, 2), (1, 1, 4)\}$

$\sigma_3 = \{(0, 0, 0), (1, 0, 0), (1, 1, 0), (1, 1, 0), (1, 1, 2)\}$

$\sigma_4 = \{(0, 0, 0), (0, 1, 0), (0, 1, 0), (1, 1, 0), (1, 1, 2)\}$

$\sigma_5 = \{(0, 0, 0), (0, 1, 0), (1, 1, 0), (1, 1, 0), (1, 1, 2)\}$

The first two runs differ only in the relative order of execution of the two transitions $y = 1$ and $g = g + 2$, which are independent operations. Similarly, runs $\sigma_4$ and $\sigma_5$ differ only in the relative order of execution of the independent operations $x = 1$ and $g = g \times 2$. By a process of elimination, we can reduce the number of distinct runs to just two, for instance to:

$\sigma_2 = \{(0, 0, 0), (1, 0, 0), (1, 1, 2), (1, 1, 4)\}$

$\sigma_3 = \{(0, 0, 0), (1, 0, 0), (1, 1, 2), (1, 1, 4)\}$

The four other runs can be obtained from these two by the permutation of adjacent independent operations. We have the following mutual dependencies in this set of transitions:

- $g = g \times 2$ and $g = g + 2$ because they touch the same data object
- $x = 1$ and $g = g + 2$ because they are both part of automaton $T_1$
- $y = 1$ and $g = g \times 2$ because they are both part of automaton $T_2$

The following operations are mutually independent:

- $x = 1$ and $y = 1$
- $x = 1$ and $g = g \times 2$
- $y = 1$ and $g = g + 2$

Using this classification of dependent and independent operations, we can partition the runs of the system into two equivalence classes: $\{\sigma_1, \sigma_2, \sigma_6\}$ and $\{\sigma_3, \sigma_4, \sigma_5\}$. Within each class, each run can be obtained from the other runs by one or more permutations of adjacent independent transitions. The eventual outcome of a computation remains unchanged under such permutations. For verification, it therefore would suffice to consider just one run from each equivalence class.

For the system from Figure 9.2 it would suffice, for instance, to consider only runs $\sigma_2$ and $\sigma_3$. In effect this restriction amounts to a reduction of the graph in Figure 9.2 to the portion that is spanned by the solid arrows, including only the states that are indicated in bold. There are three states fewer in this graph and only half the number of transitions, yet it would suffice to accurately prove LTL formulae such as:
Visibility

Would it be possible to formulate LTL properties for which a verification could return different results for the reduced graph and the full graph? To answer this question, consider the LTL formula

$$\square (x \geq y).$$

This formula indeed has the unfortunate property that it holds in the reduced graph but can be violated in the full graph.

What happened? The formula secretly introduces a data dependence that was assumed not to exist: it relates the values of the data objects x and y, while we earlier used the assumption that operations on these two data objects were always independent. The dependence of operations, therefore, does not just depend on automata structure and access to data, but also on the logical properties that we are interested in proving about a system. If we remove the pair x = 1 and y = 1 from the set of mutually independent operations, the number of equivalence classes of runs that we can deduce increases to four, and the reduced graph gains one extra state and two extra transitions.

The new graph will now correctly expose the last LTL formula as invalid, in both the full and in the reduced graph.

The potential benefits of partial order reduction are illustrated in Figure 9.3. Shown is the reduction in the number of states in the product graph that needs to be explored to perform model checking when partial order reduction is either enabled (solid line) or disabled (dashed line). In this case, the improvement increases exponentially with the problem size. It is not hard to construct cases where partial order reduction cannot contribute any improvement (e.g., if all operations are dependent). The challenge in implementing this strategy in a model checker is therefore to secure that in the worst case the graph construction will not suffer any noticeable overhead. This was done in the SPIN model checker with a static reduction method. In this case, the dependency relations are computed offline, before a model checking run is initiated, so that no noticeable run-time overhead is incurred.

**Figure 9.3. Effect of Partial Order Reduction Increase in Number of States as a Function of Problem Size (Sample of Best Case Performance for Leader Election Protocol)**

The partial order reduction strategy is enabled by default for all SPIN verification runs. There are a small number of language constructions that are not compatible with the enforcement of a partial order reduction strategy. They are listed in Chapter 16. In these cases, and for experimental purposes, the partial order reduction strategy can be disabled by compiling the verification code that is generated by SPIN with the compiler directive -DNOREDUCE.
Statement Merging

A special case of partial order reduction is a technique that tries to combine sequences of transitions within the same process into a single step, thus avoiding the creation of intermediate system states after each separate transition. The merging operation can be performed, for instance, for sequences of operations that touch only local data. In effect, this technique automatically adds d_steps into a specification, wherever this can safely be done.

To see the potential effect of statement merging, consider the following example:

```c
#define GLOBAL
byte c;
#endif

active proctype merging()
{
    #ifndef GLOBAL
    byte c;
    #endif
    if
    :: c = 0
    :: c = 1
    :: c = 2
    fi;
    do
    :: c < 2 -> c++
    :: c > 0 -> c--
    od
}
```

If we make the declaration for variable c global, none of the operations on this variable can be considered safe under the partial order reduction rules, and the statement merging technique cannot be applied.

Note that proctype merging has five control states, and variable c can take three different values, so there can be no more than fifteen system states.

There is one control state before, and one after the if statement. Then there is also one control state at each of the two arrow symbols. The fifth control control state is the termination state of the process: immediately following the do construct.

It turns out that only eight of these fifteen states can be reached, as confirmed by this first run:

```
$ spin -DGLOBAL -a merging.pml
$ cc -o pan pan.c
$ ./pan
(Spin Version 4.0.7 -- 1 August 2003)
+ Partial Order Reduction
Full statespace search for:
never claim             - (none specified)
assertion violations    +
acceptance cycles       - (not selected)
invalid end states      +
State-vector 16 byte, depth reached 6, errors: 0
8 states, stored
```

If we now turn c from a global into a local variable, all operations on this variable become local to the one process in this system, which means that the SPIN parser can recognize the corresponding transitions as necessarily independent from any other statement execution in the system. The statement merging technique can now combine the two option-sequences inside the do loop into a single step each, and thereby removes two of the control states. The result should be a reduction in the number of states that is reached in a verification. If we perform this experiment, we can see this effect confirmed:

```
$ spin -a merging.pml
$ cc -o pan pan.c
$ ./pan
(Spin Version 4.0.7 -- 1 August 2003)
+ Partial Order Reduction
Full statespace search for:
never claim             - (none specified)
assertion violations    +
acceptance cycles       - (not selected)
invalid end states      +
State-vector 16 byte, depth reached 3, errors: 0
4 states, stored
4 states, matched
8 transitions (= stored+matched)
0 atomic steps
```

There is one downside to the statement merging technique: it can make it harder to understand the automaton structure that is used in the verification process. Statement merging can be disabled with an extra command-line option in SPIN. For instance, if we generate the verifier as follows:

```
$ spin -a -o3 merging.pml
```

Statement merging is suppressed, and the system will again create eight system states during a verification.
State Compression

The aim of the partial order reduction strategy is to reduce the number of system states that needs to be visited and stored in the state space to solve the model checking problem. An orthogonal strategy is to reduce the amount of memory that is required to store each system state. This is the domain of memory compression techniques.

SPIN supports options for both lossless and lossy compression: the first type of compression reduces the memory requirements of an exhaustive search by increasing the run-time requirements. The second offers a range of proof approximation techniques that can work with very little memory, but without guarantees of exhaustive coverage.

We first consider lossless state compression. SPIN has two different algorithms of this type. The COLLAPSE compression mode exploits a hierarchical indexing method to achieve compression. The MA, or minimized automaton, compression mode reduces memory by building and updating a minimized finite state recognizer for state descriptors.
Collapse Compression

At first sight, it may strike us as somewhat curious that the number of distinct system states that the verifier can encounter during a search can become so large so quickly, despite the fact that each process and each data object can typically reach only a small number of distinct states (i.e., values). The explosion in the number of reachable system states is only caused by the relatively large number of ways in which the local states of individual system components, such as processes and data objects, can be combined. Replicating a complete description of all local components of the system state in each global state that is stored is therefore an inherently wasteful technique, although it can be implemented very efficiently.

SPIN’s collapse compression mode tries to exploit this observation by storing smaller state components separately while assigning small unique index numbers to each one. The unique index numbers for the smaller components are now combined to form the global state descriptor.

There are now several choices that can be made about how precisely to break down a global system state into separate components, ideally with as little correlation as possible between components. SPIN assigns components as illustrated in Figure 9.4.

Figure 9.4. State Components for COLLAPSE Compression

| GL: Descriptor for Global Data Objects |
| P1: Descriptor for Process 1           |
| P2: Descriptor for Process 2           |
| SV: GL:P1:P2 Global State Descriptor (state vector) |

A first component is formed by the set of all global data objects in the model, including the contents of all message channels, irrespective of whether they were declared locally or globally. This component also includes a length field that records the original length of the state vector (i.e., the state descriptor) before compression.

Next, there is one component for each active process, recording its control state together with the state of all its local variables, but excluding the contents of locally declared channels.

Because the number of component states cannot be known in advance, the method should be able to adjust the number of bits it uses to record index values. The SPIN implementation does this by adding an extra two bits to each component index to record how many bytes are used for the corresponding index field. In this way, the compressor can use up to four bytes per index, which suffices for up to 2^32 possible separate component states. The table of index widths is added to the global variables component. The width of the index for the global variables component itself is stored in a fixed separate byte of the compressed state descriptor.

To make sure no false partial matches can occur, the length of each separately stored component is also always stored with the component data.

The collapse compression method is invoked by compiling the verifier source text that is generated by SPIN with the extra compile-time directive -DCOLLAPSE. For instance:

```bash
$ spin -a model
$ cc -DCOLLAPSE -o pan pan.c
$ ./pan
```
Minimized Automaton Representation

A second lossless compression method that is supported in SPIN optionally stores the set of reachable system states not in a conventional lookup table, but instead performs state matching by building and maintaining a minimal deterministic finite state automaton that acts as a recognizer for sets of state descriptors. The automaton, represented as a finite graph, is interrogated for every system state encountered during the search, and updated immediately if a new state descriptor is seen. The savings in memory use with this method can be very large, sometimes allowing the verifier to use exponentially smaller amounts of memory than required for the standard search methods. The run-time penalty, though, can be very significant.

Figure 9.5 shows the minimized automaton structure for a state descriptor of three bits, after the first three state descriptors have been stored. All paths in the automaton that lead from node s0 to the accepting state s6 are part of the state space, all paths from node s0 to the non-accepting terminal state s3 are not part of the state space. The dashed lines separate the subsequent layers in the automaton. The edges between the node in the first (left-most) layer and the second layer represent the possible values of the first bit in the state descriptor, those between the second and the third layer represent possible values of the second bit, and so on.

Figure 9.5. Minimized Automaton Structure After Storing \{000, 001, 101\}

Figure 9.6 shows how this structure is updated when one more state descriptor is added, again restoring the minimized form. There is a close resemblance between this minimized automaton structure and OBDDs (ordered binary decision diagrams). In our implementation of this storage method, each node in the graph does not represent a single bit but a byte of information, and each node therefore can have up to 255 outgoing edges. Edges are merged into ranges wherever possible to speed up the lookup and update procedures.

Figure 9.6. Automaton Structure After Storing \{000, 001, 101, 100\}

In principle, the minimized automaton has the same expected complexity as the standard search based on the storage of system states in a hashed lookup table. In both cases, an update of the state space has expected complexity O(S), with S the maximum length of the state descriptor for a system state. The constant factors in both procedures are very different, though, which means that the minimized automaton procedure can consume considerably more time than the other optimization algorithms that are implemented in SPIN. Nonetheless, when memory is at a premium, it can well be worth the extra wait to use the more aggressive reduction technique.
Bitstate Hashing

The standard depth-first search algorithm constructs a set of states. Each state that is explored in the verification process is stored in a state space. Since the model checking problem for all practical purposes is reduced to the solution of a reachability problem (cf. Chapter 8), all the model checker does is construct states and check whether they were previously visited or new. The performance of a model checker is determined by how fast it can do this.

The state space structure serves to prevent the re-exploration of previously visited states during the search: it turns what would otherwise be an exponential algorithm into a linear one, that visits every reachable state in the graph at most once. To enable fast lookup of states, the states are normally stored in a hash table, as illustrated in Figure 9.7.

**Figure 9.7. Standard Hash Table Lookup**

Assume we have a hash table with \( h \) slots. Each slot contains a list of zero or more states. To determine in which list we store a new state \( s \), we compute a hash-value \( \text{hash}(s) \), unique to \( s \) and randomly chosen in the range \( 0..h-1 \). We check the states stored in the list in hash table slot \( \text{hash}(s) \) for a possible match with \( s \). If a match is found, the state was previously visited and need not be explored again. If no match is found, state \( s \) is added to the list, and the search continues.

Each state is represented in memory as a sequence of \( S \) bits. A simple (but very slow) hashing method would be to consider the array of bits as one large unsigned integer, and to calculate the remainder of its division by \( h \), with \( h \) a prime number. A more efficient method, and one of the methods implemented in SPIN, is to use a checksum polynomial to compute the hash values. We now choose \( h \) as a power of 2 and use the polynomial to compute a checksum of \( \log(h) \) bits. This checksum is then used as the hash value.

The default hashing method that is currently implemented in SPIN is based on a method known as Jenkins' hash. It is slightly slower than the checksum polynomial method, but it can be shown to give notably better coverage.

Let \( r \) be the number of states stored in the hash table and \( h \) the number of slots in that table. When \( h >> r \), each state can be stored in a different slot, provided that the hash function is of sufficiently good quality. The lists stored in each slot of the hash table will either be empty or contain one single state. State storage has only a constant overhead in this case, carrying virtually no time penalty.

When \( h < r \), there will be cases for which the hash function computes the same hash value for different states. These hash collisions are resolved by placing all states that hash to the same value in a linked list at the corresponding slot in the hash table. In this case we may have to do multiple state comparisons for each new state that is checked against the hash table: towards the end of the search on average \( r/h \) comparisons will be required per state. The overhead incurred increases linearly with growing \( r/h \), once the number of stored states \( r \) exceeds \( h \).

Clearly, we would like to be in the situation where \( h >> r \). In this case, a hash value uniquely identifies a state, with low probability of collision. The only information that is contained in the hash table is now primarily whether or not the state that corresponds to the hash value has been visited. This is one single bit of information. A rash proposal is now
Bloom Filters

Let \( m \) again be the size of the hash table in bits, \( r \) is the number of states stored, and \( k \) the number of hash functions used. That is, we store \( k \) bits for each state stored, with each of the \( k \) bit-positions computed with an independent hash function that uses the \( S \) bits of the state descriptor as the key.

Initially, all bits in the hash table are zero. When \( r \) states have been stored, the probability that any one specific bit is still zero is:

\[
\left(1 - \frac{1}{m}\right)^k \cdot r
\]

The probability of a hash collision on the \((r + 1)\)st state entered is then

\[
\left(1 - \left(1 - \frac{1}{m}\right)^k \cdot r\right)^k \approx \left(1 - e^{-k \cdot m/r}\right)^k
\]

which gives us an upper-bound for the probability of hash collisions on the first \( r \) states entered. (The probability of a hash collision is trivially zero for the first state entered.) The probability of hash collisions is minimal when \( k = \log(2) \cdot m/r \), which gives

\[
\left(\frac{1}{2}\right)^k = 0.6185^{m/r}
\]

For \( m = 109 \) and \( r = 107 \) this gives us an upper-bound on the probability of collision in the order 10-21, for a value of \( k = 89.315 \). Figure 9.8 illustrates these dependencies.

**Figure 9.8. Optimal Number of Hash Functions and Probability of Hash Collision** The dashed line plots the probability for optimal \( k \), the dotted line plots the probabilities for fixed \( k = 2 \), the solid line plots the optimal value for \( k \), \( 1 \leq k < 100 \).
Hash-Compact

An interesting variant of this strategy is the hash-compact method, first proposed for use in verification by Pierre Wolper. In this case we try to increase the size of \( m \) far beyond what would be available on an average machine, for instance to 264 bits. We now compute a single hash value within the range \( 0..(2^{64}-1) \) as a 64-bit number, and store this number, instead of the full state \( s \), in a regular hash table. We have one hash function, so \( k = 1 \), and we simulate a memory size of \( m = 2^{64} \gg 1019 \) bits. For the value of \( r = 107 \), we then get a probability of collision near \( 10^{-57} \), giving an expected coverage of 100%. To store 107 64-bit numbers takes less than \( m = 109 \) bits. Instead of storing 64 bits at a time, we can also store a smaller or larger number of bits. The maximum number of bits that could be accommodated is trivially \( m/r \). The 64-bit version of hash-compact, then, should be expected to perform best when \( 64 \leq m \leq r.S \). Unfortunately, although \( m \) and \( S \) are often known a priori, in most cases \( r \) is usually not known before an exhaustive verification is completed, and therefore the optimal ratio \( m/r \) is also typically unknown.

A measurement of the performance of the hash-compact method and double-bit hashing (i.e., with two independent hash functions) for a fixed problem size \( r \) and available memory \( m \) varying from 0 to \( m > r.S \) is shown in Figure 9.9, which is taken from Holzmann [1998].

**Figure 9.9. Measured Coverage of Double Bitstate Hashing (k=2) Compared with Hash-Compact (hc), and Exhaustive Search**

![Figure 9.9](image)

**Problem size:** 427567 reachable states, state descriptor 1376 bits

When sufficient memory is available, traditional exhaustive state storage is preferred, since it gives full coverage with certainty. For the problem shown in Figure 9.9 this is the area of the graph with \( m > 229 \). Barring this, if sufficient memory is available for the hash-compact method, then this is the preferred method. This is the area of the graph where \( 223 < m < 229 \). Below that, in Figure 9.9 for all values \( m < 223 \), the double-bit hashing method is superior. The latter method, for instance, still achieves a problem coverage here of 50% when only 0.1% of the memory resources required for an traditional exhaustive search are available.

The hash-compact method can be enabled by compiling a SPIN-generated verifier with the compiler directive HC4, for instance as follows (see also Chapter 19, p. 530):

```bash
$ spin -a model
$ cc -DHC4 -o pan pan.c
$ ./pan
```

Applying the hash-compact to the leader election protocol from before, using four bytes per state, produces this result:

```bash
$ cc -DNOREDUCE -DMEMLIM=200 -DHC4 -o pan pan.c
$ time ./pan
(Spin Version 4.0.7 -- 1 August 2003)
```
Bibliographic Notes

A formal treatment of the notions of dependence of actions (transitions) and the equivalence of \( \omega \)-runs can be found in, for instance, Mazurkiewicz [1986], and Kwiatkowska [1989]. The application of these notions to model checking is described in Peled [1994], and Holzmann and Peled [1994], with a small, but important, adjustment that is explained in Holzmann, Peled, and Yannakakis [1996].

A formal proof of correctness of the partial order reduction algorithm implemented in SPIN is given in Chou and Peled [1999], and is also discussed in Clarke, Grumberg, and Peled [2000].

The statement merging technique that is implemented in SPIN was first proposed in Schoot and Ural [1996]. The SPIN implementation is discussed in Holzmann [1999].

The COLLPASE compression method is described in detail in Holzmann [1997]. The design and implementation of the minimized automaton storage method is detailed in Holzmann and Puri [1999]. There are several interesting similarities, but also significant differences, between the minimized automaton procedure and methods based on the use of BDDs (binary decision diagrams) that are commonly used in model checking tools for hardware circuit verification. A discussion of these and other points can be found in Holzmann and Puri [1999].

The application of the hash-compact method to verification was described in Wolper and Leroy [1993], and also independently in Stern and Dill [1995]. An earlier theoretical treatment of this storage method can also be found in Carter at al. [1978].

Bitstate hashing, sometimes called supertrace, was introduced in Holzmann [1988] and studied in more detail in Holzmann [1998]. The first explicit description of the notion of bitstate hashing, though not the term, appeared in Morris [1968], in a paper on "scatter storage" techniques. In Bob Morris's original paper, the technique was mentioned mostly as a theoretical curiosity, unlikely to have serious applications. Dennis Ritchie and Doug McIlroy found an application of this storage technique in 1979 to speed up the UNIX spelling checking program, as later described in McIlroy [1982].

The original implementation of spell was done by Steve Johnson. The new, faster version was written by Dennis Ritchie, and was distributed as part of the 7th Edition version of UNIX. The mathematics McIlroy used in his 1982 paper to explain the working of the method is similar to the elegant exposition from Bloom [1970]. Bloom's 1970 paper, in turn, was written in response to Morris [1968], but was rediscovered only recently. Bob Morris, Dennis Ritchie, Doug McIlroy, and Steve Johnson all worked in the UNIX group at Bell Labs at the time.

The code used in the 1979 version of spell for table lookup differs significantly from the version that is used in the SPIN implementation for bitstate hashing, given the differences in target use. The first hash function that was implemented in SPIN for default state storage during verification was based on the computation of 32-bit cyclic redundancy checksum polynomials, and was implemented in close collaboration with (then) Bell Labs researchers Jim Reeds, Ken Thompson, and Rob Pike.

The current hashing code used in SPIN is based on Jenkins [1997]. Jenkins' hash function is slightly slower than the original code, but it incurs fewer collisions. The original hash functions are reinstated when the pan.c source code is compiled with directive -DOHASH.
Chapter 10. Notes on Model Extraction

"In all affairs it's a healthy thing now and then to hang a question mark on the things you have long taken for granted."

—(Bertrand Russell, 1872–1970)

Arguably, the most powerful tool we have in our arsenal for the verification of software applications is logical abstraction. By capturing the essence of a design in a mathematical model, we can often demonstrate conclusively that the design has certain inevitable properties. The purpose of a verification model, then, is to enable proof. If it fails to do so, within the resource limits that are available to the verification system, the model should be considered inadequate.
The Role of Abstraction

The type of abstraction that is appropriate for a given application depends both on the type of logical properties that we are interested in proving and on the resource limits of the verification system. This situation is quite familiar: it is no different from the one that applies in standard mathematics. When we reason about the correctness of a system without the benefit of a mechanized prover, using straight logic and pen and paper mathematics, we must also use our judgement in deciding which parts of a system are relevant, and which are not, with respect to the properties to be proven. Similarly, we must be aware of resource limitations in this situation as well. If only a very limited amount of time, or a very limited amount of mathematical talent, is available for rendering the proof, perhaps a coarser proof would have to be used. If unlimited time and talent is available, a more detailed proof may be possible. Whether we choose a mechanized process or a manual one, we have to recognize that some really difficult types of problems may remain beyond our reach. It is the skill of the verifier to solve as much of a problem as is feasible, within given resource limits.

For the best choice of an abstraction method in the construction of a verification model, we unavoidably have to rely on human judgement. Which parts of the system should we look at? What properties should apply? These types of decisions would be hard to automate. But even though there will unavoidably be a human element in the setup of a verification process, once the basic decisions about abstractions are made and recorded, it should in principle be possible to mechanize the remainder of the verification process.

Given the source text of an application and the properties of interest, we would like to generate a verification model automatically from the source text, where the model extraction process is guided by a user-defined abstraction function. In this chapter we discuss how we can do so.
From ANSI-C to PROMELA

To get an impression of what it takes to mechanically convert a C program into a PROMELA model, consider the following program. The program is one of the first examples used in Kernighan and Ritchie's introduction to the C programming language, with a slightly more interesting control structure than the infamous hello world example.

```c
#include <stdio.h>

int main(void)
{
    int lower, upper, step;
    float fahr, celsius;

    lower = 0;
    upper = 300;
    step = 20;

    fahr = lower;
    while (fahr <= upper) {
        celsius = (5.0/9.0) * (fahr - 32.0);
        printf("%4.0f %6.1f\n", fahr, celsius);
        fahr = fahr + step;
    }
}
```

The program defines a function called main, declares five local variables, and does some standard manipulations to compute a conversion table from temperature measured in degrees Fahrenheit to the equivalent expressed in degrees Celsius. Suppose we wanted to convert this little program into a PROMELA model. The first problem we would run into is that PROMELA does not support the C data-type float, and has no keyword while. The control-structure that is used in the program, though, could easily be expressed in PROMELA. If we ignore the data-types for the moment, and pretend that they are integers, the while loop could be expressed like this:

```c
fahr = lower;
do
:: (fahr <= upper) ->
    celsius = (5/9) * (fahr-32);
    printf("%d %d\n", fahr, celsius);
    fahr = fahr + step;
:: else -> break
od
```

It is not hard to see almost all control-flow structures that can be defined in C can be replicated in PROMELA. (There are some exceptions, though, that we will consider shortly.) The control structure can be derived, for instance, from the standard parse-tree representation of a program that is constructed by a C compiler. Figure 10.1 shows a parse tree for the example temperature conversion program.

**Figure 10.1. The Complete Parse Tree for fahr.c**
Embedded Assertions

Because SPIN lacks a parser for the C language, it has to treat all embedded C code fragments as trusted code that is passed through to the model checker as user-defined text strings. The intent is that the C code fragments are generated by a model extraction program, but even then the possibility still exists that the code thus generated may contain subtle bugs that cannot be intercepted by the model checker either, and that could cause the program to crash without producing any useful results. A mild remedy is to allow the user, or model extractor, to annotate every c_expr and c_code statement with a precondition that, if it evaluates to true, can guarantee that the statement can be executed correctly.

The preconditions act as embedded assertions. We can write, for instance

```c
\begin{verbatim}
c_state "int *ptr;" "Local main"
... c_code [Pmain->ptr != NULL] { *(Pmain->ptr) = 5; };;
\end{verbatim}
```

to state that the integer pointer variable ptr must have a non-zero value for the pointer dereference operation that follows in the code fragment to be safely executable. If a case is found where ptr evaluates to NULL (i.e., the precondition evaluates to false), then an assertion violation is reported and an error trail can be generated. Without the optional precondition, the model checker would try to execute the dereference operation without checks, and an unhelpful crash of the program would result.

We can use this feature to intercept at least some very common causes of program failures: nil-pointer dereferencing, illegal memory access operations, and out of bound array indexing operations. Consider the following example. For simplicity, we will ignore standard prefixing on state variables for a moment, and illustrate the concept here with access to non-state variables only.

```c
\begin{verbatim}
c_code {
    int *ptr;
    int x[256];
    int j;
};
... c_code { ptr = x; };
if :: c_expr [j >= 0 && j < 256] { x[j] != 25 } -> c_code [ptr >= x && ptr < &x[256]) { *ptr = 25; } :: else fi
\end{verbatim}
```

If the variable j is not initialized, more than likely it would cause an out of bound array index in the c_expr statement. The precondition checks for the bounds, so that such an occurrence can be intercepted as a failure to satisfy the precondition of the statement. Similarly, the correctness of indirect access to array locations via pointer ptr can be secured with the use of a precondition.
A Framework for Abstraction

Let us take another look at the temperature conversion example. We have noted that we can distinguish the problem of converting the control flow structure of the program cleanly from the problem of converting the actions that are performed: the basic statements. Converting the control flow structure is the easier of the two problems, although there can be some thorny issues there that we will consider more closely later.

We will now consider how we can apply user-defined abstractions systematically to the statements that appear in a program. It is important to note that the control flow aspect of a program is only of secondary importance in this regard. Once some of the basic statements in a program have been replaced with abstracted versions, it may well be that also the control flow structure of the program can be simplified. The latter is only done, though, if it does not change the meaning of the program. We will see some examples of this notion shortly. The abstractions we will consider here are applied exclusively to the basic statements that appear in a program, and to the data objects that they access.

Given an ANSI-C program, like the Fahrenheit to Celsius conversion example, the model extractor MODEX can generate a default translation of each procedure that appears in the program into a PROMELA proctype, using embedded C code fragments to reproduce those statements that have no equivalent in PROMELA itself. The translation can be specified as a MODEX lookup table, using a simple two column format with the source text on the left and the text for the corresponding abstraction to be used in the verification model on the right. For instance, a lookup table that describes the defaults used in MODEX (i.e., without user-defined abstraction) for the Fahrenheit program would map the nine entries:

\[
\begin{array}{ll}
(fahr<=upper) & \text{keep} \\
(! (fahr<=upper) & \text{else} \\
\text{lower}=0 & \text{keep} \\
\text{upper}=300 & \text{keep} \\
\text{step}=20 & \text{keep} \\
\text{fahr}=\text{lower} & \text{keep} \\
\text{fahr}=(\text{fahr}+\text{step}) & \text{keep} \\
\text{celsius}=\left((\frac{5}{9})\times(\text{fahr}-32)\right) & \text{keep} \\
\text{printf}("%4.0f \ \%6.1f\n", \text{fahr}, \text{celsius}) & \text{keep}
\end{array}
\]

The first entry in the table is the conditional from the while statement in the C version of the code. The negation of that statement, corresponding to the exit condition from the loop, appears as a separate entry in the table, to make it possible to define a different translation for it. It would, for instance, be possible to replace the target code for both the loop condition and the loop exit condition with the boolean value true to create a non-deterministic control structure in the model. (In this case, of course, this would not be helpful.) The default conversion for the remaining statements simply embeds the original code within a PROMELA code statement, and prefixes every variable reference so that it is visible in the model:

\[
\begin{array}{l}
c\_expr \{ \text{(Pmain->fahr<=Pmain->upper) } \} \\
ex\text{else} \\
c\_code \{ \text{Pmain->lower}=0; } \\
c\_code \{ \text{Pmain->upper}=300; } \\
c\_code \{ \text{Pmain->step}=20; } \\
c\_code \{ \text{Pmain->fahr}=\text{Pmain->lower}; } \\
c\_code \{ \text{Pmain->fahr}=\text{(Pmain->fahr+Pmain->step)}; } \\
c\_code \{ \text{Pmain->celsius}=\left((\frac{5.0}{9.0})\times(\text{Pmain->fahr}-32.0)\right)\} \\
c\_code \{ \text{printf}("%4.0f \ \%6.1f\n", } \\
\text{Pmain->fahr, Pmain->celsius); } \}
\end{array}
\]

The first entry in the table is the conditional from the while statement in the C version of the code. The negation of that statement, corresponding to the exit condition from the loop, appears as a separate entry in the table, to make it possible to define a different translation for it. It would, for instance, be possible to replace the target code for both the loop condition and the loop exit condition with the boolean value true to create a non-deterministic control structure in the model. (In this case, of course, this would not be helpful.) The default conversion for the remaining statements simply embeds the original code within a PROMELA code statement, and prefixes every variable reference so that it is visible in the model.
Sound and Complete Abstraction

One critical issue that we have not yet discussed is how we can define abstractions and how we can make sure that they are meaningful. The best abstraction to be used in a given application will depend on the types of correctness properties that we are interested in proving. The properties alone determine which aspects of the application are relevant to the verification attempt, and which are not.

Let P be the original program, and let L be a logical property we want to prove about P. Let further \( \alpha \) be an abstraction function.

Let us begin by considering the case where abstraction \( \alpha \) is defined as a MODEX lookup table. We will denote by \( \alpha(P) \) the abstract model that is derived by MODEX from program P for abstraction \( \alpha \). That is, \( \alpha(P) \) is the model in which every basic statement in P is replaced with its target from the MODEX lookup table, but with the same control flow structure which is reproduced in the syntax of PROMELA.

Under a given abstraction \( \alpha \), the original property L will generally need to be modified to be usable as a property of the abstract model \( \alpha(P) \). Property L may, for instance, refer to program locations in P or refer to data objects that were deleted or renamed by \( \alpha \). L may also refer to data objects for which the type was changed, for instance, from integer to boolean. We will denote this abstraction of L by \( \alpha(L) \).

The inverse of abstraction \( \alpha \) can be called a concretization, which we will denote by \( \bar{\alpha} \). A concretization can be used to translate, or lift, abstract statements from the model back into the concrete domain of the original program. In general, because of the nature of abstraction, any given abstract statement can map to one or more possible concrete statements. This means that for a given statements \( s \), \( \alpha(s) \) defines a single abstract statement, but concretization \( \bar{\alpha}(\alpha(s)) \) defines a set of possible concrete statements, such that

\[ \forall s, s \in \bar{\alpha}(\alpha(s)). \]

Similarly, for every abstract execution sequence \( \phi \) in model \( \alpha(P) \) we can derive a set of concrete execution sequences, denoted by \( \bar{\alpha}(\phi) \), in the original program. Given that an abstraction will almost always remove some information from a program, it is not necessarily the case that for every feasible execution \( \phi \) of the abstract program there also exists a corresponding feasible execution within \( \bar{\alpha}(\phi) \) of the concrete program. This brings us to the definition of two useful types of requirements that we can impose on abstractions: logical soundness and completeness.

**Definition 10.1 (Logical Soundness)**

Abstraction \( \alpha \) is logically sound with respect to program P and property L if for any concrete execution \( \phi \) of P that violates L there exists a corresponding abstract execution of \( \alpha(P) \) in \( \alpha(\phi) \) that violates \( \alpha(L) \).

Informally, this means that an abstraction is logically sound if it excludes the possibility of false positives. The correctness of the model always implies the correctness of the program.

**Definition 10.2 (Logical Completeness)**

Abstraction \( \alpha \) is logically complete with respect to program P and property L if, for any abstract execution \( \phi \) of \( \alpha(P) \) that violates \( \alpha(L) \), there exists a corresponding concrete execution of P in \( \bar{\alpha}(\phi) \) that violates L.

Informally, this means that an abstraction is logically complete if it excludes the possibility of false negatives. The incorrectness of the model always implies the incorrectness of the program.
Selective Data Hiding

An example of a fairly conservative and simple abstraction method that guarantees logical soundness and completeness with respect to any property that can be defined in LTL is selective data hiding. To use this method we must be able to identify a set of data objects that is provably irrelevant to the correctness properties that we are interested in proving about a model, and that can therefore be removed from the model, together with all associated operations.

This abstraction method can be automated by applying a fairly simple version of a program slicing algorithm. One such algorithm is built into SPIN. This algorithm computes, based on the given properties, which statements can be omitted from the model without affecting the soundness and completeness of the verification of those properties. The algorithm works as follows. First, a set of slice criteria is constructed, initially including only those data objects that are referred to explicitly in one or more correctness properties (e.g., in basic assertions or in an LTL formula). Through data and control dependency analysis, the algorithm then determines on which larger set of data objects the slice criteria depend for their values. All data objects that are independent of the slice criteria, and not contained in the set of slice criteria themselves, can then be considered irrelevant to the verification and can be removed from the model, together with all associated operations.

The data hiding operation can be implemented trivially with the help of a MODEX lookup table, by arranging for all irrelevant data manipulations to be mapped to either true (for condition statements) or to skip (for other statements). Note that under this transformation the basic control flow structure of the model is still retained, which means that no execution cycles can be added to or removed from the model, which is important to the preservation of liveness properties.

Although this method can be shown to preserve both logical soundness and logical completeness of the correctness properties that are used in deriving the abstraction, it does not necessarily have these desirable properties for some other types of correctness requirements that cannot be expressed in assertions or in LTL formulae. An example of such a property is absence of deadlock. Note that the introduction of extra behavior in a model can result in the disappearance of system deadlocks.
Example

To illustrate the use of selective data hiding, consider the model of a word count program shown in Figure 10.5. The program receives characters, encoded as integers, over the channel stdin, and counts the number of newlines, characters, and white-space separated words, up to an end-of-file marker which is encoded as the number -1.

Figure 10.5 Word Count Model

1 chan STDIN;
2 int c, nl, nw, nc;
3
4 init {
5     bool inword = false;
6     do
7         :: STDIN?c ->
8             if
9                 :: c == -1 -> break /* EOF */
10                :: c == '\n' -> nc++; nl++
11                :: else -> nc++
12            fi;
13         if
14             :: true ->
15                 skip
16             :: true ->
17                 if
18                     :: true ->
19                         skip; skip
20                 :: true
21             fi
22         fi
23     od;
24     assert(nc >= nl);
25     printf("%d\t%d\n", nl, nc)
26 }

The assertion checks that at the end of each execution the number of characters counted must always be larger than or equal to the number of newlines. We want to find a simpler version of the model that would allow us to check this specific property more efficiently. Variables nc and nl are clearly relevant to this verification, since they appear explicitly in the assertions. So clearly the statements in which these variables appear cannot be removed from the model. But which other statements can safely be removed?

When we invoke SPIN's built-in slicing algorithm it tells us:

$ spin -A wc.pml
spin: redundant in proctype :init: (for given property):
  line 19 ... [!(inword)]
  line 20 ... [nw = (nw+1)]
  line 20 ... [inword = true]
  line 15 ... [(((c==' ')||(c=='\t'))||(c=='\n'))]
  line 16 ... [inword = false]

spin: redundant vars (for given property):
  int    nw    0   <:global:> <variable>
  bit    inword 0   <init:> <variable>
spin: consider using predicate abstraction to replace:
  int    c    0   <:global:> <variable>

From this output we can conclude that the program fragment between lines 14 to 23 is irrelevant, and similarly variables nw and inword. SPIN also suggests that the declaration of variable c could be improved: it is declared as an integer variable, but within the model only three or four value ranges of this variable are really relevant. We could do better by using four symbolic values for those ranges, and declaring c as an mtype variable. This suggestion, though, is independent of the data hiding abstraction that we can now apply. If we preserve the entire control-flow structure of the original, the abstraction based on data hiding could now be constructed (manually) as shown in Figure 10.6.

Figure 10.6 Abstracted Word Count Model

1 chan STDIN;
2 int c, nl, nc;
3
4 init {
5     bool inword = false;
6     do
7         :: STDIN?c ->
8             if
9                 :: c == -1 -> break /* EOF */
10                :: c == '\n' -> nc++; nl++
11                :: else -> nc++
12            fi;
13         if
14             :: true ->
15                 skip
16             :: true ->
17                 if
18                     :: true ->
19                         skip; skip
20                 :: true
21             fi
22         fi
23     od;
24     assert(nc >= nl);
25     printf("%d\t%d\n", nl, nc)
26 }

We can simplify this model without adding or deleting any control-flow cycles, by collapsing sequences of consecutive true and skip statements. It is important that we do not add or omit cycles from the model in simplifications of this type, because this can directly affect the proof of liveness properties. A cycle, for instance, could only safely be added to or omitted from the model if we separately prove that the cycle always terminates within a finite number of traversals. The simplified model looks as shown in Figure 10.7.

Figure 10.7 Simplified Model

1 chan STDIN;
2 int c, nl, nc;
3
4 init {
5     do
6         :: STDIN?c ->
7             if
8                 :: c == -1 -> break /* EOF */
9                :: c == '\n' -> nc++; nl++
10                :: else -> nc++
11             fi;
12         if
13             :: true ->
14                 skip
15             :: true ->
16                 if
17                     :: true ->
18                         skip; skip
19                 :: true
20             fi
21         fi
22     od;
23     assert(nc >= nl);
24     printf("%d\t%d\n", nl, nc)
25 }

Because the abstraction we have applied is sound and complete, any possible execution that would lead to an assertion violation in this simplified model implies immediately that a similar violating execution must exist in the original concrete model. Perhaps surprisingly, there is indeed such an execution. An assertion violation can occur when the value of variable nc wraps around its maximal value of 232 - 1 before the value of variable nl does, which can happen for a sufficiently large number of input characters.
**Bolder Abstractions**

Logically sound and complete abstractions are not always sufficient to render large verification problems tractable. In those cases, one has to resort to abstraction strategies that lack either one or both of these qualities. These abstraction strategies are often based on human judgement of what the most interesting, or most suspect, system behaviors might be, and can therefore usually not be automated. Using these strategies also puts a greater burden on the user to rule out the possibility of false negatives or positives with additional, and often manual, analyses.

We will discuss two examples of abstraction methods in this class:

- Selective restriction
- Data type abstraction

The first method is neither sound nor complete. The second method is complete, but not necessarily sound.

Selective restriction is commonly used in applications of model checking tools to limit the scope of a verification to a subset of the original problem. We can do so, for instance, by limiting the maximum capacity of message buffers below what would be needed for a full verification, or by limiting the maximum number of active processes. This method is indubitably useful in an exploratory phase of a verification, to study problem variants with an often significantly lower computational complexity than the full problem that is to be solved. This type of abstraction, though, is to be used with care since it can introduce both false negatives and false positives into the verification process. An example of this type of selective restriction is, for instance, the verification model of a leader election algorithm that can be found in the standard SPIN distribution. To make finite state model checking possible, the number of processes that participate in the leader election procedure must be fixed, although clearly the full problem would require us to perform a verification for every conceivable number of processes. As another example from the same set of verification models in the SPIN distribution, consider the PROMELA model of a file transfer protocol named pftp. For exhaustive verification, each channel size should be set to a bound larger than the largest number of messages that can ever be stored in the channel. By lowering the bound, partial verifications can be done at a lower cost, though without any guarantee of soundness or completeness.

Data type abstraction aims to reduce the value range of selected data objects. An example of this type of abstraction could be to reduce a variable of type integer to an enumeration variable with just three values. The three values can then be used to represent three ranges of values in the integer domain (e.g., negative, zero, and positive). The change can be justified if the correctness properties of a model do not depend on detailed values, but only on the chosen value ranges.

A data type abstraction applied to one variable will generally also affect other variables within the same model. The type of, and operations on, all variables that depend on the modified variables, either directly or indirectly, may have to be adjusted. A data and control dependency analysis can again serve to identify the set of data objects that is affected in this operation, and can be used to deduce the required changes.

Denote by $V$ the set of concrete values of an object and by $A$ the associated set of abstract values under type abstraction $\alpha$. To guarantee logical completeness, a data type abstraction must satisfy the following relation, known as the Galois connection:[2]

\[ \forall \nu \in V, \nu \in \overline{\alpha}(\nu) \land \forall \omega \in A, \forall \xi \in \overline{\alpha}(\omega), \omega = \alpha(\xi). \]

[2] Note that concretization function $\overline{\alpha}$ defines a set.

\[ \forall (x \leq 0) \rightarrow \forall (x > 0) \]

Consider, for instance, the property

\[ \forall x \in V, \overline{\alpha}(x) \land \forall \omega \in A, \forall \xi \in \overline{\alpha}(\omega), \omega = \alpha(\xi). \]

The property depends only on the sign of variable $x$, but not on its absolute value. With a data type abstraction we can try to replace every occurrence of $x$ in the model with a new variable that captures only its sign, and not its value. For example, if the model contains assignment and condition statements such as

$(x > 5); x = 0; x++$

we can replace all occurrences of $x$ in these statements with a new boolean variable $\text{neg}_x$. The property then becomes:

The assignments and conditions are now mapped as shown in Table 10.1. Under this abstraction, precise information about the value of the integer variable $x$ can be replaced with non-deterministic guesses about the possible new values of the boolean variable $\text{neg}_x$. Note, for instance, that when $\text{neg}_x$ is true, and the value of $x$ is incremented, the new value of $x$ could be either positive or remain negative. This is reflected in a non-deterministic choice in the assignment of either true or false to $\text{neg}_x$. If, however, $x$ is known to be non-negative, it will remain so after the increment, and the value of $\text{neg}_x$ remains false. The condition $(x > 5)$ can clearly only be true when $x$ is non-negative, but beyond that we cannot guess. The Galois connection holds for these abstractions.
Dealing With False Negatives

The occurrence of false negatives as a result of a logically unsound abstraction is not as harmful as it might at first sight seem to be. By analyzing concretizations of counterexample executions it can often quickly be determined what piece of information was lost in the abstraction that permitted the generation of the false negative. The counterexample in effect proves to the user that the information that was assumed irrelevant is in fact relevant. Guided by the counterexample, the abstraction can now be refined to eliminate the false negatives one by one, until either valid counterexamples are generated, or a proof of correctness is obtained. It is generally much harder to accurately analyze a false positive result of a model checker, for instance, if selective restrictions were applied: caveat emptor.
Thorny Issues With Embedded C Code

The support in SPIN for embedded C code significantly extends the range of applications that can be verified, but it is also fraught with danger. Like a good set of knives, this extension can be powerful when used well, but also disastrous when used badly. As one simple example, it is readily possible to divide a floating pointer number by zero in an embedded C code fragment, or to dereference a nil-pointer. Since SPIN deliberately does not look inside embedded C code fragments, it cannot offer any help in diagnosing problems that are caused in this way. To SPIN, embedded C code fragments are trusted pieces of foreign code that define state transitions and become part of the model checker. In effect, the PROMELA extensions allow the user to redefine parts of the PROMELA language. It is ultimately the user's responsibility to make sure that these language extensions make sense.

We can place our trust in a model extraction tool such as MODEX to generate embedded C code that is (automatically) guarded with embedded assertions, but there are certainly still cases where also that protection can prove to be insufficient. Note, for instance, that it is readily possible within embedded C code fragments to unwittingly modify relevant state information that is beyond the purview of the model checker. External state information could, for instance, be read from external files, the contents of which can clearly not be tracked by the model checker. Hidden data could also be created and manipulated with calls to a memory allocator, or even by directly communicating with external processes through real network connections.

In cases where the model checker is set to work on a model with relevant state information that is not represented in the internal state vectors, false negatives and positives become possible. False negatives can again more easily be dealt with than false positives. Inspecting a counterexample can usually quickly reveal what state information was missed. False positives are also here the more dangerous flaw of an extended SPIN model. It will often be possible to incorporate hidden state information explicitly in a PROMELA model. Calls to a memory allocator such as malloc, for instance, can be replaced with calls to a specially constructed PROMELA model of the allocator, with all state information explicitly represented in the model. Similarly, information read from files or from network connections can be replaced with information retrieved from internal PROMELA processes, again making sure that all relevant state information becomes an explicit part of the verification model.

There can also be delicate issues in the framework we have sketched for model extraction from ANSI C source code. While it is true that most of the control-flow structures of a C program can be reproduced faithfully in a PROMELA verification model, there are some notable exceptions. The invocation of a function via a function pointer in C, for instance, could be preserved within an embedded C code fragment in PROMELA, but it would be very hard to intercept such calls and turn them into PROMELA process instantiations. In this case, too, we have to accept that there are limits to our verification technology. We can occasionally move the limits, but as these examples show, we cannot altogether remove them. Although much of the verification process can be automated, some barriers remain that can only be scaled with the help of human skill and judgement.
The Model Extraction Process

Using MODEX and SPIN, we can now approach software verification problems with the following general methodology.

- The first step is to decide what precisely the critical correctness properties of the application are. The properties of special interest are those that are non-computational in nature. Model checkers are especially strong in verifying concurrency-related problems.

- Next, we identify those parts of the system that contribute most critically to the behavior of primary interest. The effort here is again to find the smallest sufficient portion of the system to prove that the properties of interest are satisfied.

- The first two decisions can now guide us in the construction of an abstraction table that suppresses irrelevant detail and highlights the important aspects of the system. In many cases, no special user decisions will be needed and we can rely on the model extractor to use appropriate default translations. A model extractor like MODEX can also guide the user in the construction of the abstraction tables to make sure that no cases are missed.

- Verification can now begin. Inevitably, there will be things that need adjusting: mistranslations, or missed cases. The attempt itself to perform verification helps to identify these cases. If the model with its embedded C code is incomplete, for instance, either SPIN or the C compiler will reject it, in both cases with detailed explanations of the underlying reasons.

- Once we have a working verifier, we can start seeing counterexamples. Again, there will be a learning cycle, where false negatives will need to be weeded out and the abstraction tables adjusted based on everything that is learned in this phase.

- Eventually, either we find a valid counterexample, or a clean bill of health from the model checker. A valid counterexample is in this sense the desired outcome. A clean bill of health (i.e., the absence of counterexamples) should be treated with suspicion. Were the properties correctly formalized? Are they not vacuously true? Did the abstraction preserve enough information to prove or disprove them? A few experiments with properties that are known to be valid or invalid can be very illuminating in this phase, and can help build confidence in the accuracy of the results.

The process as it is sketched here still seems far removed from our ideal of developing a fully automated framework for thoroughly checking large and complex software packages. At the same time, though, it is encouraging that the approach we have described here offers an unprecedented level of thoroughness in software testing. As yet, there is no other method known that can verify distributed systems software at the level of accuracy that model extraction tools allow. The combination of model extraction and model checking enables us to eliminate the two main issues that hamper traditional testing by providing a reliable mechanism for both controllability and observability of all the essential elements of a distributed system.

To close the gap between the current user-driven methodology and a fully automated framework still requires some work to be done. Given the importance of this problem, and the number of people that are focusing on it today, we can be fairly confident that this gap can successfully be closed in the not too distant future.

[ Team LiB ]
The Halting Problem Revisited

In the days when C was still just a letter in the alphabet, and C++ a typo, it was already well established that it would be folly to search for a computer program that could decide mechanically if some arbitrary other computer program had an arbitrary given property. Turing's formal proof for the unsolvability of the halting problem was illustrated in 1965 by Strachey with the following basic argument. Suppose we had a program mc(P) that could decide in bounded time if some other program P would eventually terminate (i.e., halt); we could then write a new program nmc(P) that again inspects some other program P (e.g., after reading it), and uses mc(P) in the background. We now write nmc(P) in such a way that it terminates if P does not terminate, and vice-versa. All is well until we decide to run nmc(nmc) to see if nmc itself is guaranteed to terminate. After all, nmc is just another program, so this would be fair game.

Strachey's construction is similar to Bertrand Russell's famous class paradox, which makes it somewhat dubious to use as a basis for a logical argument. In fairness, Strachey's construction does not really prove the unsolvability of the halting problem, but it does prove that it is in general impossible to write a program that can establish arbitrary properties of itself. This, of course, does not mean that no programs could be written that can establish specific properties of themselves. A word-count program, for instance, can trivially determine its own length, and a C-compiler can confirm its own syntactic correctness, and even recompile itself.

Clearly we cannot write a program that could ever prove its own logical correctness. Note, for instance, that such a program could easily report its own correctness erroneously.

So far, this debate about arbitrary programs and arbitrary properties is purely academic, as it has been for pretty much the last 100 years. Curiously, though, the extensions to SPIN with embedded C code have made it possible to actually write a very real version of Strachey's construction. First, we write a little script that returns true if SPIN determines that a given model has at least one invalid end state, and false if it does not.

```
#!/bin/sh
### filename: halts

echo -n "testing $1: "

spin -a $1 # generate model
cc -DSAFETY -o pan pan.c # compile it
./pan | grep "errors: 0" # run it and grep stats
if $? # test exit status of grep
   echo "halts"
else
   echo "does not halt"
fi
```

We can try this on some little examples to make sure that it does the right thing. For instance, if we apply our script to the hello world example from Chapter 2, we get reassuringly:

```
$ ./halts hello.pml
halts
```

If we add a blocking statement to this model

```
active proctype main()
{
```

We can try to invoke this program in a c_expr statement with SPIN version 4, in the devious manner that was envisioned by Strachey.

```
:init { /* filename: strachey */
do
:: c_expr { system("halts strachey") } /* loop */
:: else -> break
od;
false /* block the execution */
}
```

What would happen if we now execute

```
$ ./halts strachey
```

....

The halts program ends up going into an infinite descent. Each time the verifier gets to the point where it needs to establish the executability of the c_expr, it needs to invoke the halts script once more and restart itself. The behavior of the model is defined in terms of itself, which puts it outside the scope of systems that can be verified with finitary methods. It would be hard to maintain that the infinite recursion is caused by the method that we used to implement the halts script. Note that if the halts script only needed to read the program before rendering its verdict, and did not need to execute it, the same infinite descent would still occur.

Curiously, the fact that the halts program loops on some inputs could in principle be detected by a higher-level program. But, as soon as we extend our framework again to give that new program the capability to reason about itself, we inevitably recreate the problem.

The example aptly illustrates that by allowing embedded C code inside SPIN models the modeling language becomes Turing complete, and we lose formal decidability. As yet another corollary of Kurt Gödel's famous incompleteness theorem: any system that is expressive enough to describe itself cannot be powerful enough to prove every true property within its domain.
Bibliographic Notes

Alan Turing's seminal paper on computable and uncomputable functions appeared in 1936, Turing [1936]. Christopher Strachey's elegant construction to illustrate the unsolvability of the halting problem first appeared in Strachey [1965]. In this very short note, Strachey refers to an informal conversation he had with Turing many years earlier about a different version of the proof.

The class paradox was first described in Russell [1903]. A fascinating glimpse of the correspondence between Russell and Frege about the discovery of this paradox in 1902 can be found in Heijenoort [2000]. Gödel's original paper is Gödel [1931].

General references to abstraction techniques can be found in the Bibliographic Notes to Chapter 5. Here we focus more on abstraction techniques that are used specifically for application in model extraction and model checking.

Data type abstractions can in some cases be computed mechanically for restricted types of statements and conditions, for instance, when operations are restricted to Presburger arithmetic. In these cases, one can use a mechanized decision procedure for the necessary computations (see, for instance, Levitt [1998]). A description of an automated tool for computing program or model slices based on selective data hiding can be found in Dams, Hesse, and Holzmann [2002].

In the literature, logical completeness is often defined only for abstraction methods, not for abstract models as we have done in this chapter. For a more standard discussion of soundness and completeness, see, for instance, Kesten, Pnueli, and Vardi [2001].

An excellent overview of general program slicing techniques can be found in Tip [1995].

The first attempts to extract verification models mechanically from implementation level code targeted the conversion of Java source code into PROMELA models. Among the first to pursue this, starting in late 1997, were Klaus Havelund from the NASA Ames Research Center, and Matt Dwyer and John Hatcliff from Kansas State University, as described in Havelund and Pressburger [2000], Brat, Havelund, Park, and Visser [2000], and Corbett, Dwyer, Hatcliff, et al. [2000].

The work at Ames led to the Pathfinder verification tool. The first version of this tool, written by Havelund, converted Java to PROMELA, using a one-to-one mapping. The current version, called Java Pathfinder-2, was written at Ames by Willem Visser as a stand-alone model checker, that uses an instrumented virtual machine to perform the verification.

The work at Kansas State on the Bandera tool suite targets the conversion from Java to PROMELA, and it includes direct support for data type abstraction and program slicing. The Bandera tool supports a number of other model checking tools as alternative verifiers, in addition to the SPIN tool.

The work at Bell Labs, starting in 1998, was the first attempt to convert ANSI C source code into abstract PROMELA verification models. It is described in, for instance, Holzmann and Smith [1999,2000,2002], and Holzmann [2000]. The code for the model extractor MODEX and for the extended version of SPIN is generally available today (see Appendix D). A more detailed description of the use of this tool, and the recommended way to develop a test harness definition, can be found in the online user guide for MODEX.

A related attempt to systematically extract abstract verification models from sequential C source code is pursued at Microsoft Research in the SLAM project, see Ball, Majumdar, Millstein, and Rajamani [2001]. The Bebop tool being developed in this project is based on the systematic application of predicate and data type abstractions.

The problem of detecting whether or not a property is vacuously satisfied was dealt with in the FeaVer system by implementing an automated check on the number of states that was reached in the never claim automata, see Holzmann and Smith [2000,2002]. A high fraction of unreachable states was found to correlate well with vacuously true properties. A more thorough method of vacuity checking is described in Kupferman and Vardi [1999].
Chapter 11. Using SPIN

"The difference between theory and practice is a lot bigger in practice than in theory."

—(Peter van der Linden, Expert C Programming, p. 134)

Although SPIN verifications are often performed most conveniently with the help of the graphical interface XSPIN, we will postpone a discussion of that tool for one more chapter and concentrate here on a bare bones use of SPIN itself. It can be very useful to know how to run short verification jobs manually through SPIN's command line interface, especially when trying to troubleshoot unexpected results.

The number of industrial applications of SPIN is steadily increasing. The core intended use of the tool, though, has always been to support both research and teaching of formal verification. One clear advantage of this primary focus is that the sources to SPIN remain freely available, also for commercial use.[1] The large number of users of the tool mean that any flaws that occasionally slip into the software are typically reported and fixed much more rapidly than would be possible for a commercial tool. A possible disadvantage is that the tool continues to evolve, which means that whatever version of the software you happen to be using, there is likely to be a more recent and better version available by the time you figure out how to use it. The basic use of the tool, though, does not change much from version to version, and it is this basic use that we will discuss in this chapter.

[1] Downloading instructions for SPIN can be found in Appendix D (p. 579).
SPIN Structure

The basic structure of SPIN is illustrated in Figure 11.1. The workflow starts with the specification of a high-level verification model of a concurrent system, or distributed algorithm, optionally using SPIN’s graphical front-end XSPIN. After fixing syntax errors, interactive simulation is performed until the user gains the basic confidence that the model has the intended properties. Optionally, a PROMELA correctness claim can be generated from a logic formula specified in linear temporal logic (LTL). Then, in the third main step, SPIN is used to generate an optimized on-the-fly verification program from the high-level specification. This verification program is compiled, with possible compile-time choices for the types of reduction algorithms that are to be used, and it is then executed to perform the verification itself. If any counterexamples to the correctness claims are detected, these can be fed back into the SPIN simulator. The simulation trail can then be inspected in detail to determine the cause of the correctness violation. [2]

[2] When embedded C code is used, the trail can only be reproduced by the verifier itself. See Chapter 17 for details.

Figure 11.1. The Structure of SPIN

In the remainder of this chapter we give some more detailed guidelines of how each of the main steps of specification, simulation, and verification can be performed.
A verification is often performed in an iterative process with increasingly detailed models. Each new model can be verified under different types of assumptions about the environment and for different types of correctness properties. If a property is not valid under a given set of assumptions, SPIN can produce a counterexample that shows explicitly how the property may be violated. The model can then be modified to prevent the property violation.

Once a property has been shown to hold, it is often possible to then reduce the complexity of that model by using the now trusted property as a simplifying assumption. The simpler model may then be used to prove other properties.

A more detailed sequence of steps that the (human) verifier can take in tackling a systems verification problem is as follows. We will assume that an initial verification model, saved in a file called model, has been built, including an initial formalization of all relevant correctness properties.

1. The first step is to perform a sanity check of the PROMELA code by executing the command:\[3\]

\$ spin -A model # perform thorough syntax check

The output from SPIN will include warnings about syntax errors, possibly dubious constructs that were used, as well as suggestions on possible improvements of the model. A second, more basic check of the model can be performed by attempting to generate the source code for a verifier from the model with the command:

\$ spin -a model # generate verifier

2. Once the first sanity checks are completed, and any flaws that were found have been repaired, a good insight into the behavior that is captured can be obtained with a series of either random or interactive simulation runs. If enough information can be gleaned from just the execution of print statements that are contained within the model, it may suffice to say simply:

\$ spin model # non-verbose simulation

However, especially for the first few runs, or when it is known that the simulation could continue ad infinitum, it is wise to add a more verbose output option, and to limit the maximum number of steps that may be executed, for instance, by executing the command:

\$ spin -p -u200 model # more verbose simulation

With these parameters every single step that is executed will produce at least some visible output. Also, the simulation will reliably stop after at most 200 steps were made, protecting against a runaway execution.
Simulation

We will now take a closer look at the main options for performing random, interactive, and guided simulations with SPIN.
Random Simulation

Given a model in PROMELA, say, stored in a file called model, the easiest mode of operation is to perform a random simulation. For instance,

```bash
$ spin -p model
```

tells SPIN to perform a random simulation while printing the process moves selected for execution at each step. If invoked without any options, SPIN prints no output other than what is explicitly produced by the model itself with print statements. Sometimes, simulation runs can go on indefinitely, and the output can quickly become overwhelming. One simple way of controlling the flow of output would be to pipe the output into a UNIX paging tool, for instance

```bash
$ spin -p model | more
```

This does not work on all PCs though. We can restrict the output to the first N steps by using the -uN option. Similarly, it is also possible to skip over an initial sequence of N steps with the -jN option. The two options can be used in combination, for instance, to see only the detailed output for one hundred execution steps starting at the 100th statement execution; one would say:

```bash
$ spin -p -j100 -u200 model     # print steps 100 to 200
```

A recommended way to make this work on a PC is to install the (free) cygwin toolset from [www.cygwin.com](http://www.cygwin.com), which approximates a very usable UNIX environment on Windows PCs.

```bash
$ spin -p -j100 -u200 model     # print steps 100 to 200
```

This type of simulation is random, which means that every new simulation run may produce a different type of execution. By default, the current time is used to seed the random number generator that SPIN uses in random simulation mode. To fix a user-defined seed value instead, and to make the simulation run completely reproducible, we can say, for instance

```bash
$ spin -p -j100 -u200 -n123 model     # fix seed
```

which initializes the random number generator with a user-defined seed of 123 in this case.

A range of options exists to make the results of a simulation more verbose, for example, by adding printouts of local variables (add option -l), global variables (option -g), send statements (option -s), or receive statements (option -r).

Options can be combined in arbitrary order, as in:

```bash
$ spin -p -l -g -r -s -n1 -j10 -u20 model
```

which can look quite baffling at first, but quickly starts to make sense.
Interactive Simulation

It is not always desirable to have SPIN automatically resolve all non-deterministic choices in the model with calls on a random number generator. For these cases, there is an interactive simulation mode of SPIN that is selected through command-line option -i. For instance, when we type:

$ spin -i -p model

a menu with choices is offered each time that the execution can proceed in more than one way. For instance, for the leader election model from the standard SPIN distribution, we might see:[5]

[5] We have deleted line numbers and source file references from the output for layout purposes.

Everything typed by the user after SPIN starts executing in response to a Select request from the tool is indicated in bold. The user is asked to make a choice from one or more non-deterministic alternatives for execution by typing a number within the range that is indicated by the Select request. In most cases, if there is only one choice, SPIN will immediately select that option without asking the user for guidance, but this is not always the case, as illustrated by the first query that the tool issues in the preceding example. The simulation can be stopped at any point by typing the letter q (for 'quit') at a selection menu.

If initial steps in the execution are skipped with a -jN option, then SPIN will resolve the non-determinism for those steps internally with the random number generator, and yield control to the user at the desired point. Again, it is wise to fix a seed to SPIN's random number generator in this case to make sure that the intial part of the simulation run proceeds in a reproducible way. An upper limit, specified with option -uN, will stop the simulation after N steps have been executed.

Simulations, of course, are intended primarily for the debugging of a model. Only basic assertions are checked in this mode, but even if none of these assertions are violated in a large battery of random simulation runs, we cannot conclude that such violations are impossible. To do so requires verification.
Guided Simulation

SPIN can also be run in guided simulation mode. To do so, though, requires the existence of a specially encoded trail file to guide the search. These trail files are generated only in verification mode, when the verifier discovers a correctness violation. The execution sequence leading up to the error is stored in the trail file, allowing SPIN to replay the scenario in a guided simulation, with access to all user-defined options that were discussed earlier for random simulation. We will return to this option on page 258.
Verification

Perhaps the most important feature of SPIN is that it can generate optimized verifiers from a user-defined PROMELA model. SPIN does not attempt to verify properties of a model directly, with any generic built-in code. By generating a verifier that can be compiled and run separately a significant gain in performance can be realized.
Generating a Verifier

When done debugging, we can use SPIN option -a to produce the source code for a model specific verifier, for instance, as follows:

```
$ spin -a model
```

There are actually two different semantic models that may be used to generate the verifier at this point. The alternative semantic model is obtained with the command:

```
$ spin -a -m model
```

By default, send operations are considered to be unexecutable when the channel to which the message is sent is full. With option -m, this semantic changes into one where send operations are always executable, but messages sent to full channels are lost. The standard semantics of PROMELA correspond to the default model, where option -m is not used.

The verifier is generated as a C program that is stored in a number of files with a fixed set of names, all starting with the three-letter prefix pan. For instance, we may see this result:

```

$ spin -a leader
$ ls -l pan.*
-rw-r--r--   1 gerard user 2633 Aug 18 12:33 pan.b
-rw-r--r--   1 gerard user 147964 Aug 18 12:33 pan.c
-rw-r--r--   1 gerard user 9865 Aug 18 12:33 pan.h
-rw-r--r--   1 gerard user 13280 Aug 18 12:33 pan.m
-rw-r--r--   1 gerard user 18851 Aug 18 12:33 pan.t
$ 
```

The file named pan.h is a generic header file for the verifier that contains, for instance, the translated declarations of all global variables, all channels, and all process types. File pan.m defines the executability rules for all PROMELA statements used in the model, and the effect they have on the system state when successfully executed. File pan.b defines how the effect of each statement from pan.m can be undone when the direction of the depth-first search is reversed. File pan.t contains the transition matrix that encodes the labeled transition system for each process type. Finally, file pan.c contains the algorithms for the computation of the asynchronous and synchronous products of the labeled transition systems, and the state space maintenance and cycle detection algorithms, encoding optimized versions of either a depth-first or a breadth-first search.

[ Team LiB ]
Compiling the Verifier

The best performance of the SPIN-generated verifiers can be obtained if the physical limitations of the computer system that will be used to run the verifications are known. If it is known, for instance, how much physical (not virtual) memory the system has available, the verifier can take advantage of that. Initially, the verifier can simply be compiled for a straight exhaustive verification, which can also deliver the strongest possible verification result, provided that there is sufficient memory to complete the run. Compile as follows:

$ cc -o pan pan.c # compile for exhaustive search

The pan.c file includes all other files that are generated by SPIN, so the name of only this file needs to be provided to the compiler. If this compilation attempt fails, make sure that you have an ANSI compatible C compiler. Almost all C compilers today conform to this standard. In case of doubt, though, the generally available Gnu C compilers have the right properties. They are often available as gcc, rather than cc. The result of the compilation on UNIX systems will be an executable file called pan.

On a Windows PC system with the Microsoft Visual C++ compiler installed, the compilation would be done as follows:

$ cl pan.c

which if all is well also produces an executable verifier named pan.exe.

If a memory bound is known at the time of compilation, it should be compiled into the verifier so that any paging behavior can be avoided. If, for instance, the system is known to have no more than 512 Megabytes of physical RAM memory, the compiler-directive to add would be:

$ cc -DMEMLIM=512 -o pan pan.c

If the verifier runs out of memory before completing its task, the bound could be increased to see if this brings relief, but a better strategy is to try some of SPIN's memory compression options. For instance, a good first attempt could be to compile with the memory collapse option, which retains all the benefits of an exhaustive verification, but uses less memory:

$ cc -DCOLLAPSE -o pan pan.c # collapse compression

If that also fails, the recommended strategy is to use a series of bitstate verification runs to get a better impression of the complexity of the problem that is being tackled. Although the bitstate verification mode cannot guarantee exhaustive coverage, it is often very successful in identifying correctness violations.

$ cc -DBITSTATE -o pan pan.c # bitstate compression

Whichever type of compilation was selected, an executable version of the verifier should be created in a file called either pan (on UNIX systems) or pan.exe (on PCs), and we can proceed to the actual verification step.
Tuning a Verification Run

A few decisions can be made at this point that can improve the performance of the verifier. It is, for instance, useful, though not strictly required, if we can provide the verifier with an estimate of the likely number of reachable states, and the maximum number of unique steps that could be performed along any single non-cyclic execution path (defining the maximum depth of the execution tree). We will explain in the next few sections how those estimates can be provided. If no estimates are available, the verifier will use default settings that will be adequate in most cases. The feedback from the verifier after a first trial run usually provides enough clues to pick better values for these two parameters, if the defaults do not work well.

Next, we must choose whether we want the verifier to search for violations of safety properties (assertion violations, deadlocks, etc.) or for liveness properties (e.g., to show the absence of non-progress cycles or acceptance cycles). The two types of searches cannot be combined.

A search for safety properties is the default. This default is changed into a search for acceptance cycles if run-time option `-a` is used. To perform a search for non-progress cycles, we have to compile the pan.c source with the compile-time directive `-DNP`, and use run-time option `-l`, instead of `-a`. We will return to some of these choices on page 257.
The Number of Reachable States

The verifier stores all reachable states in a lookup table. In exhaustive search mode, that table is a conventional hash table, with a default size of $2^{18}$ slots. This state storage method works optimally if the table has at least as many slots as there are reachable states that will have to be stored in it, although nothing disastrous will happen if there are less or more states than slots in the lookup table. Strictly speaking, if the table has too many slots, the verifier wastes memory. If the table has too few slots, the verifier wastes CPU cycles. In neither case is the correctness of the verification process itself in peril.

The built-in default for the size of the hash table can be changed with run-time option -wN. For instance,

```
$ ./pan -w23
```

changes the size of the lookup table in exhaustive search mode from $2^{18}$ to $2^{23}$ slots.

The hash table lookup idea works basically the same when the verifier is compiled for bitstate verification, instead of for the default exhaustive search. For a bitstate run, the size of the hash table in effect equals the number of bits in the entire memory arena that is available to the verifier. If the verifier is compiled for bitstate verification, the default size of the hash array is $2^{22}$ bits, that is, $219$ bytes. We can override the built-in default by specifying, for instance,

```
$ ./pan -w28
```

to use a hash array of $2^{22}$ bits or $225$ bytes. The optimal value to be used depends primarily on the amount of physical memory that is available to run the verification. For instance, use -w23 if you expect 8 million reachable states and have access to at least 1 Megabyte of memory ($2^{20}$ bytes). A bitstate run with too small of a setting for the hash array will get less coverage than possible, but it will also run faster. Sometimes increased speed is desired, and sometimes greater coverage.

One way to exploit the greater speed obtained with the small hash arrays is, for instance, to apply an iterative refinement method. If at least 64 Megabytes of physical memory are available, such an iterative search method could be performed as follows, assuming a UNIX system running the standard Bourne shell:

```
$ spin -a model
$ cc -DBITSTATE -DMEMLIM=80 -o pan pan.c
$ for i in 20 21 22 23 24 25 26 27 28 29
do
   ./pan -w$i
   if [ -f model.trail ]
      then exit
   fi
done
```

The search starts with a hash array of just $2^{20}$ bits (128 Kbytes), which should not take more than a fraction of a second on most systems. If an error is found, the search stops at this point. If no error is found, the hash array doubles in size and the search is repeated. This continues until either an error is found or the maximal amount of memory has been used for the hash array. In this case, that would be with a hash array of $2^{29}$ bits (64 Megabytes). The verifier source is compiled with a limit of 80 Megabytes in this case, to allow some room for other data structures.
Search Depth

By default, the verifiers generated by SPIN have a search depth restriction of 10,000 steps. If this isn't enough, the search will truncate at 9,999 steps (watch for this telltale number in the printout at the end of a run). A different search depth of \( N \) steps can be defined by using run-time option \(-mN\), for instance, by typing

$$ \text{./pan -m1000000} $$

to increase the maximum search depth to 1,000,000 steps. A deeper search depth requires more memory for the search; memory that cannot be used to store reachable states, so it is best not to overestimate here. If this limit is also exceeded, it is probably good to take some time to consider if the model defines finite behavior. Check, for instance, if attempts are made to create an unbounded number of processes, or to increment integer variables without bound. If the model is finite, increase the search depth at least as far as is required to avoid truncation of the search.

In the rare case that there is not enough memory to allocate a search stack for very deep searches, an alternative is to use SPIN's stack-cycling algorithm that arranges for the verifier to swap parts of the search stack to disk during a verification run, retaining only a small portion in memory. Such a search can be set up and executed, for instance, as follows:

$ spin -a model 
$ cc -DSC -o pan pan.c # use stack-cycling 
$ ./pan -m100000

In this case, the value specified with the \(-m\) option defines the size of the search stack that will reside in memory. There is no preset maximum search depth in this mode; the search can go arbitrarily deep, or at least it will proceed until also the diskspace that is available to store the temporary stack files is exhausted.

If a particularly nasty error is found that takes a relatively large number of steps to hit, you can try to find a shorter error trail by forcing a shorter depth-limit with the \(-m\) parameter. If the error disappears with a lower depth-limit, increase it in steps until it reappears.

Another, and often more reliable, way to find the shortest possible error sequence is to compile and run the verifier for iterative depth adjustment. For instance, if we already know that there exists an error sequence of 1,000 steps, we can try to find a shorter equivalent, as follows:

$ spin -a model 
$ cc -DREACH -o pan pan.c 
$ ./pan -i -m1000 # iteratively find shortest error

Be warned, though, that the use of \(-DREACH\) can cause an increase in run time and does not work for bitstate searches, that is, it cannot be combined with \(-DBITSTATE\).

Finally, if the property of interest is a safety property (i.e., it does not require a search for cyclic executions), we can consider compiling the verifier for a breadth-first, instead of the standard depth-first, search:

$ cc -DBFS -o pan pan.c
Cycle Detection

The most important decision to be made in setting up a verification run is to decide if we want to perform a check for safety or for liveness properties. There are optimized algorithms in the verifier for both types of verification, but only one type of search can be performed at a time. The three main types of search, with the corresponding compilation modes, are as follows:

$ spin -a model
$ cc -DSAFETY -o pan pan.c # compilation for safety
$ ./pan                  # find safety violations
$ cc -o pan pan.c        # default compilation
$ ./pan -a               # find acceptance cycles
$ cc -DNP -o pan pan.c   # non-progress cycle detection
$ ./pan -l               # find non-progress cycles

By default, that is in the absence of option -l and -a, only safety properties are checked: assertion violations, absence of unreachable code, absence of race conditions, etc. The use of the directive -DSAFETY is optional when a search for safety properties is performed. But, when the directive is used, the search for safety violations can be performed somewhat more efficiently.

If accept labels are present in the model, for instance, as part of a never claim, then a complete verification will require the use of the -a option. Typically, when a never claim is generated from an LTL formula, it will contain accept labels.

Adding run-time option -f restricts a search for liveness properties further by enforcing a weak fairness constraint:

pan -f -l  # search for fair non-progress cycles
pan -f -a  # search for fair acceptance cycles

With this constraint, a non-progress cycle or an acceptance cycle is only reported if every running process either executes an infinite number of steps or is blocked at an unexecutable statement at least once in the execution cycle. Adding the fairness constraint multiplies the time requirements of a verification by a factor that is linear in the number of running processes.

By default, the verifier will always report every statement that is found to be unreachable in the verification model. This reachability report can be suppressed with run-time option -n, as, for instance, in:

$ ./pan -n -f -a

The order in which the options such as these are listed is always irrelevant.
Inspecting Error Traces

If the verification run reports an error, SPIN dumps an error trail into a file named model.trail, where model is the name of the PROMELA specification. To inspect the trail, and to determine the cause of the error, SPIN’s guided simulation option can be used (assuming that the model does not contain embedded C code fragments, cf. p. 495). The basic use is the command

$ spin -t -p model

with as many extra or different options as are needed to pin down the error. For instance,

$ spin -t -r -s -l -g model

The verifier normally stops when a first violation has been found. If the first violation is not particularly interesting, run-time option -cN can be used to identify others. For instance,

$ ./pan -c3

ignores the first two violations and reports only the third one, assuming of course that at least three errors can be found.

To eliminate entire classes of errors, two special purpose options may be useful. A search with

$ ./pan -A

will ignore all violations of basic assertion statements in the model, and a search with

$ ./pan -E

will ignore all invalid end-state errors. For example, to search only acceptance cycles, the search could be initiated as:

$ ./pan -a -A -E

To merely count the number of all violations, without generating error trails, use

$ ./pan -c0
**Internal State Numbers**

Internally, the verifiers produced by SPIN deal with a formalization of a PROMELA model in terms of finite automata. SPIN therefore assigns state and transition numbers to all control flow points and statements in the model. The automata state numbers are listed in all the relevant outputs to make it unambiguous (source line references unfortunately do not always have that property). To reveal the internal state assignments, run-time option -d can be used. For instance,

```
$ ./pan -d
```

prints a table with all internal state and transition assignments used by the verifier for each distinct proctype in the model. The output does not clearly show merged transition sequences. To obtain that output it is best to disable the transition merging algorithm that is used in SPIN. To do so, proceed as follows:

```
$ spin -o3 model
$ cc -o pan pan.c
$ ./pan -d
```

To see the unoptimized versions of the internal state assignments, every repetition of the -d argument will arrange for an earlier version of the internal state tables to be printed, up to the original version that is exported by the SPIN parser. Try, for instance, the following command for your favorite model:

```
$ ./pan -d -d -d
```

and compare it with the output that is obtained with a single -d argument.
Special Cases

We conclude this chapter with a discussion of some special cases that may arise in the verification of PROMELA models with SPIN. In special circumstances, the user may, for instance, want to disable the partial order reduction algorithm. Alternatively, the user may want to spend some extra time to boost the performance of the partial order reduction by adding some additional declarations that SPIN can exploit. Finally, in most serious applications of automated verification tools, the user will sooner or later run into complexity bottlenecks. Although it is not possible to say specifically how complexity can be reduced in each specific case, it is possible to make some general recommendations.
Disabling Partial Order Reduction

Partial order reduction is enabled by default in the SPIN generated verifiers. In special cases, for instance, when the verifier warns the user that constructions are used that are not compatible with the partial order reduction strategy, the reduction method can be disabled by compiling the verifier's source code with an extra directive:

```bash
$ spin -a model
$ cc -DNOREDUCE -o pan pan.c # disable p.o. reduction
```
Boosting Performance

The performance of the default partial order reduction algorithm can also be boosted substantially if the verifier can be provided with some extra information about possible and impossible access patterns of processes to message channels. For this purpose, there are two special types of assertions in PROMELA that allow one to assert that specific channels are used exclusively by specific processes. For example, the channel assertions

\[
\begin{align*}
\text{xr } q_1; \\
\text{xst } q_2;
\end{align*}
\]

claim that the process that executes them is the only process that will receive messages from channel \(q_1\), and the only process that will send messages to channel \(q_2\).

If an exclusive usage assertion turns out to be invalid, the verifier will always be able to detect this and report it as a violation of an implicit correctness requirement.

Note that every type of access to a message channel can introduce dependencies that may affect the exclusive usage assertions. If, for instance, a process uses the \(\text{len}(q\text{name})\) function to check the number of messages stored in a channel named \(q\text{name}\), this counts as a read access to \(q\text{name}\), which can invalidate an exclusive access pattern.

There are two special operators that can be used to poll the size of a channel in a way that is always compatible with the reduction strategy:

- \(\text{nfull}(q\text{name})\)

  returns true if channel \(q\text{name}\) is not full, and

- \(\text{nempty}(q\text{name})\)

  returns true if channel \(q\text{name}\) contains at least one message. The SPIN parser will reject attempts to bypass the protection offered by these primitives with expressions like

  \[
  \text{!full}(q\text{name}), \\
  \text{!empty}(q\text{name}), \\
  \text{!nfull}(q\text{name}), \text{or} \\
  \text{!nempty}(q\text{name}).
  \]

In special cases, the user may want to claim that the particular type of access to message channels that is specified in \(\text{xr}\) and \(\text{xst}\) assertions need not be checked. The checks can then be suppressed by compiling the verifier with the extra directive \(-\text{DXUSAFe}\), for instance, as in:

\[
\text{\$ cc -DXUSAFe -o pan pan.c}
\]
Separate Compilation

Often, a verification model is checked for a range of logic properties, and not just a single property. If properties are specified in LTL, or with the Timeline Editor, we can build a library of properties, each of which must be checked against the model. The easiest way to do this is to first generate all property automata from the formulae, or from the visual time line specifications, and store each one in a separately named file. Next we can set up a verification script that invokes SPIN on the basic model, but for each run picking up a different property automaton file, for instance with SPIN's run-time option -N.

If the main verification model is stored in a file called model.pml and the property automata are all stored in file names with the three-letter extension .prp, we can build a minimal verification script, using the UNIX Bourne shell, for instance, as follows:

```
#!/bin/sh
for i in *.prp
do
    echo "property: $i"
    if spin -N $i -a model.pml
       then  
    else   echo "parsing error"
       exit 1
    fi
    if cc -o pan pan.c
       then  
    else   echo "compilation error"
       exit 1
    fi
    ./pan -a
od
exit 0
```

In most cases, the time that is required to parse the model, to generate the verifier source text and to compile the verifier, is small compared to the time that is required to run the actual verification. But, this is not always the case.

As the model text becomes larger, the time that is needed to compile the verifier source text will also increase. If the compilation process starts to take a noticeable amount of time, and there is a substantial library of properties that need to be checked, we may want to optimize this process.

We can assume that if the compilation time starts to become noticeable, this is typically do to the large size of the basic verification model itself, not the size of the property. In SPIN model checking it would be very rare for a property automaton to exceed a size of perhaps ten to twenty control states. A system model, though, can easily produce an automaton description that spans many thousands of process states. Compiling the automata descriptions for the main verification model, then, can sometimes require significantly more time than compiling the source code that is associated with the implementation of a property automaton.

SPIN supports a method to generate the source code for the model and for the property separately, so that these two separate parts of the source code can also be compiled separately. The idea is that we only need to generate and compile the source code for the main system model once (the slow part), and we can repeat the generation and compilation of the much smaller source code fragments for the property automata separately.

If we revise the verification script from our first example to exploit this separate compilation option, it would look like this:

```
#!/bin/sh
if spin -S1 model.pml # model, without properties
   then  
if cc -c pan_s.c # compile main part once
   then  
for i in *.prp
do
    echo "property: $i"
    if spin -N $i -S2 model.pml
       then  
    else   echo "parsing error in property"
       exit 1
    fi
    if cc -c pan_t.c                 # property code
       then  
    else   echo "compilation error in property"
       exit 1
    fi
    if cc -o pan pan_s.o pan_t.o     # link
       then  
    else   echo "link error"
       exit 1
    fi
    ./pan -a
od
exit 0
```

To get an idea of how much time the separate compilation strategy can save us, assume that we have a library of one hundred properties. If the compilation of the complete model code takes seventy-two seconds, and compilation of just the property related code takes seven seconds, then the first verification script would take:

$ 100 \times 72 = 7,200 \text{ seconds} = 2 \text{ hours}$

The second verification script, using separate compilation, would take:

$72 + 100 \times 7 = 772 \text{ seconds} = 11 \text{ minutes, } 12 \text{ seconds}$

The time to run each verification would be the same in both scenarios.

In some cases, when the property automata refer to data that is external to the module that contains the property related source code, it can be necessary to add some code into the source file. This can be done via the addition at compile-time of so-called provisioning information, as follows:

```
$ cc -DPROV="extra.c" -c pan_t.c
$ cc -o pan pan_s.o pan_t.o
```

The provisioning information (such as declarations for external variables) is provided in a separate file that is prepared by the user. It can contain declarations for external variables, and also initialization for selected global variables.
Lowering Verification Complexity

If none of SPIN’s built-in features for managing the complexity of a verification run seem to be adequate, consider the following suggestions to lower the inherent complexity of the verification model itself:

- Make the model more general; more abstract. Remove everything from the model that is not directly related to the correctness property that you are trying to prove. Remove all redundant computations and redundant data. Use the output from SPIN option -A as a starting point.

- Avoid using variables with large value ranges, such as integer counters, clocks, or sequence numbers.

- Try to split channels that receive messages from multiple senders into separate channels, one for each source of messages. Similarly, try to split channels that are read by multiple processes into separate channels, one for each receiver. The interleaving of independent message streams in a single channel can be a huge source of avoidable complexity.

- Reduce the number of slots in asynchronous channels to as small a number as seems reasonable. See Chapter 5, p. 101, on the effect that channel sizes can have on search complexity.

- Group all local computations into atomic sequences, and wherever possible into d_step sequences.

- Avoid leaving scratch data around in local or global variables. The number of reachable system states can often be reduced by resetting local variables that are used only inside atomic or d_step sequences to zero at the end of those sequences.

There is a special keyword in the language that can be used to hide a scratch variable from the verifier completely. It is mentioned only in passing here, since the mechanism is easily misused. Nonetheless, if you declare a global variable, of arbitrary type, as in:

```plaintext
hidden byte var;
```

then the variable, named var here, is not considered part of the state descriptor. Clearly, values that are stored in hidden variables cannot be assumed to persist. A typical use could be to flush the contents of a channel, for instance, as follows:

```plaintext
   do
   :: nempty(q) -> q?var
   :: else -> break
   od
```

If the variable var were not hidden, each new value stored in it would cause the creation of a new global state. In this case this could needlessly increase the size of the reachable state space. Use with caution. An alternative method is to use the predefined hidden variable named _ (underscore). This write-only variable need not be declared and is always available to store scratch values. The last example can therefore also be written as:

```plaintext
   do
   :: q?_
   :: empty(q) -> break
   od
```
Chapter 12. Notes on XSPIN

"The ability to simplify means to eliminate the unnecessary so that the necessary may speak."

—(Hans Hofmann, 1880–1966)

XSPIN is the graphical interface to SPIN that for many users is the first introduction to the tool. It can be a considerable benefit, though, if the user is familiar with the basic operation of SPIN before switching to XSPIN, especially when more subtle design problems are encountered.

The interface operates independently from SPIN itself. It synthesizes and executes SPIN commands in the background, in response to user selections and button clicks. Nonetheless, this front-end tool supplies a significant added value by providing graphical displays of, for instance, message flows and time sequence diagrams. XSPIN also provides a clean overview of the many options in SPIN that are available for performing simulations and verifications.

To run XSPIN, you first of all need to be able to run SPIN itself, which means that you minimally will need access to an ANSI compatible C preprocessor and compiler. XSPIN is written in Tcl/Tk, so if you have a local installation of the Tcl/Tk toolset,[1] you can run it directly from its source. You do not need to install Tcl/Tk to run the tool, though. It is also available as a stand-alone binary executable that is available as part of the standard SPIN distribution (see Appendix D).


This chapter gives a brief overview of the main options that are available through XSPIN. The interface is intuitive enough that most questions can be answered by simply running the tool and by exploring its options and help menus interactively.
Starting a Session With XSPIN

Assuming all the software has been installed properly, XSPIN can be started on both UNIX systems and Windows PC systems from the shell command line with the name of a file containing a PROMELA specification as an argument, for instance, as follows:

$ xspin leader

On a Windows system the program can also be selected from the start menu, or by double-clicking the source file named xspin.tcl.

When XSPIN starts, it first checks that good versions of SPIN and Tcl/Tk are available. It prints the version numbers in a command-log window, and optionally opens and loads an initial PROMELA file.

Throughout the use of XSPIN, a log of all actions performed is maintained in a special command-log window that appears at the bottom of the XSPIN display. Syntax errors, unexpected events, time-consuming actions such as background compilations and verification runs, can be tracked in the log.

The main display of XSPIN is a text window that displays the file being used, just like a graphical text editor would do. The file name, if any, is shown in the title bar. The view in the text window can be changed in four different ways:

- With the scroll bar on the left-hand side of the text window.
- By typing a line number (followed by a <return>) in the box in the title bar marked Line#:.
- By typing a regular expression pattern (followed by a <return>) in the box marked Find:.
- By moving a three-button mouse with the middle mouse button down, or a two-button mouse with both buttons down.

Moving around in the text with the mouse buttons down (the last method above) is the most convenient, and it works in most of the text displays that are provided by XSPIN.

There are four other buttons in the title bar of the XSPIN display: File.., Edit.., Run.., and Help, as shown in Figure 12.1. We will discuss each of these separately in the following sections.

Figure 12.1. XSPIN Main Window
The File Menu

The file menu gives a choice of seven actions: New, UnSelect, ReOpen, Open, Save As, Save, and Quit.

New clears the contents of the main window, but does not reset the file name or affect any other parameter.

UnSelect removes any selection highlights that the user or a background program may have placed in the main window.

ReOpen reloads the contents of the current file in the main text window, discarding any changes made since the last save operation.

Open prompts the user with a standard file dialogue, listing all files in the current directory. Double-clicking any of the files will cause XSPIN to open it and place it in its text window. Of course, this only makes sense for PROMELA specifications. Double-clicking a directory name will cause the browse window to descend into that directory and display the files listed there. Double-clicking the up-arrow icon will cause the browse window to move up to the parent directory, and display the files listed there.

Save As.. provides a file browse dialogue, allowing the user to select a file name in which the current contents of the text window should be saved. During each session, XSPIN always maintains a private copy of the current contents of the text window in a file called pan_in to avoid unintentional changes in the original source of the PROMELA specification. The source file itself is only (re)written with an explicit Save command.

Quit terminates the session of XSPIN, removing any temporary files that were created during simulation or verification runs. No warning is issued if the file being edited was changed since the last time it was saved.
The Edit Menu

The edit menu contains the three standard entries for performing Cut, Copy, and Paste operations on selected text in the main window. Text can be selected as usual, by sweeping with the left mouse button down, or by double-clicking text strings. Cut, copy, and paste operations are also available with control-key combinations: control-X for cut, control-C for copy, and control-V for paste. Be careful though, there is no undo operation implemented in XSPIN.
The Help Menu

The help menu gives a quick online review of the main usage options of SPIN and XSPIN, and contains an explanation of the proper setting of the main parameters for verification and simulation runs. The menu also provide hints for reducing search complexity. The entries in this menu will be self-explanatory.
The Run Menu

The run menu has eight entries for performing syntax checks, property-based slicing, setting simulation or verification parameters, running simulations or verifications, and viewing the internal automata structures computed by SPIN. We discuss each of these menu choices next.
Syntax Check

XSPIN runs a syntax check by asking SPIN to execute the command:

$ spin -a -v pan_in

in the background, using its private file copy of the PROMELA text in the main window. Results, if any, are displayed in the standard command log window and in a separate popup window that can be closed again with a mouse-click on its Ok button. Wherever possible, error text is highlighted in the main XSPIN window for ease of reference.
Property-Based Slicing

To run the slicing algorithm, which also provides a thorough syntax check of the PROMELA source, XSPIN executes the following command:

```
$ spin -A pan_in
```

The slicing algorithm tries to locate all logical properties that are part of the model, for instance, as expressed in assertions and in a never claim, and it uses this information to identify those parts of the model that cannot possibly affect the correctness or incorrectness of those properties. In the absence of properties, the algorithm can still do useful things, by identifying portions of the model that are redundant no matter which properties are specified.

The results that are produced are displayed both in the command log window and in a separate popup window. Included in the output are also any warnings about potentially wasteful constructs, such as variables that were declared as integers but that assume only boolean values. If no redundancies can be found in the model, SPIN will report this as well, so this option is also generally useful as a somewhat more thorough check of the model.
Set Simulation Parameters

The simulation options panel allows the user to select the types of displays that will be generated during simulation runs. In the upper right-hand corner of the panel the choice between random, guided, and interactive simulation can be made. When XSPIN is used, random simulation is by default done with a predefined seed value of one. This seed value can be changed freely to obtain different types of runs, but once the seed value is fixed, all experiments are fully reproducible. If the entry box for the seed value is left blank, the current system time is used as a seed value, which of course does not guarantee reproducibility. The guided simulation option requires the presence of a file named pan.trail, which is normally produced in a verification run when SPIN finds a counterexample to a correctness property. The number of steps that should be skipped before the display of the sequence is initiated can be specified, the default value being zero.

Two further options are selectable in the right-hand side column of the simulation options panel. For send statements, the user has a choice of semantics. Either a send operation that targets a full message channel (queue) blocks, or can be defined to be non-blocking. If non-blocking, messages sent to a full channel are lost. Up to three channel numbers (queue numbers) can be specified in the three entry boxes at the bottom of the right-hand column. If channel numbers are entered, send and receive operations that target the corresponding channels will not be displayed in graphical MSC (message sequence chart) displays.

On the left-hand side of the panel four types of outputs can be requested. By default, only two of these will be selected. A most useful type of display is the MSC (message sequence chart) panel. Normally, the execution steps in this display are tagged with identifying numbers. By moving the mouse cursor over one of the steps, the source text will show and the main text window will scroll to the corresponding statement. Alternatively, the user can also choose to have the source text shown for each step in the display. For very long runs, the message sequence chart can be compacted somewhat by selecting the condensed spacing option.

Normally, the message sequence chart will display only send and receive actions, connecting matching pairs with arrows. The output from print statements can be added to a message sequence chart by starting any newline terminated string to be printed with the prefix "MSC:" followed by a space, for instance, as in:

```
printf("MSC: this will appear in the MSC\n");
```

The default background color for text boxes that are created in this manner is yellow. The color of the box can also be changed by starting the text string to be printed with a special two-character control sequence. For instance,

```
printf("MSC: ~W uses a white box\n");
printf("MSC: ~G uses a green box\n");
printf("MSC: ~R uses a red box\n");
printf("MSC: ~B uses a blue box\n");
```

The prefix MSC: and an optional two-character control codes for setting colors do not appear in the output itself.

As a special feature of print statements, if the statement

```
printf("MSC: BREAK\n");
```

causes XSPIN to suspend the simulation run temporarily, simulating a breakpoint in the run. The run can be restarted from the main simulation output panel.
(Re)Run Simulation

When the simulation parameters have been set once, they persist for the remainder of the session, or until the setting is changed. New simulation runs can now be initiated directly with these settings by selecting this menu option from the Run menu. The option is grayed out, and remains unselectable, until the simulation parameters panel has been displayed at least once.
Set Verification Parameters

The verification parameters panel gives visual control over most of the options that SPIN provides for performing automated verifications. The initial settings of all parameters are chosen in such a way that they provide a reasonable starting point for most applications. A first verification run, therefore, can in most cases safely be performed by hitting the Run button in the lower right corner of the panel, without altering the default settings.

When a verification run completes, XSPIN attempts to provide hints about ways to proceed, based on the results obtained. No hints are provided when a clean run is performed, that is, a complete exhaustive search that did not reveal any errors. The default hint in cases like these would be to consider whether or not the properties that were proven are the correct ones, and whether or not other properties still remain to be proven.

The default settings define a search for safety properties only. Proving liveness properties (properties of infinite behaviors as manifested by execution cycles) requires a separate verification run with the appropriate options selected in the Correctness Properties section of the verification parameters panel, shown in Figure 12.5.

Figure 12.5. Basic Verification Options

![Basic Verification Options]

Note that if the PROMELA specification contains syntax errors, these errors will show up in the XSPIN log when the Run button is selected. The run itself is canceled in that case. It is useful to keep an eye on such error reports, and to be aware of the types of things that XSPIN or SPIN perform in the background.

Three main search modes are selectable in the upper right-hand corner of the panel: exhaustive verification, bitstate approximation, or hash-compact. Some of the more rarely used settings for performing verifications are delegated to a special Advanced Options panel, shown in Figure 12.6, that can be selected in the lower right-hand corner of the basic verification options panel. Especially in the beginning, this panel can safely be ignored.

Figure 12.6. Advanced Verification Options

![Advanced Verification Options]
(Re)Run Verification

When the verification parameters panel has been displayed at least once, this menu entry becomes selectable. It will initiate a new verification run, preserving all parameter settings that were chosen earlier. This can be useful, for instance, when small changes in the PROMELA model are made to remedy problems uncovered in earlier verification runs.
LTL Property Manager

Selecting this entry from the Run menu brings up a panel for entering an LTL formula to be used in a verification attempt, shown in Figure 12.7. By clicking on the button labeled Generate, or by typing a return character in the formula entry box, the formula is converted into a never claim. Both this claim and the main PROMELA specification are now submitted to SPIN when the Run Verification button is selected.

Figure 12.7. The LTL Property Manager

Templates of standard forms of LTL formulae can be loaded into the LTL property window with the Load option in the upper right corner of the display. Four templates are predefined for invariance properties, response properties, precedence properties, and objective properties. They have the following general form:

\[
[] p \quad \# \text{invariance} \\
p -> <> q \quad \# \text{response} \\
p -> (q U r) \quad \# \text{precedence} \\
p -> <> (q || r) \quad \# \text{objective}
\]

Each of these generic types of properties can (and will generally have to) be prefixed by temporal operators such as [], <>[], []<>[], or <>[]. The property type named objective can be read to mean that p (a state property) is an enabling condition that determines when the requirement becomes applicable. Once enabled, the truth of state property q can signify the fulfillment of the requirement, while the truth of r can be treated as a discharging condition that voids the requirement.

LTL properties consist of temporal and logical operators and user-defined propositional symbols. For propositional symbols, names that start with a lowercase letter are used. It is not customary to use blank spaces.

Boolean operators can also be used inside LTL formulae, using standard PROMELA syntax:

- `&&` logical and
- `!` logical negation
- `||` logical or

Arithmetic operators are not allowed within an LTL formula, but can be used within the macro definitions of the propositional symbols.

Two shorthands are available for defining logical implication and equivalence.

- `->` logical implication
- `<->` logical equivalence

The formula (p -> q) is short for (!p || q) and (p <-> q) is short for (p -> q) && (q -> p).

Recall that logical implication and logical equivalence are boolean and not temporal operators, and that therefore no passage of time is implied by the use of a subformula such as (p -> q). (On this point, see also the section on Using Temporal Logic in Chapter 6.)

The names of operands in an LTL formula must be alphanumeric names, always beginning with a lowercase letter. The preferred style is to use only single-character names, such as p, q, and r. Prudence, further, dictates that the right-hand side of each of the corresponding symbol definitions is enclosed in round braces, to protect against unintended effects of operator precedence rules.
The Automaton View Option

The automaton view option, finally, allows for the selection of one of the proctypes that are part of the PROMELA specification, so that it can be displayed in automaton form.

When this option is selected, XSPIN first generates and compiles an executable verifier. It then uses the output from PAN's run-time option -d to synthesize the automaton view. It is highly recommended to have a copy of the graph layout tool dot installed on the system.[2] If it is present, XSPIN will use it to compute the layout for the automaton graph, as illustrated in Figure 12.8. If absent, a cruder approximation of the layout will be used.


**Figure 12.8. The Automata View**

The view in Figure 12.8 shows all states in proctype node from the leader election protocol example. For simplicity, we have turned off the display of the statement labels in this display. They can be restored by selecting the button labeled Add Labels at the bottom of the display.

Each state in the graph by default shows the line number in the source file that correspond to that state. Moving the cursor over a state causes the corresponding line to be highlighted in the main text window, and changes the line number text for the internally assigned state number. The display of the line number is restored when the cursor is moved away from the state. The graphical display that is generated is for information only; it cannot be edited.
In Summary

XSPIN synthesizes commands that are issued to the SPIN model checker based on user selections and preferences. For each run performed by SPIN in the background, XSPIN also intercepts the output and presents it in a slightly more pleasing visual way through its graphical interface.

An arbitrary number of assertions, progress, accept, and end state labels can be defined in a model, but at all times there can be only one never claim. If never claims are derived from LTL formulae, the LTL property manager makes it easy to build a library of formulae, each of which can be stored in a separate file and checked against the model. The results of each run are stored automatically in the file that contains the corresponding LTL property. These files have the default extension .ltl.
Chapter 13. The Timeline Editor

A design without requirements cannot be incorrect. It can only be surprising.

—(Willem L. van der Poel, 1926–)

Although SPIN provides direct support for the formalization of correctness requirements in terms of linear temporal logic formulae, the use of this logic is not always as intuitive as one would like. The precise meaning of a temporal logic formula is sometimes counterintuitive, and can confound even the experts.

An alternative method, that we will explore in this chapter, is to express properties visually, with the help of a graphical tool. The tool we discuss here is called the timeline editor, created by Margaret Smith at Bell Labs. The inspiration for this tool came directly from lengthy discussions on the semantics of temporal logic, which led us to draw many small pictures of timelines on the whiteboard to illustrate sample execution sequences that were either intended to satisfy or to violate a given property. The timeline pictures were so useful that we decided to provide direct tool support for them. The tool was originally envisioned to generate only linear temporal logic formula as its output, but we later found it more effective to generate never claim automata in PROMELA syntax that can be used directly by SPIN in verifications.

Technically, the types of properties that can be expressed with the timeline editor tool do not cover everything that can be verified by SPIN, that is, they cover only a small subset of the set of all \( \omega \)-regular properties. The tool is not even expressive enough to let us specify everything that can be expressed with linear temporal logic, which itself also covers only a subset of the \( \omega \)-regular properties. Yet, the types of properties that can be expressed seems rich enough to specify many of the types of properties that one needs in system verification in practice. Users of model checking tools often tend to shy away from the use of truly complex temporal properties and restrict themselves wisely to a smaller subset of formulae for which it is easier to develop an accurate intuition. The timeline tool appears to capture just that subset and not much more.

The timeline tool allows us to define a causal relation on the events that can occur in a distributed system. It also allows us to restrict the set of sequences that contain the specified events to smaller sets that satisfy additional constraints on specific, user-defined intervals on the timeline. That is, the timeline allows us to select the set of execution sequences that is of interest to us, and then define some correctness criteria for them. The correctness criteria are expressed in the form of events that either must or may not be present at specific points in the execution.
An Example

A first example of a timeline specification is shown in Figure 13.1. It defines two events and one constraint on a system execution. At the top of the drawing canvas is a grey horizontal bar that represents the timeline. Time progresses from left to right along the bar. At regular intervals, there are vertical blue lines, called marks, that intersect the timeline. The first mark, numbered 0, is colored grey and for reference only. The remaining marks indicate points on the timeline where events and constraints can be attached. Marks do not represent clock ticks, but are simply used to indicate points of interest during a possibly long system execution. In between two marks any number of execution steps could pass.

Figure 13.1. Simple Example of a Timeline Specification

Events are attached directly to marks, and placed on the timeline itself. In Figure 13.1 there are two events: offhook and onhook. Constraints are placed underneath the timeline, spanning intervals between marks. One constraint, named !dialtone, is also shown. During verification the model checker attempts to match each system execution to the events that are placed on the timeline, provided that all corresponding constraints are satisfied. In Figure 13.1, no constraint applies to the occurrence of the first event, offhook, but as soon as it has occurred (immediately in the next state), the constraint !dialtone must be satisfied for the execution sequence to continue to match the timeline. If eventually, with the constraint still satisfied, the event onhook is seen, the timeline is completely matched. Reaching the end of a timeline by itself does not constitute an error condition. In this case, though, an error can be reported because the final event matched on the timeline is a fail event.

The requirement specified with the timeline in Figure 13.1 states that it is an error if an offhook event can be followed by an onhook event without a dialtone event occurring first.

For the purposes of property specification, the term event is somewhat of a misnomer. Both events and constraints are really conditions (state properties) that must be satisfied (i.e., that must hold) at specific points in an execution. In a PROMELA model, a state property is simply a boolean condition on global state variables that is said to be satisfied when it evaluates to true. This means that within the context of SPIN, an event occurrence is not necessarily an instantaneous phenomenon, but can persist for any amount of time. As a simple, though contrived, example, we could define the meaning of event offhook in Figure 13.1 to be true. This would mean that the event can be detected in any system state, and the event occurrence, as it were, persists forever. If the event persists forever, this merely means that it can be matched at any time during a system execution, so wherever we would place such an event on the timeline, it could always be matched. An event defined as false, on the other hand, could never be matched. If we define onhook as false in Figure 13.1, for instance, then the timeline specification could never be violated, not even if we also define the constraint !dialtone as true.

[ Team LiB ]
Types of Events

There are three different types of events that can be placed on a timeline.

- Regular events are labeled with the letter e. If a regular event occurs at a point in a system execution where its occurrence is specified, the execution matches the timeline. If it does not occur, the execution does not match. This does not mean that the execution is in error; it only means that the timeline property does not apply to the non-matching execution.

- Required events are labeled with the letter r. A required event can be matched in a system execution just like a regular event. This time, though, it is considered an error if the required event does not appear in the system execution at the point where it is specified, assuming of course that all earlier events on the timeline were matched, and all applicable constraints are satisfied.

- Failure events are labeled with the letter f. Failure events record conditions that should never be true at the point in a system execution where they are specified. It is considered to be an error if a failure event is matched. It is not an error if a failure event does not occur (i.e., is skipped).

Constraints are specified underneath a timeline. Each constraint persists over specific intervals of the timeline. Constraints are denoted by horizontal lines below the main timeline. The start and the end point of each constraint is always associated with a specific timeline mark. Optionally, the constraint can include or exclude the events that are attached to the begin and end marks on the timeline.

There can be any number of events and any number of constraints in a timeline specification, but only one event can be attached to any single timeline mark.
Defining Events

Events and constraints are represented by user-defined names on the timeline. The name can contain special characters, such as the negation symbols that we used in the name of the constraint in Figure 13.1. The names can be used directly to generate PROMELA never claims, but more typically one will want to define them more precisely to reflect the exact, perhaps more complex, conditions that must be satisfied for the corresponding event or constraint to apply. For the example in Figure 13.1, we can provide definitions for the events offhook, onhook, and !dialtone. The details of these definitions depend on the specifics of the verification model that is used to verify the timeline property. The timeline properties themselves are intended to be definable in a format that is largely model independent. For the final version of the model of a phone system that we develop in Chapter 14, the definitions of the events and the constraint used in Figure 13.1 could be as follows:

```
#define offhook   (last_sent == offhook)
#define onhook    (last_sent == onhook)
#define !dialtone !(session_ss7@Dial)
```

where the dialtone constraint is specified with the help of a remote reference to the process of type session_ss7. There is no real difference in the way that events or constraints are defined. Both events and constraints define state properties: boolean conditions on the system state that can be evaluated to true or false in any reachable system state of the model. Only their relative placement on a timeline determine their precise semantics, that is, whether they are used to act as events to guide the matching of system executions, or as constraints to restrict the types of executions that can match.
Matching a Timeline

The verification of a timeline proceeds as follows. In the initial system state, the first mark on the timeline is designated as the current mark. At each execution step of the system, the verifier evaluates the event condition attached to the current mark on the timeline, and it evaluates all constraint conditions attached to intervals that intersect the blue vertical line for this mark. If the next event to be matched is a failure event, then the event that follows it on the timeline, if any, will also be evaluated. If a condition evaluates to true, the corresponding event or constraint is said to be matched; otherwise, it is not matched. The context now determines what happens next. There are several possibilities.

- The current execution sequence no longer matches the timeline specification because a constraint condition is now violated. The verification attempt for this sequence can be abandoned.

- If all constraint conditions are satisfied and the event condition at the current mark is matched and that event is a failure event, an error can be reported.

- If under the same conditions the event at the current mark is not a failure event, the current mark is advanced to the next mark on the timeline, and the verification is repeated after the next system execution step is performed.

- If all constraint conditions are matched, but the event condition is not matched and the current event is not a failure event, then the current mark remains where it is, and the verification is repeated after the next system execution step is performed.

- If under the same conditions the current event is a failure event, and the next event on the timeline, if any, is matched, the current mark moves to the event that follows that next event, and the verification is repeated after the next system execution step is performed. The timeline tool does not permit two adjacent failure events on a timeline, so an event that follows a failure event is either a regular or a required event.

- If the end of an execution sequence is reached, but the end of the timeline has not been reached and the event at the current mark of the timeline is a required event, an error can be reported for this execution sequence.

If the end of a timeline is reached before the end of an execution, the verification effort can also be abandoned, since no further errors are possible.
Automata Definitions

The Büchi automaton that corresponds to the timeline specification from Figure 13.1 is shown in Figure 13.2. The automaton has three states, one of which, state s2, is accepting. The initial state of the automaton is s0.

**Figure 13.2. Büchi Automaton for the Timeline in Figure 13.1**

The automaton can be generated automatically by the timeline editor either in graphical form, as shown in Figure 13.2, or in PROMELA syntax as a never claim. The PROMELA version of the automaton is shown in Figure 13.3.

The second state of the automaton can only be reached if an offhook event occurs, which is followed by an interval in which dialtone remains false and no onhook event is detected. Then the transition to the accepting can be made if an onhook event occurs, still in the absence of a dialtone event. Once the accepting state is reached, the remainder of the run is automatically accepted due to the self-loop on true in state s2: the violation has already occurred and can no longer be undone by any future event.

**Figure 13.3 Never Claim for the Timeline in Figure 13.1**

```c
#define p1 (last_sent == offhook)    /* offhook */
#define p2 (last_sent == onhook)     /* onhook */
#define p3 !(session_ss7@Dial)       /* !dialtone */

never {
  S0: do
       :: p1 -> goto S1
       :: true
     od;
  acceptF0:
    assert(0);
    0;
  S1: do
       :: p2 && p3 -> goto acceptF0
       :: !p2 && p3
     od;
}
```
Constraints

A constraint interval always has one of four possible forms, depending on whether the start and the end points of the interval are included or excluded from the constraint. By adding constraints, we never really modify the structure of the Büchi automaton, or of the PROMELA never claim, that corresponds to a timeline. Added constraints can only restrict the number of sequences that can be matched at each step of the timeline, by adding conditionals to the transitions of an existing automaton structure.
Variations on a Theme

We have not said much about the rationale for the property that is expressed by the timeline specification from Figure 13.1. Informally, the property states that it would be an error if there can exist execution sequences in which an offhook event can be followed by an onhook event, without dialtone being generated in the interim. It may of course be possible for a telephone subscriber to generate a fast offhook–onhook sequence, but we may want to use the timeline specification to inspect precisely what happens under these circumstances by generating the matching execution scenarios.

We can also attempt to express this property in a different way. There can be small differences in semantics, depending on whether conditions are used as events or as constraints. As a small example, consider the variant of this property that is shown in Figure 13.4. We have switched the roles of dialtone and onhook as event and constraint here, compared to Figure 13.1.

Figure 13.4. Variation on the Timeline from Figure 13.1

At first blush, this timeline appears to express the same property, this time labeling the appearance of dialtone after an offhook as a required event, and the absence of onhook as a constraint.

We can see more clearly what is required to match this timeline by inspecting the corresponding automaton structure, as shown in Figure 13.5.

Figure 13.5. Büchi Automaton for the Timeline in Figure 13.4

This time, state s1 is the Büchi accepting state. The only way for an execution-sequence to trigger an error would be if it contained an offhook event that is never followed by either an onhook or a dialtone event. When state s2 is reached instead, the requirement expressed by the timeline specification is satisfied, and no further errors can result. This means that, technically, state s2, and the transition that leads to it, is redundant and could be omitted from the automaton without changing its meaning.

Assume now that there were an execution of the switch system we intended to verify that would occasionally fail to give dialtone after an offhook. Very likely, both in a verification model and in real life, the unlucky subscriber who encounters this behavior will not remain offhook forever, but eventually return the phone onhook. This means that the error, if present, would not be caught by this specific variant of the specification, unless we explicitly model behavior where the subscriber can permanently keep the phone off-hook.

In reality, the dialtone property for a telephone switch has both a functional and a real-time performance requirement. Dialtone should not only be generated after an offhook event, but on average also follow that event in 0.6 seconds. In 98.5% of the cases, further, dialtone should appear within 3 seconds after an offhook. Since timelines and SPIN models target the verification of only functional system requirements, the real-time performance aspects of
## Timelines With One Event

There are only two useful types of timelines that contain one single event. A timeline with a single regular event is not of use, since it does not express any requirement on an execution. That is, the timeline might match an execution that contains the event that is specified, but no matching execution can ever be flagged as erroneous in this way. The two smallest timelines of interest are the ones that contain either a single required or a single fail event, as illustrated in Figures 13.6 and 13.7.

**Figure 13.6. Timeline and Automaton for a Single Required Event**

<table>
<thead>
<tr>
<th>START</th>
<th>TIME</th>
</tr>
</thead>
<tbody>
<tr>
<td>a</td>
<td>r</td>
</tr>
</tbody>
</table>

The timeline specification from Figure 13.6 traps a system execution error in the same cases as the LTL formula that we would use to express the violation of a system invariant property

$$\Box \neg a = \neg \Diamond a.$$  

The timeline specification in Figure 13.7, similarly, traps a system execution error in the same cases as the property

$$\Diamond a.$$  

These first two properties can be seen as duals: one requires the absence of an event, and the other requires at least one occurrence.
Timelines With Multiple Events

With two events, we can form five different types of timelines. Each of the two events can be one of three different types, but clearly four of the nine possible combinations are not meaningful. A timeline with two regular events, for instance, cannot fail any system execution to which it is applied. Further, if the last event of the timeline is a regular event, then that event would always be redundant. And, finally, a timeline with two fail events that are placed on adjacent marks has no reasonable semantics, and is therefore rejected by the timeline tool. (In this case the conditions for the two fail events should probably be combined into a single condition.)

One of the five remaining meaningful combinations of two events is reproduced, with the corresponding automaton, in Figure 13.8.

Figure 13.8. Timeline and Automaton for a Regular and a Required Event

The timeline property from Figure 13.8 is similar, though not identical, to the LTL response property:

Note that the LTL property requires condition a to hold at the start of each sequence, since it is not preceded by a temporal operator. The timeline specification does not have that requirement. The LTL formula that precisely captures the timeline property from Figure 13.8 is somewhat more complex, namely:

\[ \neg (\Box (a \rightarrow X(\Diamond b))). \]

The example timeline in Figure 13.9 contains three of the five possible combinations of two events.

Figure 13.9. A More Complex Timeline Specification

We have labeled the four events on this timeline with letters from a to d, and added a constraint named z. A specification of this type could be used to check one of the requirements for the implementation of call waiting on telephone lines. Event a could then represent the occurrence of an incoming call on a line that is currently involved in a stable two-party call. The requirements state that with the call waiting feature in effect, the subscriber should at this point receive a call waiting alert tone, which would correspond to event b. Provided that none of the parties involved abandon their call attempts, or take any other action (which can be captured in constraint z), the first alert tone must be followed by a second such tone, but there may not be more than these two alerts. So, events b, c, and d would in this application of the timeline all represent the appearance of a call waiting alert tone, which is required twice, but...
The Link With LTL

It is not hard to show that for every timeline specification there exists a formalization in LTL, but the reverse is not necessarily true. Timelines are strictly less expressive than linear temporal logic, and therefore they are also less expressive than $\omega$-automata (which includes PROMELA never claims).

Consider, for instance, the LTL formula: $!(a U b)$. The positive version of this requirement would match any run in which a remains true at least until the first moment that b becomes true. If b is already true in the initial state, the requirement is immediately satisfied. The negation of the requirement matches any run where the positive version is violated. This means that in such a run b cannot be true in the initial state, and a must become false before b becomes true.

This seems like a requirement that we should be able to express in a timeline specification. The timeline we may draw to capture it is shown, together with the corresponding Büchi automaton, in Figure 13.13. We are slightly pushing the paradigm of timeline events here, by putting a negation sign before the name of a timeline event. Doing so, we exploit the fact that at least in the context of SPIN an event is really a state property that can be evaluated to true or false in every reachable system state.

Figure 13.13. Attempt to Express the LTL property $!(a U b)$

Unfortunately, the automaton that is generated does not precisely capture the LTL semantics. The correct Büchi automaton, generated with SPIN's built-in LTL converter, is shown in Figure 13.14. It closely resembles the timeline automaton from Figure 13.13, but it is not identical. In the correct version, the self-loop on state $s_0$ requires only $b$ to be false, but makes no requirement on the value of $a$.

Figure 13.14. The Correct Büchi Automaton for LTL property $!(a U b)$

In the timeline from Figure 13.13 we used a negation sign in front of an event symbol, in an attempt to capture the semantics of the LTL until property. If we go a little further and use arbitrary boolean expressions as place holders for events, we can create many more types of timelines. As just one example, consider the timeline that is shown in Figure 13.15. Although it looks very different from the timeline from Figure 13.13, it turns out to define precisely the same property.

Figure 13.15. A Variant of the Timeline in Figure 13.13
Bibliographic Notes

Several other visual formalisms for specifying systems and properties have been proposed over the years. The best known such proposals include Harel [1987] for systems specifications, and Schlor and Damm [1993] or Dillon, Kutty, Moser, et al. [1994] for property specification.

An alternative method to make it easier to capture complex logic properties as formulae in temporal logic is pursued by Matt Dwyer and colleagues at Kansas State University. Dwyer, Avrunin, and Corbett [1999] describe the design and construction of a comprehensive patterns database with formula templates for the most commonly occurring types of correctness properties.

Information for downloading the timeline editor, which is freely available from Bell Labs, can be found in Appendix D.
Chapter 14. A Verification Model of a Telephone Switch

"For when the actual facts show a thing to be impossible we are instantly convinced that it is so."

—(Polybius, The Histories, Book XII)

When faced with a software verification problem, it is often tempting to build a model that is as close to reality as possible. If an implementation exists, the temptation is to duplicate its functionality as faithfully as possible within the language of the model checker used. If only a design exists, the attempt can be to build a trial implementation for verification purposes. The purpose of this chapter is to show that this is not the best approach. The proper management of computational complexity is a key issue in all but the simplest applications of formal verification, and more often than not determines the success or failure of the attempt.
General Approach

The intuitive approach to software verification sketched here should be contrasted with the standard approach that one routinely takes in physics or mathematics. When one wants to analyze, say, the structural integrity of a bridge or a building, one does not start with a description of the structure that is as close to reality as possible. The best approach is to start with the simplest possible description of the structure that can capture the essential characteristics that must be analyzed. The reason is proper management of complexity. Even when mathematics is sufficiently expressive to describe reality in its minutest details, doing so would not only be a laborious task, it would not help in the least to simplify analytical chores. Computations on highly detailed descriptions, by man or by machine, can become so complex and time-consuming that the end results, if obtainable at all, become subject to doubt.
Keep it Simple

The purpose of a model checking exercise is not to build and analyze verification models that are as detailed as possible: it is the opposite. The best we can do is to find and build the smallest sufficient model to describe the essential elements of a system design. To construct that model, we attempt to simplify the problem, eliminating elements that have no direct bearing on the characteristics we want to verify. There is no universal recipe for how this can be accomplished. What works best is almost always problem dependent. Sometimes the smallest sufficient model can be constructed by generalizing a problem, and sometimes it requires specializing a problem.

The hardest problem of a verification project is to get started. The best advice that can be given here is to make a deliberate effort to start simple, perhaps even with a coarser abstraction than may seem justified. Then slowly evolve the verification model, and the corresponding correctness requirements, until sufficient confidence in the correctness of the design has been established. It is only reasonable to invest considerable resources into a verification at the very last phase of a project—to perform a final and thorough check to make sure that nothing of importance was missed in the earlier steps.

Throughout most of a verification effort, a tool like SPIN should be used in a mode where one can get instantaneous feedback about relatively simple descriptions of the design problem. Slowly, the description can become more refined, and as our confidence in its accuracy grows, our willingness to spend a little more time on each verification task can grow.
Managing Complexity

On a reasonably modern machine SPIN verifications should not consume more than a few seconds during the initial development of a verification model, and no more than a few minutes during the latter stages of verification. In very rare cases it may be necessary to spend up to a portion of an hour on a thorough verification in a final check, but this should be a very rare exception indeed.

To summarize this approach:[1]

[1] This approach to verification was first articulated by Prof. Jay Strother Moore from the University of Texas at Austin, when describing the proper use of interactive theorem provers.

- Start simple. Try to find the smallest sufficient model that can express something interesting about the problem you are trying to solve.

- Check the initial model thoroughly. More often than not you will be surprised that what you believed to be trivially true in the simplified world is not true at all. The typical reasons are small misjudgements in the development of the model, or subtle misunderstanding in the formulation of the properties checked for.

- Evolve the model and, if possible, its correctness properties step by step. Keep each incremental step small, and repeat the checks at each step. Stop when the complexity grows too rapidly and rethink the last change made. Try to find alternatives that can reduce the complexity. The numbers of asynchronously executing processes and the size of message buffers are the two most important sources of complexity in SPIN models, so try to keep these as small as possible at first.

- Keep the verification tool on a short leash. Do not spend more than a few seconds on initial verifications until you have developed sufficient confidence that what you ask the tool to verify is actually what you are interested in.

To illustrate this approach, we will discuss the development of a SPIN verification model for a significant fragment of an important and very well-known type of distributed system: a telephone switch. The problem context is familiar enough that many have attempted to build models like the ones we will discuss. Many of these attempts have ended in either a lost battle with the fundamental complexity of the underlying problem, or the adoption of simplifying but rather unrealistic assumptions about how a phone system actually works. We will try to do better here.
Modeling a Switch

The telephone system is so familiar to us that few of us realize that the underlying behavior can be phenomenally complex. Much of this complexity is due to the addition of feature behavior. Features such as three-way calling, call waiting, and call forwarding can interact in often unforeseen ways. Making sure that all such possible interactions comply with the relevant standards is a non-trivial task, even for experts. The problem is still quite non-trivial if we trim it down to its bare essence: providing support for only basic POTS (Plain Old Telephone Service) calls.

The normal dialogue for a POTS call looks simple. After taking the receiver off-hook, the subscriber hears a dial tone. This is the signal for the subscriber to dial a number. If that number is valid, the subscriber can expect to hear either a ring tone or a busy tone. If the number is invalid, an error tone or a busy tone will be the result. After a while, a ring tone can disappear when the call is answered, or it can turn into a busy tone when the maximum ring-time is exceeded. At any time during this sequence, the subscriber can abort the call and return the phone on-hook. This scenario is illustrated in Figure 14.1.

Figure 14.1. Typical Scenario for a POTS Call

Before reading on, put this book aside and attempt to build a small SPIN model that captures the interactions between a subscriber and a switch, as just sketched, restricting to outgoing calls for simplicity. Then do some verifications with SPIN to discover all the things that can go wrong with your model.
Subscriber Model

To develop a model that can reproduce the behavior from Figure 14.1, we will minimally have to model two entities: subscribers and switches. Because our focus will be on verifying properties of switch behavior, we should try to keep the number of assumptions we make about the behavior of subscribers as small as possible. We do not need to know, for instance, when or why subscribers place calls, why they hang up or why they sometimes fail to hang up. All we need to know about subscribers is what they can do that is visible to the switch. The set of things that a subscriber can do that is visible to the switch is blissfully small: the subscriber can lift the receiver off-hook, or return it on-hook. In between those two actions the subscriber can dial digits and flash the hook [2], and that is all we need to know.

[2] A flash-hook signal can have special significance for certain call features, such as, for instance, three-way calling. We will discuss this feature later in the chapter.

Let us first consider the sample subscriber model from Figure 14.2. It tries to capture the behavior of a fairly reasonable subscriber, responding to the tones that may be generated by the switch. Some of these tones are generated in response to subscriber actions and some can be generated seemingly spontaneously by the switch, for instance, to alert the subscriber to incoming calls.

Figure 14.2. Initial Behavior Model of a POTS Subscriber (Solid arrows refer to events triggered by the subscriber, and dashed arrows refer to signals that are generated by the switch.)

It is important to realize at this point that the subscriber model from Figure 14.2, though quite persuasive, is inadequate for our verification task. For our current purpose, the subscriber model is meant to capture the minimal set of assumptions that the switch can make about subscriber actions. In this context, then, it is unnecessary and even unwarranted to assume that the subscriber will always behave reasonably. Fortunately, many potentially unreasonable behaviors of the subscriber are in fact physically impossible. The subscriber cannot, for instance, generate two off-hook signals in a row without an intervening on-hook, and the subscriber cannot dial digits with the phone on-hook. There is, however, no reason to assume that the subscriber will always wait for a dial tone before aborting a call attempt, as Figure 14.2 seems to indicate. In fact, a subscriber may well ignore all tones from the switch in deciding what to do next.

We can modify the model from Figure 14.2 to reflect these assumptions by combining all states that are connected by transitions that correspond to the generation of audible tones in the switch (i.e., all dashed arrows). This produces the three-state model shown on the left in Figure 14.3.
Switch Model

The real complexity inevitably comes in the definition of the switch behavior, so it is again important to keep things as simple as possible at first. We will develop a switch model here for the handling of outgoing calls only, reducing the number of issues that we will have to confront somewhat. The interplay of incoming and outgoing calls can be subtle, but it can be studied separately once we have confidence in the basic model we are developing here.

A first-cut model of the switch behavior can then be formalized in PROMELA, in a simple state-oriented format, as shown in Figure 14.5. Because the audible tones are generated more for information than to restrict the subscriber actions, they appear in this model as print statements only. In particular, these signals need not be recorded in state variables.

**Figure 14.5 Simple Switch Model for Outgoing Calls**

```c
active proctype switch() /* outgoing calls only */ {
    Idle: if :: tpc?offhook ->
        printf("dial tone\n"); goto Dial
    fi;
    Dial:
        if :: tpc?digits ->
            printf("no tone\n"); goto Wait
        :: tpc?onhook ->
            printf("no tone\n"); goto Idle
        fi;
    Wait:
        if :: printf("ring tone\n") -> goto Connect;
            :: printf("busy tone\n") -> goto Busy
        fi;
    Connect:
        if :: printf("busy tone\n") -> goto Busy
            :: printf("no tone\n") -> goto Busy
        fi;
    Busy:
        if :: tpc?onhook ->
            printf("no tone\n"); goto Idle
        fi
}
```

In this model, the success or failure of an outgoing call is represented as a non-deterministic choice between the generation of a ring tone or a busy tone signal in state named Wait. The state named Connect represents the situation where call setup is completed. The call can now end either by the remote subscriber (which is not explicitly present in the model here) hanging up first, or the local subscriber hanging up first. In the first case, a busy tone will be generated; in the latter case no tone is generated. The two possibilities are again formalized with the help of a non-deterministic choice, indicating that both scenarios are possible.

There is no interaction with remote switches in the network represented in this model just yet. We will add that shortly, after we can convince ourselves that the simpler model is on track. As a first check, we can perform some short simulation runs, limiting the run to twenty steps. Such simulations show sensible call scenarios for this model, for instance, as follows:

```
$ spin -c -u20 version1
proc 0 = subscriber
proc 1 = switch
```

```c
q\p   0   1
1   tpc!offhook
1   .   tpc?offhook
dialtone
1   tpc!digits
1   .   tpc?digits
notone
ringtone
notone
1 tpc!onhook
1 .   tpc?onhook
notone
1 tpc!offhook
1 .   tpc?offhook
dialtone
1 tpc!digits
1 .   tpc?digits
notone
ringtone
-------------
depth-limit (-u20 steps) reached
-------------
final state:
-------------
#processes: 2
20:    proc 1 (switch) line 29 "version1" (state 12)
20:    proc 0 (subscriber) line 11 "version1" (state 6)
2 processes created
```

Next, we perform a verification. The verification run confirms that there are no major problems and that the behavior is still exceedingly simple, with just nine reachable, and no unreachable states. The results are as follows:

```
$ spin -a version1
$ cc -o pan pan.c
$ ./pan
(Spin Version 4.0.7 -- 1 August 2003)
+ Partial Order Reduction
Full statespace search for:
never claim            - (none specified)
assertion violations   +
acceptance cycles      - (not selected)
invalid end states     +
State-vector 24 byte, depth reached 11, errors: 0
9 states, stored
6 states, matched
15 transitions (= stored+matched)
0 atomic steps
hash conflicts: 0 (resolved)
(max size 2^18 states)
1.573   memory usage (Mbyte)
unreached in proctype subscriber
line 15, state 8, "-end-"
(1 of 8 states)
unreached in proctype switch
line 40, state 29, "-end-"
(1 of 29 states)
```

This puts us in a good position to extend our first model to a slightly more realistic one by adding the possible interactions with remote switches.
Remote Switches

So far, our switch model decides internally whether or not a call attempt failed or succeeded by making a non-deterministic decision on the generation of either a ring tone or a busy tone. We will now add a little more of the dialogue that can actually take place inside the switch during the setup of an outgoing call. In most cases the switch will have to interact with remote switches in the network to determine if the called number and the network resources that are needed to connect to it are available. The protocol for that is known as Signaling System 7, SS7 for short. A typical SS7 dialogue is shown in Figure 14.6.

Figure 14.6. SS7 Scenario for Call Setup

The first message sent by the local switch to a remote switch is called the initial address message, iam. The message triggers an address complete message, acm, in response. When the call is answered, an answer message, anm, follows. The teardown phase is started with a release, rel, request, which is acknowledged with a release confirmation, rlc.

To model this interaction we have to add a model of a remote switch. Note that we do not need to model the behavior of remote subscribers directly, because their behavior is not directly visible to the local switch. The remote subscribers are hidden behind remote switches and all negotiations about the setup and teardown of calls happen only through the intermediation of the remote switches. Also note that even though every switch acts both as a local switch to its local subscribers and as a remote switch to the rest of the network, it would be overkill to clone the local switch behavior to derive remote switch behavior. Doing so has the unintended consequence of making the detailed internal behavior of remote switches and remote subscribers visible to the verifier, which can significantly increase verification complexity.

Let us first extend the model of the local switch with the new SS7 message exchanges. This leads to the extended switch model shown in Figure 14.7.

Figure 14.7 Extended Local Switch Model

```
mttype = { iam, acm, anm, rel, rlc }; /* ss7 messages */
chan rms = [1] of { mtype }; /* channel to remote switch */

active proctype switch_ss7()
{
  Idle:
    if
      :: tpc?offhook -> printf("dial tone\n"); goto Dial
    fi;
  Dial:
    if
      :: tpc?digits -> printf("no tone\n"); rms!iam;
    fi;
  Connect:
    if
      :: tpc?onhook -> rms!rel; goto Zombie1
    fi;
  Zombie1:        /* on-hook, waiting for rlc */
    if
      :: tpc?rlc -> goto Zombie2
    fi;
  Zombie2:        /* remote switch is idle */
    if
      :: tpc?rel -> go
Adding Features

At this point we can improve the model by adding a treatment for incoming calls that originate at remote switches. We could also consider extending the model to handle multiple subscribers or end-to-end connections. Instead, we will try extend the switch behavior in a slightly more interesting way—by adding a call processing feature.
Three-Way Calling

We would like to add the capability for a subscriber to flash the hook after a call has been set up (i.e., quickly going on-hook and back off-hook) to place the currently connected party on hold and get a new dial tone. The subscriber should then be able to dial a new call, and establish a three-way connection by flashing the hook a second time. A third flash of the hook should terminate the three-way connection by dropping the last dialed party. We will assume that an on-hook from the originating subscriber during the call terminates all connections, independent of the current state of the call.

The addition of feature behavior like this to an existing call model often introduces unexpected types of interaction between the existing, trusted behavior and the newly added behavior. Being able to check these types of extensions with small verification models can therefore be of considerable value.

The switch must now be able to manage two connections for the same subscriber, so we will need to extend the model to have at least two instantiations of the model for a remote switch. We want to keep the control of the different connections separate, to make sure that we do not unnecessarily complicate the behavior of the switch. We can accomplish this by introducing a subscriber line session manager process that can interact with multiple session handlers. The manager keeps track of which session is active and shuttles the messages between sessions and subscriber. The various sessions are unaware of each other's existence and can behave just like in the single connection model from before.

A first change that we have to make to accomplish all this in the last model is to change the role of the switch process into that of a session manager. Before making any other changes to support the three-way calling feature directly, we will make and check this change. Figure 14.10 shows the new version of the switch process.

**Figure 14.10 Switch Session Management Structure**

```c
chan sess = [0] of { mtype };  
mtype = { idle, busy }; /* call states */ 
mtype s_state = idle;  
active proctype switch() 
{  
    mtype x;  
    atomic  
    {  
        run session_ss7(sess, rms);  
        run remote_ss7(rms, sess)  
    }  
    end: do  
    :: tpc?x ->  
    if  
    :: x == offhook ->  
    assert(s_state == idle);  
    s_state = busy  
    :: x == onhook ->  
    assert(s_state == busy);  
    s_state = idle  
    :: else  
    fi;  
    sess!x /* forward message */  
    od  
}
```

In this version of the switch process we have used a slightly different approach to the representation of the call states. Instead of using labeled control-flow points (as in Figure 14.9), we use mtype variables to store the state information.

The switch process now creates instantiations for a single session handler process and a remote switch, passing the proper message channels for input and output as parameters to these processes. We have added a channel named sess to be used by the switch process to pass call control messages from the subscriber to the local session handler.
A Three-Way Calling Scenario

Did we actually succeed in reproducing the three-way calling behavior we had in mind? We can make sure of this by formalizing and checking some properties that can together establish compliance with the required feature behavior. As one of those checks, we can check that the intended three-way calling behavior is at least possible, simply by claiming that it cannot occur and allowing SPIN to generate a counterexample. We can, for instance, check the behavior that results if the subscriber generates the sequence of off-hook, digit, and flash signals that corresponds to the correct setup of a three-way call. The problem we have to solve now is to detect the occurrence of these events with a system state property. The interaction between subscriber and the switch currently takes place via a rendezvous port, which cannot be polled for the presence of messages. We can get around this problem in two different ways. The more obvious method is perhaps to change the rendezvous port named tpc into a one-slot buffered message channel, so that the contents of the single slot can be polled. This change is effective, but it also increases the complexity of the verification, and it may introduce new behaviors. A quick check with SPIN tells us that the number of system states roughly triples (reaching 97,791 states), but no error behaviors are introduced.

Another method, which in this case incurs lower overhead, is to add a global state variable called last_sent, and to change the subscriber process in such a way that it always assigns the value of the last sent message to that variable, where it can be checked with a simple state property. The updated version of the subscriber process would then look as shown in Figure 14.14.

Figure 14.14 Revised Subscriber Process

```c
mtype last_sent;

active proctype subscriber()
{
    Idle:  tpc!offhook;
           last_sent = offhook;

    Busy:  if
           :: atomic { tpc!digits ->
                      last_sent = digits;
                      goto Busy
           }
           :: atomic { tpc!flash ->
                      last_sent = flash;
                      goto Busy
           }
           :: atomic { tpc!onhook ->
                      last_sent = onhook;
                      goto Idle
           }

    fi
}
```

With this change, the number of reachable states increases from 30,479 to 35,449 system states, a far smaller penalty.

The claim we are interested in can be formalized as shown in Figure 14.15. In this claim, we need to refer to the process instantiation numbers of the processes of type remote_ss7 and session_ss7. A simple way to find out what these pid numbers are is to print them in a verbose simulation run of the system.

Figure 14.15 Never Claim to Trigger Three-Way Calling Scenario

```c
#define Final \
    subscriber@Idle && switch@end \ 
    && remote_ss7[4]@Idle && remote_ss7[5]@Idle \ 
    && session_ss7[2]@Idle && session_ss7[3]@Idle
```

In Summary

In this chapter we have developed a relatively simple model of a telephone switch that represents an interesting fragment of its behavior for handling outgoing calls.

By starting with a very simple model that was revised in small and easily understood increments, we can catch errors at an early stage and avoid large blowups in the complexity of verification. After each small incremental step, we can check our intuition about the behavior of the model with short simulation and verification runs. Despite a few obvious limitations (e.g., the absence of a treatment for incoming calls), the model already includes some feature behavior that can be very challenging to implement correctly. The hard part of an exercise like this is to keep the model and its state space small, so that we can continue to verify it rigorously. This is an exercise in restriction and judicious abstraction. The target of this exercise is always to find the smallest sufficient model that allows us to verify all properties of interest.

Perhaps one of the nicer things about the use of a model checker such as SPIN is that the tool does not expect us to get things right on the first attempt. The tool can help us find both sources of complexity and sources of error. A model checking tool is often conveniently used as an exploratory tool: allowing the user to answer quick what-if questions about possible directions that might be taken to solve complex software design problems.
Chapter 15. Sample SPIN Models

"Few things are harder to put up with than the annoyance of a good example."

—(Mark Twain, 1835–1910)

In this chapter we will discuss a few small PROMELA models that exploit some interesting and possibly useful features of the specification language. We will focus mostly on language and modeling issues here. More examples of PROMELA models can be found in the standard SPIN distribution.
Eratosthenes

Our first example is a PROMELA version of an ancient algorithm for finding primes by counting off numbers and systematically intercepting the non-primes among them. The algorithm, a favorite programming exercise today, is due to the Greek philosopher and mathematician Eratosthenes of Cyrene (a city in modern day Libya which is today called Shahhat). Figure 15.1 shows a version in PROMELA that makes use of the fact that we can use dynamic process creation and pass channel identifiers between running processes.

Figure 15.1 The Sieve of Eratosthenes

```c
1 /*
2 The Sieve of Eratosthenes (c. 276-196 BC)
3 Prints all prime numbers up to MAX
4 */
5 #define MAX 25
6
7 mtype = { number, eof };
8
9 chan root = [0] of { mtype, int };
10
11 proctype sieve(chan c; int prime)
12 { chan child = [0] of { mtype, int };
13   bool haschild;
14   int n;
15
16   printf("MSC: %d is prime\n", prime);
17   end: do
18     :: c?number(n) ->
19       if
20         :: (n%prime) == 0 ->
21           printf("MSC: %d = %d*%d\n", n, prime, n/prime)
22         :: else ->
23           if
24             :: !haschild -> /* new prime */
25               haschild = true;
26               runsieve(child, n);
27             :: else ->
28               child!number(n)
29             fi;
30         fi
31     :: c?eof(0) ->
32       break
33   od;
34   if
35     :: haschild ->
36       child!eof(0)
37     :: else
38       fi
39 }
40
41 init
42 { int n = 2;
43   run sieve(root, n);
44   do
45     :: (n < MAX) -> n++; root!number(n)
46     :: (n >= MAX) -> root!eof(0); break
47   od
48 }
```

Because a PROMELA model must always be finite, we have to place an upper-bound on the largest integer value that we will test for primality. SPIN is not designed to handle computational problems, so do not expect to get away with a very large bound here. The bound is defined in Figure 15.1 in a macro definition named MAX. We have used

Process Scheduling

The next problem concerns the design of a reasonably efficient method for scheduling process execution in a multiprocessor system. The processes compete for access to shared resources, and they may have to be suspended when a resource is temporarily unavailable. The process suspension is done with a system call named sleep, which also records the particular resource that the process is waiting to access. When a process releases a resource, it calls the routine wakeup, which checks if any processes are currently suspended, waiting for the resource being released, and if so resumes execution of those processes. The data structures that record the state of the resource, and the data structures that record the state of the processes, are themselves also shared resources in the system, and access to them has to be protected with locks. In a uniprocessor system simply masking interrupts can suffice to lock out competing processes while operations on shared data structures are performed, but in a multiprocessor system this is not sufficient and we need to rely on higher-level locks.

In most systems, the availability of a global, indivisible test and set instruction can be assumed to solve this problem. If, for instance, we have a lock variable named lk, the indivisible test and set instruction, which is called spinlock in the UTS system, can be modeled in PROMELA as

```c
#define spinlock(lk) atomic { (lk == 0) -> lk = 1 }
```

and the matching lock release operation as

```c
#define freelock(lk) lk = 0
```

The scheduling problem is easy to solve if we would allow a process to simply set the spinlock for the duration of all access to the resource: it would effectively lock out all other processes. Such a solution would be very inefficient, though, forcing other processes to continue executing while competing to set the lock variable. The real challenge is to minimize the use of global locks, suspending process executions where possible, while securing that no process can accidentally be suspended forever. The latter problem is called a "missed wakeup."

The algorithm that was adopted for the Plan9 operating system was discussed in Pike et al. [1991], including a verification with and early version of SPIN. Another solution was proposed in Ruane [1990] for use in Amdahl's UNIX time sharing system, UTS®. We will consider Ruane's method here. An earlier discussion of this method appeared in Holzmann [1997b] with a commentary, exposing some flaws in that discussion, appearing in Bang [2001].

For our current purpose it is sufficient to restrict the number of shared resources in the system to just one single resource. This resource can be represented in the C implementation by a data structure of the following type:

```c
typedef struct R {
    int lock; /* locks access to resource */
    int wanted; /* processes waiting */
    ... /* other fields */
} R;
R *r; /* pointer to resource structure */
```

A process that gains access to the resource will set the lock field in the resource data structure to record that the resource is in use. If a process finds the resource locked, it suspends itself after setting the wanted flag to one, to indicate that it is waiting to acquire the resource.実際、これらの問題を解決するためには、プロセスがリソースへの全てのアクセスを简单にスピンロックで置ける効果的なロックを制御することが必要である。しかし、そのような解決策は非常に無効で、他のプロセスがリソースにアクセスするのを続けながら、リソースを競争して設定する必要がある。実質的な挑戦は、グローバルロックの使用を最小限に抑えることで、可能な場合でプロセス実行を停止するのではなく、リソースを无事故に停止できるようにすることである。この問題は "missed wakeup" と呼ばれる。


我々の目的を達成するためには、リソースを単一リソースであると考えることが十分である。このリソースは、C アセンブリによって次の型のデータ構造で表すことができる。

```c
typedef struct R {
    int lock; /* locks access to resource */
    int wanted; /* processes waiting */
    ... /* other fields */
} R;
R *r; /* pointer to resource structure */
```

プロセスがリソースにアクセスする場合、lock フィールドをリソースデータ構造に設定してリソースが使用されていることを記録する。リソースをロックした場合、リソースを取得しようとしているプロセスは、wanted フィールドを 1 に設定し、リソースを取得するのを待つことを示す。
A Client-Server Model

It is relatively simple to create SPIN models with a dynamically changing number of active processes. Each newly created process can declare and instantiate its own set of local variables, so through the creation of a new process we can also create additional message channels. It may be somewhat confusing at first that message channel identifiers can have a process local scope, if declared within a proctype body, but that the message channels themselves are always global objects. The decision to define channels in this way makes it possible to restrict the access to a message channel to only specifically identified processes: message channels can be passed from one process to another. We will use this feature in the design of a simple, and fairly generic client-server model.

We will design a system with a single, fixed server that can receive requests from clients over a known global channel. When the server accepts a request for service, it assigns that request to an agent and provides a private channel name to the client that the client can use to communicate with the agent. The remainder of the transaction can now place between agent and client, communicating across a private channel without further requiring the intermediacy of the server process. Once the transaction is complete, the agent returns the identifier for the private channel to the server and exits.

_Figure 15.5_ shows the design of the agent and server processes. The fixed global channel on which the server process listens is declared as a rendezvous port called server. The server process has a private, locally declared, set of instantiated channels in reserve. We have given the server process a separate local channel, named pool, in which it can queue the channels that have not yet been assigned to an agent. The first few lines in the server process declaration fill up this queue with all available channels.

**Figure 15.5 Agent and Server Processes**

```c
#define N 2

mtype = { request, deny, hold, grant, return };

chan server = [0] of { mtype, chan };

proctype Agent(chan listen, talk) {
    do
        :: talk!hold(listen)
        :: talk!deny(listen) -> break
        :: talk!grant(listen) ->
    wait:
        listen?return; break
        od;
        server!return(listen)
}

active proctype Server() {
    chan agents[N] = [0] of { mtype };
    chan pool = [N] of { chan };
    chan client, agent;
    byte i;

    do
        :: i < N -> pool!agents[i]; i++
        :: else -> break
        od;

    end: do
        :: server?request(client) ->
            if
                :: empty(pool) ->
                    client!deny(0)
                :: nempty(pool) ->
                    pool?agent;
                    run Agent(agent,client)
            fi
        od;
}
```

_A Client-Server Model_
Square Roots?

We began our introduction to PROMELA in Chapter 2 almost inevitably with the PROMELA version of hello world. In retrospect, we can see that this example stretches the meaning of the term verification model. It defines only one single process, so clearly not much process interaction or synchronization could be happening. A model checker may be used to demonstrate that this little system cannot deadlock or get entangled into non-progress cycles, but the results that are obtained from such experiments will not be much of a revelation. Of course, PROMELA does not prevent us from writing such models, although it does try to deprive us from the tools we would need to put too much emphasis on non-concurrency aspects. This shows up specifically in the rudimentary support in the language for specifying pure computations. There are, for instance, no data types for float, double, or real in PROMELA. There is also no direct support for function calls or for recursion. These omissions are not accidental. It is deliberately hard to specify anything other than rudimentary computations in PROMELA, and deliberately easy to specify the infrastructure and the mutual dependency of concurrently executing processes.

This is not to say that no computation whatsoever can be done in PROMELA. It can. As a small example, consider the following PROMELA program that computes the integer square root of a given integer number. [1]


```
proctype sqroot(int N)
{
    int x, y;
    y = 1<<15;
    do
        :: y > 0 ->
            x = x^y; /* set bit */
            if
                :: x*x > N -> /* too large */
                    x = x^y /* clear bit */
                :: else /* leave set */
                    fi;
            y = y>>1 /* next bit */
        :: else ->
            break /* done */
    od;
    printf("integer sqrt(%d) = %d\n", N, x)
}
```

A few constructs are used here that will look familiar to C programmers. The proctype named sqroot is declared non-active, which means that no instance of it is assumed to be started by default. An instance can be initiated by another process, and at the same time that process can then pass an integer parameter, N, to the newly instantiated process, specifying the number for which the integer square root is to be computed. That instantiation can look, for instance, as follows:

```
active proctype main()
{
    run sqroot(3601)
}
```

which uses the second mechanism in PROMELA to instantiate processes: through the use of the run operator.

Another, perhaps more convenient, way of defining the instantiation would be with a parameter, as in:
Adding Interaction

The main objection we can levy against the last example is that it really defines only sequential, not concurrent, behavior, with no synchronizations or interactions. With a few small changes we can turn the example into a slightly more interesting, though still rather minimal, distributed system model. We will set up the integer square root routine as a little square root server process that can perform its computations at the request of client processes. We will rearrange the code somewhat to accomplish this.

The first thing that we need to do is to declare a message channel for communication between clients and server, for instance, as follows:

```
#define NC 4
chan server = [NC] of { chan, int };
```

The first line defines a constant named NC. The constant is used in the declaration to set the capacity of the channel named server. The messages that can be passed through this channel are declared to have two fields: one of type chan that can hold a channel identifier, and one of type int that can hold an integer value.

Next, we rewrite the square root server process, so that it will read requests from this channel and respond to the client with the computed value, via a channel that the client provides in the request. The new version looks as follows:

```
active proctype sqroot()
{
    chan who;
    int val, n;

    do
        :: server?who,n ->
            compute(n, val);
        who!val
    od
}
```

First, the server process declares a channel identifier named who, which this time is not initialized in the declaration. It also declares an integer variable n. These two variables are used to store the parameter values for the communication with a client, as provided by that client. A second integer variable val will be used to retrieve the result value that is to be communicated back to the client. The body of the square root server consists of a do loop with just one option, guarded by a message receive operation.

We have moved the actual computation into an inline definition, named compute. The variable name n, recording the value received from the client, is passed to the inline, as is the name of the variable val in which the result is to be computed.

After the call to compute completes, the value is returned to the client process in a send operation.

Before we fill in the details of the inline call, recall that an inline is merely a structured piece of macro text where the names of variables that are passed in as parameters textually substitute their placeholders inside the inline definition. Therefore, inlines are not the same as procedures: they cannot return results, and they do not have their own variable scope. All variables that are visible at the point of call of an inline are also visible inside the inline body, and, perhaps more noteworthy, all variables declared inside the inline are also visible outside it, after the point of call.

The inlined code for compute can now be written as follows:

```
inline compute(N, x)
{

    int y;

    
    {       chan who;
    
        int val, n;
        do
            :: server?who,n ->
                compute(n, val);
            who!val
        od

    y = y>>1       /* next bit */
    :: else
        y = y>>1       /* next bit */
        :: else               /* leave set */
            x = x^y    /* clear bit */
        :: x*x > N ->   /* too large */
            if
        
    y > 0 ->
        do
            :: server?who,n ->
                compute(n, val);
            who!val
        od
    fi;
    return val;
}
```

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    y = y>>1       /* next bit */
    :: else
        y = y>>1       /* next bit */
        :: else               /* leave set */
            x = x^y    /* clear bit */
        :: x*x > N ->   /* too large */
            if
        
    y > 0 ->
        do
            :: server?who,n ->
                compute(n, val);
            who!val
        od
    fi;
    return val;
}
```
Adding Assertions

In the last version of the model we captured the behavior of a system of at least a few concurrent processes, and there was some interaction to boot. It is still not quite a verification model, though. The only thing we could prove about this system, for instance, is that it cannot deadlock and has no unreachable code segments. SPIN does not allow us to prove any mathematical properties of this (or any) square root algorithm. The reason is that SPIN was designed to prove properties of process interactions in a distributed system, not of process of computations.

To prove some minor additional facts about the process behaviors in this example, we can nonetheless consider adding some assertions. We may, for instance, want to show that on the specific execution of the square root computations that we execute, the result will be in the expected range. We could do so in the client processes, for instance, by modifying the code as follows:

```promela
active [NC] proctype client()
{
    chan me = [0] of { int };
    int v;
    server!me(10*_pid) -> me?v;
    assert(v*v <= 10*_pid && (v+1)*(v+1) > 10*_pid)
}
```

Another thing we can do is to select a more interesting set of values on which to run the computation. A good choice would be to select a value in the middle of the range of integer values, and a few more that try to probe boundary cases. Since we cannot directly prove the mathematical properties of the code, the best we can do is to use one approach that resembles testing here. To illustrate this, we now change the client processes into a single tester process that is defined as follows:

```promela
active proctype tester()
{
    chan me = [0] of { int };
    int n, v;
    if
        :: n = -1   /* fails */
        :: n = 0   /* ok */
        :: n = 1023   /* ok */
        :: n = 1<<29 /* ok */
        :: n = 1<<30 /* fails */
        fi;
    server!me(n) -> me?v;
    assert(v*v <= n && (v+1)*(v+1) > n)
}
```

Executing this model in SPIN's simulation mode as before may now succeed or fail, depending on the specific value for n that is chosen in the non-deterministic selection at the start of the tester. Along the way, it is worth observing that the five option sequences in this selection structure all consist of a single guard, and the guards are all assignments, not conditional expressions. The PROMELA semantics state that assignments are always executable, independent of the value that is assigned. If we execute the little model often enough, for example, five or more times, we will likely see all possible behaviors.

Not surprisingly, the algorithm is not equipped to handle negative numbers as input; the choice of -1 leads to an assertion failure. All other values, except for the last, work fine. When the value 1<<30 is chosen, though, the result is:
A Comment Filter
In Chapter 3 (p. 69) we briefly discussed a seldom used feature in PROMELA that allows us to read input from the
user terminal in simulation experiments. The use of STDIN immediately implies that we are not dealing with a closed
system, which makes verification impossible. Still, the feature makes for nice demos, and we will use it in this last
example to illustrate the use of PROMELA inlines.
The problem we will use as an excuse to write this model is to strip C-style comments from text files. Figure 15.8
shows the general outline of a deterministic automaton for stripping comment strings from C programs. According to
the rules of C, the character pair /* starts a comment and the first subsequent occurrence of the pair */ ends it. There
are some exceptions to this rule though. If the combination /* appears inside a quoted string, for instance, it does not
start a comment, so the automaton must be able to recognize not just comments but also quoted strings. To make
things more interesting still, the quote character that starts or ends a string can itself be quoted (as in '"') or escaped
with a backslash (as in "\""). In the automaton from Figure 15.8, states s1 and s2 deal with strings, and states s6, s7,
and s8 deal with quoted characters.
Figure 15.8. A Sample Automaton to Check C-Style Comment Conventions

The transition labels that we have used in Figure 15.8 represent classes of input characters that must be matched for
the transition to be executable. The meaning is as follows. A transition label that consists of a single symbol, represents
a match in the input stream of the corresponding ASCII character. A dot symbol, for example, on the transition from
s2 to s1, represents a match of any single character in the input stream. The symbol ¬ (pronounced not) represents a
match on any character other than all those that are listed behind the ¬ symbol in the transition label. This symbol is
not itself an ASCII character, so there can be no confusion about its meaning. The label ¬ * on the transition from s3
to s4, for instance, represents the match of any character other than *, and the label ¬ /"on the self-loop at state s0
means any character other than the forward slash character / or the quote character".
If the input sequence provided to this automaton conforms to the C comment conventions that are captured here, the
automaton should terminate in its initial (and final) state s0.
Part of the complexity of this automaton comes from the fact that characters can be escaped with backslashes, and
can appear inside single or double quote marks. The comment delimiters could also appear inside text strings, making
it hard to accurately recognize where a comment begins and ends in cases such as these:

/* the comment begins here
* printf("but it doesn't end */ here yet\n");
*/
if (s == '"') /* not the start of a string */
printf("/* not a comment */\n");


Chapter 16. PROMELA Language Reference

"The infinite multitude of things is incomprehensible, and more than a man may be able to contemplate."

—(Giambattista della Porta, 1535–1615, Natural Magick)

The PROMELA manual pages that are included in this book can be grouped into seven main sections. The first five of these sections, plus the grammar description given here, describe the language proper. The entries from the sixth section cover those things that are deliberately not in the language, and contain a brief explanation of why they were left out. The entries from the seventh and last section cover the more recent extensions to the PROMELA language to support the use of embedded C code statements and data declarations. The main sections are:

1. Meta Terms (translated by preprocessors into vanilla PROMELA)
2. Declarators (for defining process, channel, and data objects)
3. Control Flow Constructors (separators, compound statements, jumps, labels, etc.)
4. Basic Statements (such as send, receive, assignment, etc.)
5. Predefined Functions and Operators (such as len, run, nempty, etc.)
6. Omissions (such as floating point, probabilities, etc.)
7. Extensions (for embedded C code)

This chapter contains the manual pages for the first six of these sections, listed in alphabetical order with the section name indicated at the top of each page. Chapter 17 separately introduces the extensions for embedded C code and contains the corresponding manual pages from the last section in our list.

In the tradition of the classic UNIX manuals, each manual page contains some or all of the following eight defining elements.
Name

A one sentence synopsis of the language construct and its main purpose.
Syntax

The syntax rules for the language construct. Optional terms are enclosed in (non-quoted) square brackets. The Kleene star * is used to indicate zero or more repetitions of an optional term. When the special symbols '[', ']', or '*', appear as literals, they are quoted. For instance, in

```c
chan name = '\[const\]' of { typename [, typename ] * }
```

the first two square brackets are literals, and the last two enclose an optional part of the definition that can be repeated zero or more times. The terms set in italic, such as name, const, and typename, refer to the grammar rules that follow.
EXECUTABILITY

Defines all conditions that must be satisfied for a basic statement from the fourth section to be eligible for execution. Some standard parts of these conditions are assumed and not repeated throughout. One such implied condition is, for instance, that the executing process has reached the point in its code where the basic statement is defined. Implied conditions of this type are defined in the description of PROMELA semantics in Chapter 7. If the executability clause is described as true, no conditions other than the implied conditions apply.
EFFECT

Defines the effect that the execution of a basic statement from the fourth section will cause on the system state. One standard part of the effect is again always implied and not repeated everywhere: the execution of the statement may change the local state of the executing process. If the effect clause is described as none, no effect other than the implicit change in local state is defined. See also the PROMELA semantics description in Chapter 7.
DESCRIPTION

Describes in informal terms the purpose and use of the language construct that is defined.
Examples

Gives some typical applications of the construct.
Notes

Adds some additional notes about special circumstances or cautions.
See Also

Gives references to other manual pages that may provide additional explanations.
Grammar Rules

The following list defines the basic grammar of PROMELA. Choices are separated by vertical bars; optional parts are included in square brackets; a Kleene star indicates zero or more repetitions of the immediately preceding grammar fragment; literals are enclosed in single quotes; uppercase names are keywords; lowercase names refer to the grammar rules from this list. The name any_ascii_char appears once, and is used to refer to any printable ASCII character except ".". PROMELA keywords are spelled like the token-names in the grammar, but in lowercase instead of uppercase.

The statement separator used in this list is the semicolon ';'. In all cases, the semicolon can be replaced with the two-character arrow symbol '<->' without change of meaning.

We will not attempt to include a full grammar description for the language C, as it can appear inside the embedded C code statements. Where it appears, we have abbreviated this as ... C ... in the grammar rules that follow.

```
spec  : module [ module ] *
module : utype    /* user defined types */
        | mtype    /* mtype declaration */
        | decl_lst /* global vars, chans */
        | proctype /* proctype declaration */
        | init     /* init process - max 1 per model */
        | never    /* never claim - max 1 per model */
        | trace    /* event trace - max 1 per model */
        | c_code   '{' ... C ... '}'
        | c_decl   '{' ... C ... '}'
        | c_state  string string [ string ]
        | c_track  string string
proctype: [ active ] PROCTYPE name '{' [ decl_lst ]'}'
        [ priority ] [ enabler ] '{' sequence '}'
init    : INIT [ priority ] '{' sequence '}'
never   : NEVER '{' sequence '}'
trace   : TRACE '{' sequence '}'
        | NOTRACE '{' sequence '}'
utype   : TYPEDEF name '{' decl_lst '}'
mttype  : MTYPE [ '=' ] '{' name [ ',' name ] * '}'
dec_lst: one_decl [ ';' one_decl ] *
one_decl: [ visible ] typename ivar [',' ivar ] *
typename: BIT  | BOOL  | BYTE  | PID
        | SHORT | INT  | MTYPE | CHAN
        | name  /* user defined typenames (see utype) */
active  : ACTIVE [ '[' const ']' ] /* instantiation */
priority: PRIORITY const          /* simulation only */
enabler : PROVIDED '([' expr ']'  /* constraint */
visible : HIDDEN
        | SHOW
sequence: step [ ';' step ] *
```

"Grammar Rules"
Main Sections

The manual pages that follow are in alphabetical order, with the section name indicated. The pages can be grouped per section as follows:

Meta Terms

comments (p. 396), false (p. 416), inline (p. 428), ltl (p. 434), macros (p. 436), skip (p. 478), true (p. 486).

Declarators

accept (p. 379), active (p. 381), arrays (p. 383), bit (p. 403), bool (p. 403), byte (p. 403), chan (p. 394),
D_proctype (p. 458), datatypes (p. 403), end (p. 413), hidden (p. 422), init (p. 426), int (p. 403), local (p. 433),
ntype (p. 438), never (p. 441), notrace (p. 483), pid (p. 403), priority (p. 453), proctype (p. 458), progress (p. 459),
provided (p. 461), short (p. 403), show (p. 477), trace (p. 483), typedef (p. 487), unsigned (p. 403), xr (p. 493),
xp (p. 493).

Control Flow

atomic (p. 390), break (p. 393), d_step (p. 401), do (p. 406), fi (p. 424), goto (p. 420), if (p. 424), labels (p. 430),
od (p. 406), separators (p. 475), sequence (p. 476), unless (p. 490).

Basic Statements

assert (p. 385), assign (p. 388), condition (p. 400), printf (p. 451), printm (p. 451), receive (p. 466), send (p. 473).

Predefined

_ (p. 373), _last (p. 373), _nr_pr (p. 373), _pid (p. 377), cond_expr (p. 398), else (p. 408), empty (p. 410),
enabled (p. 412), eval (p. 415), full (p. 419), len (p. 432), nempty (p. 440), nfull (p. 446), np_ (p. 447),
pc_value (p. 448), poll (p. 450), remoterefs (p. 468), run (p. 470), STDIN (p. 480), timeout (p. 481).

Embedded C Code

c_expr (p. 511), c_code (p. 505), c_decl (p. 508), c_state (p. 508), c_track (p. 508).

Omissions

float (p. 417), hierarchy (p. 423), pointers (p. 449), probabilities (p. 454), procedures (p. 455), rand (p. 462),
realtime (p. 464), scanf (p. 472).
Reference

Table 16.1 gives an overview of all the manual pages that describe the PROMELA language, together with the corresponding page numbers. Five of the primitives are discussed in Chapter 17, with the corresponding manual pages following on pages 505 to 511.
Special Cases

Several language features apply only in special cases. Two types of special cases include those features that only affect the specific way in which either a simulation or a verification run is performed. Other types of special case include features that are either incompatible with the enforcement of SPIN’s partial order reduction method or with the breadth-first search option, and features that are mutually incompatible. We summarize all these special cases next.

Table 16.1. Index of All Manual Pages

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Name

_ - a predefined, global, write-only, integer variable.

Syntax

Description

The underscore symbol _ refers to a global, predefined, write-only, integer variable that can be used to store scratch values. It is an error to attempt to use or reference the value of this variable in any context.

Examples

The following example uses a do-loop to flush the contents of a channel with two message fields of arbitrary type, while ignoring the values of the retrieved messages:

do
:: q?_,_
:: empty(q) -> break
od

See Also

_nr_pr, _last, _pid, np_, hidden
**_last**

**Name**

_last - a predefined, global, read-only variable of type pid.

**Syntax**

_last

**Description**

_last is a predefined, global, read-only variable of type pid that holds the instantiation number of the process that performed the last step in the current execution sequence. The initial value of _last is zero.

The _last variable can only be used inside never claims. It is an error to assign a value to this variable in any context.

**Examples**

The following sample never claim attempts to match an infinite run in which the process with process initialization number one executes every other step, once it starts executing.

```plaintext
never {
    do
    :: (_last != 1)
    :: else -> break
    od;

    accept:
    do
    :: (_last != 1) -> (_last == 1)
    od
}
```

Because the initial value of variable _last is zero, the first guard in the first do loop is always true in the initial state. This first loop is designed to allow the claim automaton to execute dummy steps (passing through its else clause) until the process with instantiation number one executes its first step, and the value of _last becomes one. Immediately after this happens, the claim automaton moves from into its second state, which is accepting. The remainder of the run can only be accepted, and reported through SPIN's acceptance cycle detection method, if the process with instantiation number one continues to execute every other step. The system as a whole may very well allow other executions, of course. The never claim is designed, though, to intercept just those runs that match the property of interest.

**Notes**

During verifications, this variable is not part of the state descriptor unless it is referred to at least once. The additional state information that is recorded in this variable will generally cause an increase of the number of reachable states. The most serious side effect of the use of the variable _last in a model is, though, that it prevents the use of both partial order reduction and of the breadth-first search option.

**See Also**

_, _nr_pr, _pid, never, np_
_nr_pr

Name

_nr_pr - a predefined, global, read-only, integer variable.

Syntax

_nr_pr

Description

The predefined, global, read-only variable _nr_pr records the number of processes that are currently running (i.e., active processes). It is an error to attempt to assign a value to this variable in any context.

Examples

The variable can be used to delay a parent process until all of the child processes that it created have terminated. The following example illustrates this type of use:

```proctype child()
{
    printf("child %d\n", _pid)
}
active proctype parent()
{
    do :: (_nr_pr == 1) ->
        run child()
    od
}
```

The use of the precondition on the creation of a new child process in the parent process guarantees that each child process will have process instantiation number one: one higher than the parent process. There can never be more than two processes running simultaneously in this system. Without the condition, a new child process could be created before the last one terminates and dies. This means that, in principle, an infinite number of processes could result. The verifier puts the limit on the number of processes that can effectively be created at 256, so in practice, if this was attempted, the 256th attempt to create a child process would fail, and the run statement from this example would then block.

See Also

_, _last, _pid, active, procedures, run
_pid

Name

_pid - a predefined, local, read-only variable of type pid that stores the instantiation number of the executing process.

Syntax

_pid

Description

Process instantiation numbers begin at zero for the first process created and count up for every new process added. The first process, with instantiation number zero, is always created by the system. Processes are created in order of declaration in the model. In the initial system state only process are created for active proctype declarations, and for an init declaration, if present. There must be at least one active proctype or init declaration in the model.

When a process terminates, it can only die and make its _pid number available for the creation of another process, if and when it has the highest _pid number in the system. This means that processes can only die in the reverse order of their creation (in stack order).

The value of the process instantiation number for a process that is created with the run operator is returned by that operator.

Instantiation numbers can be referred to locally by the executing process, through the predefined local _pid variable, and globally in never claims through remote references.

It is an error to attempt to assign a new value to this variable.

Examples

The following example shows a way to discover the _pid number of a process, and gives a possible use for a process instantiation number in a remote reference inside a never claim.

```plaintext
active [3] proctype A()
{
    printf("this is process: %d
", _pid);
L:    printf("it terminates after two steps
")
}
never {
    do
        :: A[0]@L -> break
    od
}
```

The remote reference in the claim automaton checks whether the process with instantiation number zero has reached the statement that was marked with the label L. As soon as it does, the claim automaton reaches its end state by executing the break statement, and reports a match. The three processes that are instantiated in the active proctype declaration can execute in any order, so it is quite possible for the processes with instantiation numbers one and two to terminate before the first process reaches label L.

Notes

A never claim, if present, is internally also represented by the verifier as a running process. This claim process has no visible instantiation number, and therefore cannot be referred to from within the model. From the user's point of view, the process instantiation numbers are independent of the use of a never claim.

See Also

_, _last, _nr_pr, active, init, never, proctype, remoterefs, run
**accept**

**Name**

accept - label-name prefix used for specifying liveness properties.

**Syntax**

accept [a-zA-Z0-9_] *: stmt

**Description**

An accept label is any label name that starts with the six-character sequence accept. It can appear anywhere a label can appear as a prefix to a PROMELA statement.

Accept labels are used to formalize Büchi acceptance conditions. They are most often used inside never claims, but their special meaning is also recognized when they are used inside trace assertions, or in the body of a proctype declaration. There can be any number of accept labels in a model, subject to the naming restrictions that apply to all labels (i.e., a given label name cannot appear more than once within the same defining scope).

A local process statement that is marked with an accept label can also mark a set of global system states. This set includes all states where the marked statement has been reached in the process considered, but where the statement has not yet been executed. The SPIN generated verifiers can prove either the absence or presence of infinite runs that traverse at least one accept state in the global system state space infinitely often. The mechanism can be used, for instance, to prove LTL liveness properties.

**Examples**

The following proctype declaration translates into an automaton with precisely three local states: the initial state, the state in between the send and the receive, and the (unreachable) final state at the closing curly brace of the declaration.

The accept label in this model formalizes the requirement that the second state cannot persist forever, and cannot be revisited infinitely often either. In the given program this would imply that the execution should eventually always stop at the initial state, just before the execution of sema!p.

```plaintext
active proctype dijkstra()
{
    do
    :: sema!p ->
    accept:  sema?v
    od
}
```

**Notes**

When a never claim is generated from an LTL formula, it already includes all required accept labels. As an example, consider the following SPIN generated never claim:

```plaintext
dell: spin -f '[]<>(p U q)'
never {
/* []<>(p U q) */
T0_init:
    if
```
active

Name

active - prefix for proctype declarations to instantiate an initial set of processes.

Syntax

active proctype name ( [ decl_lst ] ) { sequence}
active [ 'const' ] proctype name ( [ decl_lst ] ) { sequence }

Description

The keyword active can be prefixed to any proctype declaration to define a set of processes that are required to be active (i.e., running) in the initial system state. At least one active process must always exist in the initial system state. Such a process can also be declared with the help of the keyword init.

Multiple instantiations of the same proctype can be specified with an optional array suffix of the active prefix. The instantiation of a proctype requires the allocation of a process state and the instantiation of all associated local variables. At the time of instantiation, a unique process instantiation number is assigned. The maximum number of simultaneously running processes is 255. Specifying a constant greater than 255 in the suffix of an active keyword would result in a warning from the SPIN parser, and the creation of only the first 255 processes.

Processes that are instantiated through an active prefix cannot be passed arguments. It is, nonetheless, legal to declare a list of formal parameters for such processes to allow for argument passing in additional instantiations with a run operator. In this case, copies of the processes instantiated through the active prefix have all formal parameters initialized to zero. Each active process is guaranteed to have a unique _pid within the system.

Examples

active proctype A(int a) { ... }
active [4] proctype B() { run A(_pid) }

One instance of proctype A is created in the initial system state with a parameter value for a of zero. In this case, the variable a is indistinguishable from a locally declared variable. Four instances of proctype B are also created. Each of these four instances will create one additional copy of proctype A, and each of these has a parameter value equal to the process instantiation number of the executing process of type B. If the process of type A is assigned _pid zero, then the four process of type B will be assigned _pid numbers one to three. All five processes that are declared through the use of the two active prefixes are guaranteed to be created and instantiated before any of these processes starts executing.

Notes

In many PROMELA models, the init process is used exclusively to initialize other processes with the run operator. By using active prefixes instead, the init process becomes superfluous and can be omitted, which reduces the amount of memory needed to store global states.

If the total number of active processes specified with active prefixes is larger than 255, only the first 255 processes (in the order of declaration) will be created.

See Also

_pid, init, proctype, remoterefs, run
arrays

Name

arrays - syntax for declaring and initializing a one-dimensional array of variables.

Syntax

typename name [' const '] [ = any_expr ]

Description

An object of any predefined or user-defined datatype can be declared either as a scalar or as an array. The array elements are distinguished from one another by their array index. As in the C language, the first element in an array always has index zero. The number of elements in an array must be specified in the array declaration with an integer constant (i.e., it cannot be specified with an expression). If an initializer is present, the initializing expression is evaluated once, and all array elements are initialized to the same resulting value.

In the absence of an explicit initializer, all array elements are initialized to zero.

Data initialization for global variables happens in the initial system state. All process local variables are initialized at process instantiation. The moment of creation and initialization of a local variable is independent of the precise place within the proctype body where the variable declaration is placed.

Examples

The declaration

byte state[N]

with N a constant declares an array of N bytes, all initialized to zero by default. The array elements can be assigned to and referred to in statements such as

state[0] = state[3] + 5 * state[3*2/n]

where n is a constant or a variable declared elsewhere. An array index in a variable reference can be any valid (i.e., side-effect free) PROMELA expression. The valid range of indices for the array state, as declared here, is 0..N-1.

Notes

Scalar objects are treated as shorthands for array objects with just one element. This means that references to scalar objects can always be suffixed with [0] without triggering a complaint from the SPIN parser. Be warned, therefore, that if two arrays are declared as

byte a[N], b[N];
assert

Name

assert - for stating simple safety properties.

Syntax

assert (expr)

Executability

ture

EFFECT

none

Description

An assert statement is similar to skip in the sense that it is always executable and has no other effect on the state of the system than to change the local control state of the process that executes it. A very desirable side effect of the execution of this statement is, however, that it can trap violations of simple safety properties during verification and simulation runs with SPIN.

The assert statement takes any valid PROMELA expression as its argument. The expression is evaluated each time the statement is executed. If the expression evaluates to false (or, equivalently, to the integer value zero), an assertion violation is reported.

Assertion violations can be ignored in a verification run, by invoking the SPIN generated verifier with run-time option -A, as in:

```
$ ./pan -A
```

Examples

The most common type of assertion statement is one that contains just a simple boolean expression on global or local variable values, for instance, as in:

```
assert(a > b)
```

A second common use of the assertion is to mark locations in a proctype body that are required, or assumed, to be unreachable, as in:

```
assert(false)
```
**assignment**

**Name**

assignment - for assigning a new value to a variable.

**Syntax**

\[
\text{varref} = \text{any_expr}
\]

\[
\text{varref}++ \text{ as shorthand for } \text{varref} = \text{varref} + 1
\]

\[
\text{varref}-- \text{ as shorthand for } \text{varref} = \text{varref} - 1
\]

**Executability**

true

**Effect**

Replaces the value of varref with the value of any_expr, where necessary truncating the latter value to the range of the datatype of varref.

**Description**

The assignment statement has the standard semantics from most programming languages: replacing the value stored in a data object with the value returned by the evaluation of an expression. Other than in the C language, the assignment as a whole returns no value and can therefore itself not be part of an expression.

The variable reference that appears on the left-hand side of the assignment operator can be a scalar variable, an array element, or a structure element.

**Examples**

\[
a = 12 \quad /* \text{scalar} */
\]

\[
r.b[a] = a \times 4 + 7 \quad /* \text{array element in structure} */
\]

Note that it is not valid to write:

\[
a = b++
\]

because the right-hand side of this assignment is not a side effect free expression in PROMELA, but it is shorthand for another assignment statement. The effect of this statement can be obtained, though, by writing:

\[
\text{atomic} \{ \ a = b; \ b++ \ \}
\]
atomic

Name

atomic - for defining a fragment of code that is to be executed indivisibly.

Syntax

atomic { sequence }

Effect

Within the semantics model, as defined in Chapter 7, a side effect of the execution of any statement, except the last, from an atomic sequence is to set global system variable exclusive to the instantiation number of the executing process, thus preserving the exclusive privilege to execute.

Description

If a sequence of statements is enclosed in parentheses and prefixed with the keyword atomic, this indicates that the sequence is to be executed as one indivisible unit, non-interleaved with other processes. In the interleaving of process executions, no other process can execute statements from the moment that the first statement of an atomic sequence is executed until the last one has completed. The sequence can contain arbitrary PROMELA statements, and may be non-deterministic.

If any statement within the atomic sequence blocks, atomicity is lost, and other processes are then allowed to start executing statements. When the blocked statement becomes executable again, the execution of the atomic sequence can be resumed at any time, but not necessarily immediately. Before the process can resume the atomic execution of the remainder of the sequence, the process must first compete with all other active processes in the system to regain control, that is, it must first be scheduled for execution.

If an atomic sequence contains a rendezvous send statement, control passes from sender to receiver when the rendezvous handshake completes. Control can return to the sender at a later time, under the normal rules of non-deterministic process interleaving, to allow it to continue the atomic execution of the remainder of the sequence. In the special case where the recipient of the rendezvous handshake is also inside an atomic sequence, atomicity will be passed through the rendezvous handshake from sender to receiver and is not interrupted (except that another process now holds the exclusive privilege to execute).

An atomic sequence can be used wherever a PROMELA statement can be used. The first statement of the sequence is called its guard, because it determines when the sequence can be started. It is allowed, though not good style, to jump into the middle of an atomic sequence with a goto statement, or to jump out of it in the same way. After jumping into the sequence, atomic execution may begin when the process gains control, provided that the statement jumped to is executable. After jumping out of an atomic sequence, atomicity is lost, unless the target of the jump is also contained in an atomic sequence.

Examples

atomic { /* swap the values of a and b */
    tmp = b;
    b = a;
    a = tmp
}

In the example, the values of two variables a and b are swapped in an uninterruptable sequence of statement executions. The execution of this sequence cannot be blocked, since all the statements it contains are always unconditionally executable.

An example of a non-deterministic atomic sequence is the following:

atomic {
    if :: a = 1 :: a = 2 fi;
    if :: b = 1 :: b = 2 fi
}

In this example, the variables a and b are assigned a single value, with no possible intervening statement from any other process. There are four possible ways to execute this atomic sequence.

It is possible to create a global atomic chain of executions, with two or more processes alternately executing, by passing control back and forth with rendezvous operations.

chan q = [0] of { bool }
active proctype X() { atomic { A; q!0; B } }
active proctype Y() { atomic { q?0 -> C } }

In this example, for instance, execution could start in process X with the program block named A. When the rendezvous handshake is executed, atomicity would pass to process Y, which now starts executing the block named C. When it terminates, control can pass back to X, which can then atomically execute the block named B.

It is often useful to use atomic sequences to start a series of processes in such a way that none of them can start executing statements until all of them have been initialized:

atomic {
    run A(1,2);
    run B(2,3);
    run C(3,1)
}

Notes

Atomic sequences can be used to reduce the complexity of a verification. If an infinite loop is accidently included in an atomic sequence, the verifier cannot always recognize the cycle. In the default depth-first search mode, the occurrence of such an infinite cycle will ultimately lead to the depth limit being exceeded, which will truncate the loop. In breadth-first search mode, though, this type of an infinite cycle will be detected. Note that it is an error if an infinite cycle appears inside an atomic sequence, since in that case the atomic sequence could not possibly be executed atomically in any real implementation.

PROMELA d_step sequences can be executed significantly more efficiently by the verifier than atomic sequences, but do not allow non-determinism.

See Also
d_step, goto, receive, send
break

Name

break - jump to the end of the innermost do loop.

Syntax

break

Description

The keyword break does not indicate an executable statement, but it instead acts like a special type of semicolon: merely indicating the next statement to be executed. The search for the next statement to execute continues at the point that immediately follows the innermost do loop.

When the keyword break does not follow a statement, but appears as a guard in an option of a selection structure or do loop, then the execution of this statement takes one execution step to reach the target state, as if it were a skip. In all other cases, the execution of a break statement requires no separate step; the move to the target state then occurs after the execution of the preceding statement is completed.

If the repetition structure in which the break statement occurs is the last statement in a proctype body or never claim, then the target state for the break is the process's or claim's normal termination state, where the process or claim remains until it dies and is removed from the system.

Examples

L1: do
    :: t1 -> t2
    :: t3 -> break
    :: break
    od;
L2: ...

In this example, control reaches the label L1 immediately after statement t2 is executed. Control can also reach label L2 immediately after statement t3 is executed, and optionally, in one execution step, control can also move from label L1 to label L2.

Notes

It is an error to place a break statement where there is no surrounding repetition structure. The effect of a break statement can always be replicated with the use of a goto statement and a label.

See Also

do, goto, if, labels, skip
**chan**

**Name**

chan - syntax for declaring and initializing message passing channels.

**Syntax**

```plaintext
chan name
chan name = [' const '] of { typename [, typename ] * }
```

**Description**

Channels are used to transfer messages between active processes. Channels are declared using the keyword `chan`, either locally or globally, much like integer variables. Channels by default store messages in first-in first-out order (but see also the sorted send option in the manual page for `send` and the random receive option in the manual page for `receive`).

The keyword `chan` can be followed by one or more names, in a comma-separated list, each optionally followed by a channel initializer. The syntax

```plaintext
chan a, b, c[3]
```

declares the names `a`, `b`, and `c` as uninitialized channels, the last one as an array of three elements.

A channel variable must be initialized before it can be used to transfer messages. It is rare to declare just a channel name without initialization, but it occurs in, for instance, proctype parameter lists, where the initialized version of a channel is not passed to the process until a process is instantiated with a run operator.

The channel initializer specifies a channel capacity, as a constant, and the structure of the messages that can be stored in the channel, as a comma-separated list of type names. If the channel capacity is larger than zero, a buffered channel is initialized, with the given number of slots to store messages. If the capacity is specified to be zero, a rendezvous port, also called a synchronous channel, is created. Rendezvous ports can pass messages only through synchronous handshakes between sender and receiver, but they cannot store messages.

All data types can be used inside a channel initializer, including typedef structure names, but not including the `typename unsigned`.

**Examples**

The following channel declaration contains an initializer:

```plaintext
chan a = [16] of { short }
```

The initializer says that channel `a` can store up to 16 messages. Each message is defined to have only one single field, which must be of type `short`. Similarly,
comments

Name

comments - default preprocessing rules for comments.

Syntax

/* [ any_ascii_char ] */

Description

A comment starts with the two character sequence /* and ends at the first occurrence of the two character sequence */. In between these two delimiters, any text, including newlines and control characters, is allowed. None of the text has semantic meaning in PROMELA.

A comment can be placed at any point in a verification model where white space (spaces, tabs, newlines) can appear.

Examples

/* comment */ init /* comment */ {
    int /* an integer */ v /* variable */;
    v /* this / * is * / okay */ ++;
}

This PROMELA fragment is indistinguishable to the parser to the following PROMELA text, written without comments:

init {
    int v;
    v++;
}

Notes

Comments are removed from the PROMELA source before any other operation is performed. The comments are removed by invoking the standard C preprocessor cpp (or any equivalent program, such as gcc -E), which then runs as an external program in the background. This means that the precise rules for comments are determined by the specific C preprocessor that is used. Some preprocessors, for instance, accept the C++ commenting style, where comments can start with two forward slashes and end at the first newline. The specific preprocessor that is used can be set by the user. For more details on this, see the manual page for macros.

With the default preprocessor, conform ANSI-C conventions, comments do not nest. Be careful, therefore, that if a closing comment delimiter is accidently deleted, all text up to and including the end of the next comment may be stripped.

On a PC, SPIN first tries to use a small, built-in macro preprocessor. When this fails, for instance, when macros with multiple parameters are used or when additional preprocessor directives are provided on the command line, the
**cond_expr**

**Name**

conditional expression - shorthand for a conditional evaluation.

**Syntax**

( any_expr -> any_expr : any_expr )

**Description**

The conditional expression in PROMELA is based on the version from the C programming language. To avoid parsing conflicts, though, the syntax differs slightly from C. Where in C one would write

\[ p?q:r \]

the corresponding expression in PROMELA is

\[(p -> q : r)\]

The question mark from the C version is replaced with an arrow symbol, to avoid confusion with the PROMELA receive operator. The round braces around the conditional expression are required, in this case to avoid the misinterpretation of the arrow symbol as a statement separator.

When the first expression (p in the example) evaluates to non-zero, the conditional expression as a whole obtains the value of the second expression (q), and else it obtains the value of the last expression (r).

**Examples**

The following example shows a simple way to implement conditional rendezvous operations.

```promela
chan q[3] = [0] of { mtype };
sender: q[(P -> 1 : 2)]!msg -> ...
receiver: q[(Q -> 1 : 0)]?msg -> ...
```

Two dummy rendezvous channels (q[0] and q[2]) are used here to deflect handshake attempts that should fail. The handshake can only successfully complete (on channel q[1]) if both the boolean expression P at the receiver side and the boolean expression Q at the sender side evaluate to true simultaneously. The dummy rendezvous channels q[0] and q[2] that are used here do not contribute any measurable overhead in a verification, since rendezvous channels take up no memory in the state vector.

An alternative way of specifying a conditional rendezvous operation is to add an extra message field to the channel and to use the predefined eval function in the receive statement, as follows.

```promela
global: chan port = [0] of { mtype, byte, byte };
sender: port!mesg(12, (P -> 1 : 0))
receiver: port?mesg(data, eval(Q -> 1 : 2))
```

Unfortunately, the message field cannot be declared as a boolean, since we need a third value to make sure no match occurs when both P and Q evaluate to false.
condition

Name

condition statement - for conditional execution and synchronization.

Syntax

expr

Executability

(expr != 0)

Effect

none

Description

In PROMELA, a standalone expression is a valid statement. A condition statement is often used as a guard at the start of an option sequence in a selection or repetition structure. Execution of a condition statement is blocked until the expression evaluates to a non-zero value (or, equivalently, to the boolean value true). All PROMELA expressions are required to be side effect free.

Examples

(1)                 /* always executable               */
(0)                 /* never executable                */
skip                /* always executable, same as (1) */
true                /* always executable, same as skip */
false               /* always blocks, same as (0) */
a == b              /* executable only when a equals b */

A condition statement can only be executed (passed) if it holds. This means that the statement from the first example can always be passed, the second can never be passed, and the last cannot be passed as long as the values of variables a and b differ. If the variables a and b are local, the result of the evaluation cannot be influenced by other processes, and this statement will work as either true or false, depending on the values of the variables. If at least one of the variables is global, the statement can act as a synchronizer between processes.

See Also

do, else, false, if, skip, true, timeout, unless
**d_step**

**Name**

d_step - introduces a deterministic code fragment that is executed indivisibly.

**Syntax**

d_step { sequence }

**Description**

A d_step sequence is executed as if it were one single indivisible statement. It is comparable to an atomic sequence, but it differs from such sequences on the following three points:

- No goto jumps into or out of a d_step sequence are allowed.

- The sequence is executed deterministically. If non-determinism is present, it is resolved in a fixed and deterministic way, for instance, by always selecting the first true guard in every selection and repetition structure.

- It is an error if the execution of any statement inside the sequence can block. This means, for instance, that in most cases send and receive statements cannot be used inside d_step sequences.

**Examples**

The following example uses a d_step sequence to swap the value of all elements in two arrays:

```c
#define N 16
byte a[N], B[N];

init {
    d_step {
        /* swap elements */
        byte i, tmp;
        i = 0;
        do
            :: i < N ->
                tmp = b[i];
                b[i] = a[i];
                a[i] = tmp; i++
            :: else ->
                break
        od;
        skip /* add target for break */
    }
    ...
}
```

A number of points should be noted in this example. First, the scope of variables i and tmp is independent of the precise point of declaration within the init body. In particular, by placing the declaration inside the d_step sequence we declare i and tmp outside of the d_step sequence and can use them in the declaration of the loop.

Notes

A d_step sequence can be executed much more efficiently during verifications than an atomic sequence. The difference in performance can be significant, especially in large-scale verifications.

The d_step sequence also provides a mechanism in PROMELA to add new types of statements to the language, translating into new types of transitions in the underlying automata. A c_code statement has similar properties.

See Also

atomic, c_code, goto, sequence
**datatypes**

**Name**

bit, bool, byte, pid, short, int, unsigned - predefined data types.

**Syntax**

typename name [ = anyexpr ]

unsigned name : constant [ = anyexpr ]

**Description**

There are seven predefined integer data types: bit, bool, byte, pid, short, int, and unsigned. There are also constructors for user-defined data types (see the manual pages for mtype, and typedef), and there is a separate predefined data type for message passing channels (see the manual page for chan).

Variables of the predefined types can be declared in C-like style, with a declaration that consists of a typename followed by a comma-separated list of one or more identifiers. Each variable can optionally be followed by an initializer. Each variable can also optionally be declared as an array, rather than as a scalar (see the manual page for arrays).

The predefined data types differ only in the domain of integer values that they provide. The precise domain may be system dependent in the same way that the corresponding data types in the C language can be system dependent.

Variables of type bit and bool are stored in a single bit of memory, which means that they can hold only binary, or boolean values.

ISO compliant implementations of C define the domains of all integer data types in a system header file named limits.h, which is accessible by the C compiler. Table 16.2 summarizes these definitions for a typical system.

Variables of type unsigned are stored in the number of bits that is specified in the (required) constant field from the declaration. For instance,

```
unsigned x : 5 = 15;
```

declares a variable named x that is stored in five bits of memory. This declaration also states that the variable is to be initialized to the value 15. As with all variable declarations, an explicit initialization field is optional. The default initial value for all variables is zero. This applies both to scalar variables and to array variables, and it applies to both global and to local variables.

If an attempt is made to assign a value outside the domain of the variable type, the actual value assigned is obtained by a type cast operation that truncates the value to the domain. Information is lost if such a truncation is applied. SPIN will warn if this happens only during random or guided simulation runs.

Table 16.2. Typical Data Ranges

<table>
<thead>
<tr>
<th>Type</th>
<th>C-Equivalent</th>
<th>limits.h</th>
<th>Typical Range</th>
</tr>
</thead>
<tbody>
<tr>
<td>bit</td>
<td>bit-field</td>
<td>-</td>
<td>0..1</td>
</tr>
</tbody>
</table>
do

Name

do - repetition construct.

Syntax

do :: sequence [ :: sequence ] * od

Description

The repetition construct, like all other control-flow constructs, is strictly seen not a statement, but a convenient method to define the structure of the underlying automaton.

A repetition construct has a single start and stop state. Each option sequence within the construct defines outgoing transitions for the start state. The end of each option sequence transfers control back to the start state of the construct, allowing for repeated execution. The stop state of the construct is only reachable via a break statement from within one of its option sequences.

There must be at least one option sequence in each repetition construct. Each option sequence starts with a double-colon. The first statement in each sequence is called its guard. An option can be selected for execution only when its guard statement is executable. If more than one guard statement is executable, one of them will be selected non-deterministically. If none of the guards are executable, the repetition construct as a whole blocks.

A repetition construct as a whole is executable if and only if at least one of its guards is executable.

Examples

The following example defines a cyclic process that non-deterministically increments or decrements a variable named count:

```promela
byte count;

active proctype counter()
{
    do
        :: count++
        :: count-
        :: (count == 0) ->
            break
    od
}
```

In this example the loop can be broken only when count reaches zero. It need not terminate, though, because the other two options always remain unconditionally executable. To force termination, we can modify the program as follows:

```promela
active proctype counter()
{
    do
        :: count != 0 ->
            if
```
else

Name

else - a system defined condition statement.

Syntax

else

Description

The predefined condition statement else is intended to be used as a guard (i.e., the first statement) of an option sequence inside selection or repetition constructs.

An else condition statement is executable if and only if no other statement within the same process is executable at the same local control state (i.e., process state).

It is an error to define control flow constructs in which more than one else may need to be evaluated in a single process state.

Examples

In the first example, the condition statement else is equivalent to the regular expression statement \((a < b)\).

```plaintext
if
:: a > b -> ...
:: a == b -> ...
:: else -> ... /* evaluates to: a < b */
fi
```

Note also that round braces are optional around expression statements.

In this example:

```plaintext
A: do
:: if
    :: x > 0 -> x--
    :: else -> break
fi
:: else -> x = 10
od
```

both else statements apply to the same control state, which is marked with the label A here. To show the ambiguity more clearly, we can rewrite this example also as:

```plaintext
A: do
:: x > 0 -> x--
:: else -> break
:: else -> x = 10
```
**empty**

**Name**

empty - predefined, boolean function to test emptiness of a buffered channel.

**Syntax**

`empty ( name )`

**Description**

Empty is a predefined function that takes the name of a channel as an argument and returns true if the number of messages that it currently holds is zero; otherwise it returns false. The expression

```
empty(q)
```

where q is a channel name, is equivalent to the expression

```
(len(q) == 0)
```

**Examples**

```
chan q = [8] of { mtype };

d_step {
  do
  :: q?_
  :: empty(q) -> break
  od;
  skip
}
```

This example shows how the contents of a message channel can be flushed in one indivisible step, without knowing, or storing, the detailed contents of the channel. Note that execution of this code is deterministic. The reason for the `skip` statement at the end is explained in the manual page for `d_step`.

**Notes**

A call on `empty` can be used as a guard, or it can be used in combination with other conditionals in a boolean expression. The expression in which it appears, though, may not be negated. (The SPIN parser will intercept this.) Another predefined function, `nempty`, can be used when the negated version is needed. The reason for the use of `empty` and `nempty` is to assist SPIN’s partial order reduction strategy during verification.

If predefined functions such as `empty` and `nempty` are used in the symbol definitions of an LTL formula, they may unintentionally appear under a negation sign in the generated automaton, which can then trigger a surprising syntax error from SPIN. The easiest way to remedy such a problem, if it occurs, is to revise the generated never claim
enabled

Name

enabled - predefined boolean function for testing the enabledness of a process from within a never claim.

Syntax

enabled ( any_expr )

Description

This predefined function can only be used inside a never claim, or equivalently in the symbol definition for an LTL formula.

Given the instantiation number of an active process, the function returns true if the process has at least one executable statement in its current control state, and false otherwise. When given the instantiation number of a non-existing process, the function always returns false.

In every global state where enabled(p) returns true, the process with instantiation number p has at least one executable statement. Of course, the executability status of that process can change after the next execution step is taken in the system, which may or may not be from process p.

Examples

The following never claim attempts to match executions in which the process with instantiation number one remains enabled infinitely long without ever executing.

```
never {
    accept:
        do :: _last != 1 && enabled(1)
        od
}
```

Notes

The use of this function is incompatible with SPIN's partial order reduction strategy, and can therefore increase the computational requirements of a verification.

See Also

_last, _pid, ltl, never, pc_value, run
**end**

**Name**

end - label-name prefix for marking valid termination states.

**Syntax**

end [a-zA-Z0-9_] *: stmt

**Description**

An end-state label is any label name that starts with the three-character sequence end. End-state labels can be used in proctype, trace, and notrace declarations.

When used in a proctype declaration, the end-state label marks a local control state that is acceptable as a valid termination point for all instantiations of that proctype.

If used in an event trace definition, the end-state label marks a global control state that corresponds to a valid termination point for the system as a whole.

If used in an event notrace definition, though, the normal meaning reverses: the event trace is now considered to have been completely matched when the end state is reached, thus signifying an error condition, rather than normal system termination.

End-state labels have no special meaning when used in never claims.

**Examples**

In the following example the end-state label defines that the expected termination point of the process is at the start of the loop.

```plaintext
active proctype dijkstra()
{
    end:    do
        :: sema!p -> sema?v
    od
}
```

It will now be flagged as an invalid end-state error if the system that contains this proctype declaration can terminate in a state where the process of type dijkstra remains at the control state that exists just after the arrow symbol.

**Notes**

It is considered an invalid end-state error if a system can terminate in a state where not all active processes are either at the end of their code (i.e., at the closing curly brace of their proctype declarations) or at a local state that is marked with an end-state label.

If the run-time option -q is used with the compiled verifier, an additional constraint is applied for a state to be considered a valid end state: all message channels must then also be empty.

**See Also**

accept, labels, notrace, progress, trace
eval

Name

eval - predefined unary function to turn an expression into a constant.

Syntax

eval ( any_expr )

Description

The intended use of eval is in receive statements to force a match of a message field with the current value of a local or global variable. Normally, such a match can only be forced by specifying a constant. If a variable name is used directly, without the eval function, the variable would be assigned the value from the corresponding message field, instead of serving as a match of values.

Examples

In the following example the two receive operations are only executable if the precise values specified were sent to channel q: first an ack and then a msg.

```plaintext
mtype = { msg, ack, other };  
chan q = [4] of { mtype };  
mtype x;  

x = ack; q?eval(x)     /* same as: q?ack */  
x = msg; q?eval(x)     /* same as: q?msg */
```

Without the eval function, writing simply

```
q?x
```

would mean that whatever value was sent to the channel (e.g., the value other) would be assigned to x when the receive operation is executed.

Notes

Any expression can be used as an argument to the eval function. The result of the evaluation of the expression is then used as if it were a constant value.

This mechanism can also be used to specify a conditional rendezvous operation, for instance by using the value true in the sender and using a conditional expression with an eval function at the receiver; see also the manual page for conditional expressions.

See Also

cond_expr, condition, poll, receive
false

Name

false - predefined boolean constant.

Syntax

false

Description

The keyword false is a synonym of the constant value zero (0), and can be used in any context. If it is used as a stand-alone condition statement, it will block system execution as if it were a halt instruction.

Notes

Because they are intercepted in the lexical analyzer as meta terms, false, true, and skip do not show up as such in error traces. They will appear as their numeric equivalents (0) or (1).

See

condition, skip, true
float

Name

float - floating point numbers.

Description

There are no floating point numbers in basic PROMELA because the purpose the language is to encourage abstraction from the computational aspects of a distributed application while focusing on the verification of process interaction, synchronization, and coordination.

Consider, for instance, the verification of a sequential C procedure that computes square roots. Exhaustive state-based verification would not be the best approach to verify this procedure. In a verification model, it often suffices to abstract this type of procedure into a simple two-state demon that non-deterministically decides to give either a correct or incorrect answer. The following example illustrates this approach.

```plaintext
mtype = { number, correct, incorrect }
chan sqrt = [0] of { mtype, chan };

active proctype sqrt_server()
{
    do
        :: sqrt?number(answer) ->
            /* abstract from local computations */
            if
                :: answer!correct
                :: answer!incorrect
            fi
    od
}

active proctype user()
{
    chan me = [0] of { mtype };
    do
        :: sqrt!number(me);
        if
            :: me?correct -> break
            :: me?incorrect ->
                ...
        fi;
    od;
    ...
}
```

The predefined data types from PROMELA are a compromise between notational convenience and modest constraints that can facilitate the construction of tractable verification models. The largest numeric quantity that can be manipulated is, for instance, a 32-bit integer number. The number of different values that even one single integer variable can record, for instance, when used as a simple counter, is already well beyond the scope of a state-based model checker. Even integer quantities, therefore, are to be treated with some suspicion in verification models, and can very often be replaced advantageously with byte or bit variables.

Notes

In the newer versions of SPIN, there is an indirect way to use external data types, such as float, via embedded code and embedded declarations. The burden on the user to find abstractions can thus be lightened, in return for a potential increase in verification complexity. When using embedded C code, the user can decide separately if some or all of the embedded data objects should be treated as part of the state descriptor in the verification model, with the use of `c_state` or `c_track` declarators. See Chapter 17 for a detailed description.

See Also
c_code, c_decl, c_expr, datatypes
full

Name

full - predefined, boolean function to test fullness of a channel.

Syntax

full ( varref )

Description

Full is a predefined function that takes the name of a channel as an argument and returns true if that channel currently contains its maximum number of messages, and otherwise it returns false. It is equivalent to the expression

(len(q) == QSZ)

where q is the channel name, and QSZ is the message capacity of the channel.

This function can only be applied to buffered channels. The value returned for rendezvous channels would always be false, since a rendezvous channel cannot store messages.

Examples

```plaintext
chan q = [8] of { byte };
byte one_more = 0;

do
:: q!one_more; one_more++       /* send messages */
:: full(q) -> break            /* until full    */
do;
assert(len(q) == 8)
```

Notes

Full can be used as a guard, by itself, or it can be used as a general boolean function in expressions. It can, however, not be negated (for an explanation see also the manual page for empty).

If predefined functions such as full, or nfull are used in the symbol definitions of an LTL formula, they may unintentionally appear under a negation sign in the generated automaton, which can then trigger a surprising syntax error from SPIN.

See Also

condition, empty, len, ltl, nempty, nfull
goto

Name

goto - unconditional jump to a labeled statement.

Syntax

goto name

Description

The goto is normally not executed, but is used by the parser to determine the target control state for the immediately preceding statement; see also the manual page for break. The target state is identified by the label name and must be unique within the surrounding proctype declaration or never claim.

In cases where there is no immediately preceding statement, for instance, when the goto appears as a guard in an option of a selection or repetition structure, the goto is executed as if it were a skip, taking one execution step to reach the labeled state.

Examples

The following program fragment defines two control states, labeled by L1 and L2:

L1:     if
:: a != b -> goto L1
:: a == b -> goto L2
fi;
L2:     ...

If the values of variables a and b are equal, control moves from L1 to L2 immediately following the execution of condition statement a == b. If the values are unequal, control returns to L1 immediately following the execution (evaluation) of a != b. The statement is therefore equivalent to

L1:     do
:: a != b
:: a == b -> break
od;
L2:     ...

and could also be written more efficiently in PROMELA as simply:

L1:     a == b;
L2:     ...

Note that the last version makes use of the capability of PROMELA to synchronize on a standalone condition statement.
hidden

Name

hidden - for excluding data from the state descriptor during verification.

Syntax

hidden typename ivar

Description

The keyword hidden can be used to prefix the declaration of any variable to exclude the value of that variable from the definition of the global system state. The addition of this prefix can affect only the verification process, by potentially changing the outcome of state matching operations.

Examples

hidden byte a;
hidden short p[3];

Notes

The prefix should only be used for write-only scratch variables. Alternatively, the predefined write-only scratch variable _ (underscore) can always be used instead of a hidden integer variable.

It is safe to use hidden variables as pseudo-local variables inside d_step sequences, provided that they are not referenced anywhere outside that sequence.

See Also

_, datatypes, local, show
hierarchy

Name

hierarchy - for defining layered systems.

Description

There is no mechanism for defining a hierarchically layered system in PROMELA, nor is there a good excuse to justify this omission. At present, the only structuring principles supported in PROMELA are proctypes, inlines, and macros.

See Also

inline, macros, proctype, procedures
The selection construct, like all other control-flow constructs, is strictly seen not a statement, but a convenient method to define the structure of the underlying automaton. Each selection construct has a unique start and stop state. Each option sequence within the construct defines outgoing transitions for the start state, leading to the stop state. There can be one or more option sequences. By default, the end of each option sequence leads to the control state that follows the construct.

There must be at least one option sequence in each selection construct. Each option sequence starts with a double-colon. The first statement in each sequence is called its guard. An option can be selected for execution only when its guard statement is executable. If more than one guard statement is executable, one of them will be selected non-deterministically. If none of the guards are executable, the selection construct as a whole blocks.

The selection construct as a whole is executable if and only if at least one of its guards is executable.

Examples

Using the relative values of two variables a and b to choose between two options, we can write

```plaintext
if
:: (a != b) -> ...
:: (a == b) -> ...
fi
```

This selection structure contains two option sequences, each preceded by a double colon. Only one sequence from the list will be executed. A sequence can be selected only if its guard statement is executable (the first statement). In the example the two guards are mutually exclusive, but this is not required.

The guards from a selection structure cannot be prefixed by labels individually. These guards really define the outgoing transitions of a single control state, and therefore any label on one guard is really a label on the source state for all guards belonging on the selection construct itself (cf. label L0 in the next example). It is tempting to circumvent this rule and try to label a guard by inserting a skip in front of it, for instance, as follows:

```plaintext
L0:    if
       :: skip;
L1:      (a != b) -> ...
       :: (a == b) -> ...
fi;
```

But note that this modification alters the meaning of the selection from a choice between (a != b) and (a == b), to a choice between (a != b) and true. The addition of the skip statement also adds an extra intermediate state, immediately following the skip statement itself.
init

Name

init - for declaring an initial process.

Syntax

init { sequence }

Description

The init keyword is used to declare the behavior of a process that is active in the initial system state.

An init process has no parameters, and no additional copies of the process can be created (that is, the keyword cannot be used as an argument to the run operator).

Active processes can be differentiated from each other by the value of their process instantiation number, which is available in the predefined local variable _pid. Active processes are always instantiated in the order in which they appear in the model, so that the first such process (whether it is declared as an active process or as an init process) will receive the lowest instantiation number, which is zero.

Examples

The smallest possible PROMELA model is:

\begin{verbatim}
init { skip }
\end{verbatim}

where skip is PROMELA's null statement, or perhaps more usefully

\begin{verbatim}
init { printf("hello world\n") }
\end{verbatim}

The init process is most commonly used to initialize global variables, and to instantiate other processes, through the use of the run operator, before system execution starts. Any process, not just the init process, can do so, though.

It is convention to instantiate groups of processes within atomic sequences, to make sure that their execution begins at the same instant. For instance, in the leader election example, included as a test case in the SPIN distribution, the initial process is used to start up N copies of the proctype node. Each new instance of the proctype is given different parameters, which in this case consist of two channel names and an indentifying number. The node proctype is then of the form:

\begin{verbatim}
proctype node(chan in, chan out, byte mynumber)
{
    ... 
}
\end{verbatim}

and the init process is structured as follows.
inline

Name

inline - a stylized version of a macro.

Syntax

inline name ( [ arg_lst ] ) { sequence }

Description

An inline definition must appear before its first use, and must always be defined globally, that is, at the same level as a proctype declaration. An inline definition works much like a preprocessor macro, in the sense that it just defines a replacement text for a symbolic name, possibly with parameters. It does not define a new variable scope. The body of an inline is directly pasted into the body of a proctype at each point of invocation. An invocation (an inline call) is performed with a syntax that is similar to a procedure call in C, but, like a macro, a PROMELA inline cannot return a value to the caller.

An inline call may appear anywhere a stand-alone PROMELA statement can appear. This means that, unlike a macro call, an inline call cannot appear in a parameter list of the run operator, and it cannot be used as an operand in an expression. It also cannot be used on the left- or right-hand side of an assignment statement.

The parameters to an inline definition are typically names of variables.

An inline definition may itself contain other inline calls, but it may not call itself recursively.

Examples

The following example illustrates the use of inline definitions in a version of the alternating bit protocol.

```plaintext
mtype = { msg0, msg1, ack0, ack1 };
chan sender = [1] of { mtype };
chan receiver = [1] of { mtype };
inline recv(cur_msg, cur_ack, lst_msg, lst_ack)
{   
do
:: receiver?cur_msg ->
    sender!cur_ack; break /* accept */
:: receiver?lst_msg ->
    sender!lst_ack
   od;
}
inline phase(msg, good_ack, bad_ack)
{   
do
:: sender?good_ack -> break
:: sender?bad_ack
:: timeout ->
    if
:: receiver!msg;
:: skip /* lose message */
fi;
   od
}
```

In simulations, line number references are preserved and will point to the source line inside the inline definition where possible. In some cases, in the example for instance at the start of the Sender and the Receiver process, the control point is inside the proctype body and not yet inside the inline.

Notes

The PROMELA scope rules for variables are not affected by inline definitions. If, for instance, the body of an inline contains variable declarations, their scope would be the same as if they were declared outside the inline, at the point of invocation. The scope of such variables is the entire body of the proctype in which the invocation appears. If such an inline would be invoked in two different places within the same proctype, the declaration would also appear twice, and a syntax error would result.

See Also

comments, macros
labels

Name

label - to identify a unique control state in a proctype declaration.

Syntax

name : stmt

Description

Any statement or control-flow construct can be preceded by a label. The label can, but need not, be used as a destination of a goto or can be used in a remote reference inside a never claim. Label names must be unique within the surrounding proctype, trace, notrace, or never claim declaration.

A label always prefixes a statement, and thereby uniquely identifies a control state in a transition system, that is, the source state of the transition that corresponds to the labeled statement.

Any number of labels can be attached to a single statement.

Examples

The following proctype declaration translates into a transition system with precisely three local process states: initial state S1, state S2 in between the send and the receive, and the (unreachable) final state S3, immediately following the repetition construct.

```
active proctype dijkstra()
{
  S0:
  S1: do
    :: q!p ->
  S2:     q?v
    :: true
    od
/* S3 */
}
```

The first state has two labels: S0 and S1. This state has two outgoing transitions: one corresponding to the send statement q!p, and one corresponding to the condition statement true. Observe carefully that there is no separate control state at the start of each guard in a selection or repetition construct. Both guards share the same start state S1.

Notes

A label name can be any alphanumeric character string, with the exception that the first character in the label name may not be a digit or an underscore symbol.

The guard statement in a selection or repetition construct cannot be prefixed by a label individually; see the manual page for if and do for details.

There are three types of labels with special meaning, see the manual pages named accept, end, and progress.

See Also

accept, do, end, if, goto, progress, remoterefs
len

Name

len - predefined, integer function to determine the number of messages that is stored in a buffered channel.

Syntax

len ( varref )

Description

A predefined function that takes the name of a channel as an argument and returns the number of messages that it currently holds.

Examples

#define QSZ 4
chan q = [QSZ] of { mtype, short };

len(q) > 0 /* same as nempty(q) */
len(q) == 0 /* same as empty(q) */
len(q) == QSZ /* same as full(q) */
len(q) < QSZ /* same as nfull(q) */

Notes

When possible, it is always better to use the predefined, boolean functions empty, nempty, full, and nfull, since these define special cases that can be exploited in SPIN's partial order reduction algorithm during verification.

If len is used stand-alone as a condition statement, it will block execution until the channel is non-empty.

See Also

chan, condition, empty, full, nempty, nfull, xr, xs
local

Name

local - prefix on global variable declarations to assert exclusive use by a single process.

Syntax

local typename ivar

Description

The keyword local can be used to prefix the declaration of any global variable. It persuades the partial order reduction algorithm in the model checker to treat the variable as if it were declared local to a single process, yet by being declared global it can freely be used in LTL formulae and in never claims.

The addition of this prefix can increase the effect of partial order reduction during verification, and lower verification complexity.

Examples

local byte a;
local short p[3];

Notes

If a variable marked as local is in fact accessed by more than one process, the partial order reduction may become invalid and the result of a verification incomplete. Such violations are not detected by the verifier.

See Also

_, datatypes, hidden, ltl, never, show
**ltl**

**Name**

ltl - linear time temporal logic formulae for specifying correctness requirements.

**Syntax**

Grammar:

\[ \text{ltl} ::= \text{opd} \mid ( \text{ltl} ) \mid \text{ltl binop ltl} \mid \text{unop ltl} \]

Operands (opd):

- true, false, and user-defined names starting with a lower-case letter

Unary Operators (unop):

- \[ \] (the temporal operator always )
- <> (the temporal operator eventually )
- ! (the boolean operator for negation )

Binary Operators (binop):

- \( \text{U} \) (the temporal operator strong until)
- \( \text{V} \) (the dual of \( \text{U} \)): \( (p \text{ V} q) \text{ means } !(!p \text{ U} !q) \)
- && (the boolean operator for logical and)
- || (the boolean operator for logical or)
- \( \text{A} \) (alternative form of &&)
- \( \text{V} \) (alternative form of ||)
- -> (the boolean operator for logical implication)
- <-> (the boolean operator for logical equivalence)

**Description**

SPIN can translate LTL formulae into PROMELA never claims with command line option -f. The never claim that is generated encodes the Büchi acceptance conditions from the LTL formula. Formally, any \( \omega \)-run that satisfies the LTL formula is guaranteed to correspond to an accepting run of the never claim.
macros

Name

macros and include files - preprocessing support.

Syntax

#define name token-string
#define name (arg, ..., arg) token-string
#ifdef name
#ifndef name
#if constant-expression
#else
#endif
#undef name
#include "filename"

Description

PROMELA source text is always processed by the C preprocessor, conventionally named cpp, before being parsed by SPIN. When properly compiled, SPIN has a link to the C preprocessor built-in, so that this first processing step becomes invisible to the user. If a problem arises, though, or if a different preprocessor should be used, SPIN recognizes an option -Pxxx that allows one to define a full pathname for an alternative preprocessor. The only requirement is that this preprocessor should read standard input and write its result on standard output.

Examples

#include "promela_model"
#define p       (a>b)
never { /* <>!p */
  do
    :: !p -> assert(false)
    :: else /* else ignore */
  od
}

It is always wise to put braces around the replacement text in the macro-definitions to make sure the precedence of operator evaluation is preserved when a macro name is used in a different context, for example, within a composite boolean expression.

Notes

The details of the working of the preprocessor can be system dependent. For the specifics, consult the manual pages for cpp that came with the C compiler that is installed on your system.

On PCs, if no macros with more than one parameter appear in the model, and no extra compiler directives are defined on the command line, SPIN will use a simple built-in version of the C preprocessor to bypass the call on the external program. When needed, this call can be suppressed by adding a dummy compiler directive to the command line, as in:

$ spin -DDUMMY -a model

The call could also be suppressed by adding a dummy macro definition with more than one parameter to the model itself, as in:

#define dummy (a,b)     (a+b)

The preprocessor that is used can be modified in several ways. The default preprocessor, for instance, can be set to m4 by recompiling SPIN itself with the compiler directive -DCPP=/bin/m4. The choice of preprocessor can also be changed on the command line, for instance, by invoking SPIN as:

$ spin -P/bin/m4    model

Extra definitions can be passed to the preprocessor from the command line, as in:

$ spin -E-I/usr/greg -DMAX=5 -UXAM model

which has the same effect as adding the following two definitions at the start of the model:

#define MAX     5
#undef  XAM

as well as passing the additional directive -I/usr/greg to the preprocessor, which results in the addition of directory /usr/greg to the list of directories that the preprocessor will search for include files.

See Also

comments, never
mtype

Name

mtype - for defining symbolic names of numeric constants.

Syntax

mtype \[ = \] \{ name [, name ]* \}

mtype name \[ = \text{mtype}_\text{name} \]

mtype name '\[ const '\] \[ = \text{mtype}_\text{name} \]

Description

An mtype declaration allows for the introduction of symbolic names for constant values. There can be multiple mtype declarations in a verification model. If multiple declarations are given, they are equivalent to a single mtype declaration that contains the concatenation of all separate lists of symbolic names.

If one or more mtype declarations are present, the keyword mtype can be used as a data type, to introduce variables that obtain their values from the range of symbolic names that was declared. This data type can also be used inside chan declarations, for specifying the type of message fields.

Examples

The declaration

\[
mtype = \{ \text{ack, nak, err, next, accept} \}
\]

is functionally equivalent to the sequence of macro definitions:

\[
\begin{align*}
\text{#define ack} & \quad 5 \\
\text{#define nak} & \quad 4 \\
\text{#define err} & \quad 3 \\
\text{#define next} & \quad 2 \\
\text{#define accept} & \quad 1
\end{align*}
\]

Note that the symbols are numbered in the reverse order of their definition in the mtype declarations, and that the lowest number assigned is one, not zero.

If multiple mtype declarations appear in the model, each new set of symbols is prepended to the previously defined set, which can make the final internal numbering of the symbols somewhat less predictable.

The convention is to place an assignment operator in between the keyword mtype and the list of symbolic names that follows, but this is not required.

The symbolic names are preserved in tracebacks and error reports for all data that is explicitly declared with data type mtype.
nempty

Name

nempty - predefined, boolean function to test emptiness of a channel.

Syntax

nempty ( varref)

Description

The expression nempty(q), with q a channel name, is equivalent to the expression

\[\text{len}(q) \neq 0\]

where q is a channel name. The PROMELA grammar prohibits this from being written as !empty(q).

Using nempty instead of its equivalents can preserve the validity of reductions that are applied during verifications, especially in combination with the use of xr and xs channel assertions.

Notes

Note that if predefined functions such as empty, nempty, full, and nfull are used in macro definitions used for propositional symbols in LTL formulae, they may well unintentionally appear under a negation sign, which will trigger syntax errors from SPIN.

See Also

condition, empty, full, len, ltl, nfull, xr, xs
**never**

**Name**

never - declaration of a temporal claim.

**Syntax**

never { sequence }

**Description**

A never claim can be used to define system behavior that, for whatever reason, is of special interest. It is most commonly used to specify behavior that should never happen. The claim is defined as a series of propositions, or boolean expressions, on the system state that must become true in the sequence specified for the behavior of interest to be matched.

A never claim can be used to match either finite or infinite behaviors. Finite behavior is matched if the claim can reach its final state (that is, its closing curly brace). Infinite behavior is matched if the claim permits an \( \omega \)-acceptance cycle. Never claims, therefore, can be used to verify both safety and liveness properties of a system.

Almost all PROMELA language constructs can be used inside a claim declaration. The only exceptions are those statements that can have a side effect on the system state. This means that a never claim may not contain assignment or message passing statements. Side effect free channel poll operations, and arbitrary condition statements are allowed.

Never claims can either be written by hand or they can be generated mechanically from LTL formula, see the manual page for ltl.

There is a small number of predefined variables and functions that may only be used inside never claims. They are defined in separate manual pages, named _last, enabled, np_, pc_value, and remoterefs.

**Examples**

In effect, when a never claim is present, the system and the claim execute in lockstep. That is, we can think of system execution as always consisting of a pair of transitions: one in the claim and one in the system, with the second transition coming from any one of the active processes. The claim automaton always executes first. If the claim automaton does not have any executable transitions, no further move is possible, and the search along this path stops. The search will then backtrack so that other executions can be explored.

This means that we can easily use a never claim to define a search restriction; we do not necessarily have to use the claim only for the specification of correctness properties. For example, the claim

```promela
never /* [] p */
{
    do
    :: p
    od
}
```

would restrict system behavior to those states where property p holds.

We can also use a search restriction in combination with an LTL property. To prove, for instance, that the model
nfull

Name

nfull - predefined, boolean function to test fullness of a channel.

Syntax

nfull ( varref )

Description

The expression nfull(q) is equivalent to the expression

\[(\text{len}(q) < \text{QSZ})\]

where q is a channel name, and QSZ the capacity of this channel. The PROMELA grammar prohibits the same from being written as !full(q).

Using nfull instead of its equivalents can preserve the validity of reductions that are applied during verifications, especially in combination with the use of xr and xs channel assertions.

Notes

Note that if predefined functions such as empty, nempty, full, and nfull are used in macro definitions used for propositional symbols in LTL formulae, they may well unintentionally appear under a negation sign, which will trigger syntax errors from SPIN.

See Also

condition, empty, full, len, ltl, nempty, xr, xs
**np_**

**Name**

np_ - a global, predefined, read-only boolean variable.

**Syntax**

np_

**Description**

This global predefined, read-only variable is defined to be true in all global system states that are not explicitly marked as progress states, and is false in all other states. The system is in a progress state if at least one active process is at a local control state that was marked with a user-defined progress label, or if the current global system state is marked by a progress label in an event trace definition.

The np_ variable is meant to be used exclusively inside never claims, to define system properties.

**Examples**

The following non-deterministic never claim accepts all non-progress cycles:

```plaintext
never { /*<>[] np_ */
  do
    :: true
    :: np_ -> break
  od;
accept: do
  :: np_
  od
}
```

This claim is identical to the one that the verifier generates, and automatically adds to the model, when the verifier source is compiled with the directive -DNP, as in:

```
$ cc -DNP -o pan pan.c
```

Note that the claim automaton allows for an arbitrary, finite-length prefix of the computation where either progress or non-progress states can occur. The claim automaton can move to its accepting state only when the system is in a non-progress state, and it can only stay there infinitely long if the system can indefinitely remain in non-progress states only.

**See Also**

condition, ltl, never, progress
pc_value

Name

pc_value - a predefined, integer function for use in never claims.

Syntax

pc_value ( any_expr )

Description

The call pc_value(x) returns the current control state (an integer) of the process with instantiation number x. The correspondence between the state numbers reported by pc_value and statements or line numbers in the PROMELA source can be checked with run-time option -d on the verifiers generated by SPIN, as in:

$ spin -a model.pml
$ cc -o pan pan.c
$ ./pan -d
...

The use of this function is restricted to never claims.

Examples

never {
  do
    :: pc_value(1) <= pc_value(2)
    && pc_value(2) <= pc_value(3)
    && pc_value(3) <= pc_value(4)
    && pc_value(4) <= pc_value(5)
  od
}

This claim is a flawed attempt to enforce a symmetry reduction among five processes. This particular attempt is flawed in that it does not necessarily preserve the correctness properties of the system being verified. See also the discussion in Chapter 4, p. 94.)

Notes

As the example indicates, this function is primarily supported for experimental use, and may not survive in future revisions of the language.

See Also

condition, never
pointers

Name

pointers - indirect memory addressing.

Description

There are no pointers in the basic PROMELA language, although there is a way to circumvent this restriction through the use of embedded C code.

The two main reasons for leaving pointers out of the basic language are efficiency and tractability. To make verification possible, the verifier needs to be able to track all data that are part of reachable system states. SPIN maintains all such data, that is, local process states, local and global variables, and channel contents, in a single data structure called the system "state vector." The efficiency of the SPIN verifiers is in large part due to the availability of all state data within the simple, flat state vector structure, which allows each state comparison and state copying operation to be performed with a single system call.

The performance of a SPIN verifier can be measured in the number of reachable system states per second that can be generated and analyzed. In the current system, this performance is determined exclusively by the length of the state vector: a vector twice as long requires twice as much time to verify per state, and vice versa; every reduction in the length of a state vector translates into an increase of the verifier's efficiency. The cost per state is in most cases a small constant factor times the time needed to copy the bits in the state vector from one place to another (that is, the cost of an invocation of the system routine memcpy()).

The use of data that are only accessible through pointers during verification runs requires the verifier to collect the relevant data from all memory locations that could be pointed to at any one time and copy such information into the state vector. The associated overhead immediately translates in reduced verification efficiency.

See Chapter 17 for a discussion of the indirect support for pointers through the use of embedded C code fragments.

See Also

c_code, c_decl, c_expr
poll

Name

poll - a side effect free test for the executability of a non-rendezvous receive statements.

Syntax

name ? ['recv_args ']

name ?? ['recv_args ']

Description

A channel poll operation looks just like a receive statement, but with the list of message fields enclosed in square brackets. It returns either true or false, depending on the executability of the corresponding receive (i.e., the same operation written without the square brackets). Because its evaluation is side effect free, this form can be used freely in expressions or even assignments where a standard receive operation cannot be used.

The state of the channel, and all variables used, is guaranteed not to change as a result of the evaluation of this condition statement.

Examples

In the following example we use a channel poll operation to place an additional constraint on a timeout condition:

qname?[ack, var] && timeout

Notes

Channel poll operations do not work on rendezvous channels because synchronous channels never store messages that a poll operation could refer to. Messages are always passed instantly from sender to receiver in a rendezvous handshake.

It is relatively simple to create a conditional receive operation, with the help of a channel poll operation. For instance, if we want to define an extra boolean condition P that must hold before a given receive operation may be executed, we can write simply:

atomic { P && qname?[ack, var] -> qname[ack, var] }

This is harder to do for rendezvous channels; see the manual page for cond_expr for some examples.

See Also

cond_expr, condition, eval, receive

[ Team LiB ]
printf

Name

printf - for printing text during random or guided simulation runs.

Syntax

printf ( string [, arg_lst ] )

printm ( expression )

Executability

ture

Effect

none

Description

A printf statement is similar to a skip statement in the sense that it is always executable and has no other effect on the state of the system than to change the control state of the process that executes it. A useful side effect of the statement is that it can print a string on the standard output stream during simulation runs. The PROMELA printf statement supports a subset of the options from its namesake in the programming language C. The first argument is an arbitrary string, in double quotes.

Six conversion specifications are recognized within the string. Upon printing, each subsequent conversion specification is replaced with the value of the next argument from the list that follows the string.

%c a single character,

%d a decimal value,

%e an mtype constant,

%o an unsigned octal value,

%u an unsigned integer value,

%x a hexadecimal value.

In addition, the white-space escape sequences \t (for a tab character) and \n (for a newline) are also recognized. Unlike the C version, optional width and precision fields are not supported.

The alternative form printm can be used to print just the symbolic name of an mtype constant. The two print commands in the following sequence, for instance, would both print the string pear:

```c
mtype = { apple, pear, orange };
mtype x = pear;
printf("%e", x);
printm(x);
```
priority

Name

priority - for setting a numeric simulation priority for a process.

Syntax

active [ '[' const ']' ] proctype name ([ decl_lst ] ) priority const { sequence }

run name ([ arg_lst ] ) priority const

Description

Process priorities can be used in random simulations to change the probability that specific processes are scheduled for execution.

An execution priority is specified either as an optional parameter to a run operator, or as a suffix to an active proctype declaration. The optional priority field follows the closing brace of the parameter list in a proctype declaration.

The default execution priority for a process is one. Higher numbers indicate higher priorities, in such a way that a priority ten process is ten times more likely to execute than a priority one process.

The priority specified in an active proctype declaration affects all processes that are initiated through the active prefix, but no others. A process instantiated with a run statement is always assigned the priority that is explicitly or implicitly specified there (overriding the priority that may be specified in the proctype declaration for that process).

Examples

run name(...) priority 3
active proctype name() priority 12 { sequence }

If both a priority clause and a provided clause are specified, the priority clause should appear first.

active proctype name() priority 5 provided (a<b) {...}

Notes

Priority annotations only affect random simulation runs. They have no effect during verification, or in guided and interactive simulation runs. A priority designation on a proctype declaration that contains no active prefix is ignored.

See Also

active, proctype, provided

[ Team LiB ]
probabilities

Name

probabilities - for distinguishing between high and low probability actions.

Description

There is no mechanism in PROMELA for indicating the probability of a statement execution, other than during random simulations with priority tags.

SPIN is designed to check the unconditional correctness of a system. High probability executions are easily intercepted with standard testing and debugging techniques, but only model checking techniques are able to reproducibly detect the remaining classes of errors.

Disastrous error scenarios often have a low probability of occurrence that only model checkers can catch reliably. The use of probability tags on statement executions would remove the independence of probability, which seems counter to the premise of logic model checking. Phrased differently, verification in SPIN is concerned with possible behavior, not with probable behavior. In a well-designed system, erroneous behavior should be impossible, not just improbable.

To exclude known low probability event scenarios from consideration during model checking, a variety of other techniques may be used, including the use of model restriction, LTL properties, and the use of progress-state, end-state, and accept-state labels.

See Also

if, do, priority, progress, unless
procedures

Name

procedures - for structuring a program text.

Description

There is no explicit support in the basic PROMELA language for defining procedures or functions. This restriction can be circumvented in some cases through the use of either inline primitives, or embedded C code fragments.

The reason for this restriction to the basic language is that SPIN targets the verification of process interaction and process coordination structures, and not internal process computations. Abstraction is then best done at the process and system level, not at a computational level. It is possible to approximate a procedure call mechanism with PROMELA process instantiations, but this is rarely a good idea. Consider, for instance, the following model:

```plaintext
#ifndef N
#define N 12
#endif

int f = 1;

proctype fact(int v)
{
    if
        :: v > 1  ->  f = v*f;  run fact(v-1)
        :: else
            fi

    init {
        run fact(N);
        (_nr_pr == 1)  ->
            printf("%d! = %d\n", N, f)
    }
}

init {
    run fact(N);
    (_nr_pr == 1)  ->
        printf("%d! = %d\n", N, f)
}
```

Initially, there is just one process in this system, the init process. It instantiates a process of type fact passing it the value of constant N, which is defined in a macro. If the parameter passed to the process of type fact is greater than one, the value of global integer f is multiplied by v, and another copy of fact is instantiated with a lower value of the parameter.

The procedure of course closely mimics a recursive procedure to compute the factorial of N. If we store the model in a file called badidea and execute the model, we get

```plaintext
5 spin badidea
12! = 479001600
13 processes created
```

which indeed is the correct value for the factorial. But, there are a few potential gotcha's here. First, the processes that are instantiated will execute asynchronously with the already running processes. Specifically, we cannot assume that the process that is instantiated in a run statement terminates its execution before the process that executed the run reaches its next statement. Generally, the newly created process will start executing concurrently with its creator. Nothing can be assumed about the speed of execution of a running process. If a particular order of execution is
proctype

Name

proctype - for declaring new process behavior.

Syntax

proctype name ( [ decl_lst] ) { sequence }

D_proctype name ( [ decl_lst ] ) { sequence }

Description

All process behavior must be declared before it can be instantiated. The proctype construct is used for the
declaration. Instantiation can be done either with the run operator, or with the prefix active that can be used at the
time of declaration.

Declarations for local variables and message channels may be placed anywhere inside the proctype body. In all
cases, though, these declarations are treated as if they were all placed at the start of the proctype declaration. The
scope of local variables cannot be restricted to only part of the proctype body.

The keyword D_proctype can be used to declare process behavior that is to be executed completely
deterministically. If non-determinism is nonetheless present in this type of process definition, it is resolved in
simulations in a deterministic, though otherwise undefined, manner. During verifications an error is reported if
non-determinism is encountered in a D_proctype process.

Examples

The following program declares a proctype with one local variable named state:

proctype A(mtype x) { mtype state; state = x }

The process type is named A, and has one formal parameter named x.

Notes

Within a proctype body, formal parameters are indistinguishable from local variables. Their only distinguishing feature
is that their initial values can be determined by an instantiating process, at the moment when a new copy of the
process is created.

See Also

_pid, active, init, priority, provided, remoterefs, run
**progress**

**Name**

progress - label-name prefix for specifying liveness properties.

**Syntax**

progress [a-zA-Z0-9_]* : stmnt

**Description**

A progress label is any label name that starts with the eight-character sequence progress. It can appear anywhere a label can appear.

A label always prefixes a statement, and thereby uniquely identifies a local process state (i.e., the source state of the transition that corresponds to the labeled statement). A progress label marks a state that is required to be traversed in any infinite execution sequence.

A progress label can appear in a proctype, or trace declaration, but has no special semantics when used in a never claim or in notrace declarations. Because a global system state is a composite of local component states (e.g., proctype instantiations, and an optional trace component), a progress label indirectly also marks global system states where one or more of the component systems is labeled with a progress label.

Progress labels are used to define correctness claims. A progress label states the requirement that the labeled global state must be visited infinitely often in any infinite system execution. Any violation of this requirement can be reported by the verifier as a non-progress cycle.

**Examples**

```plaintext
active proctype dijkstra()
{
    do
    :: sema!p ->
    progress: sema?v
    od
}
```

The requirement expressed here is that any infinite system execution contains infinitely many executions of the statement sema?v.

**Notes**

Progress labels are typically used to mark a state where effective progress is being made in an execution, such as a sequence number being incremented or valid data being accepted by a receiver in a data transfer protocol. They can, however, also be used during verifications to eliminate harmless variations of liveness violations. One such application, for instance, can be to mark message loss events with a pseudo progress label, to indicate that sequences that contain infinitely many message loss events are of secondary interest. If we now search for non-progress executions, we will no longer see any executions that involve infinitely many message loss events.

SPIN has a special mode to prove absence of non-progress cycles. It does so with the predefined LTL formula:
**provided**

**Name**

provided - for setting a global constraint on process execution.

**Syntax**

```plaintext
proctype name ([ decl_lst ]) provided ( expr ) { sequence }
```

**Description**

Any proctype declaration can be suffixed by an optional provided clause to constrain its execution to those global system states for which the corresponding expression evaluates to true. The provided clause has the effect of labeling all statements in the proctype declaration with an additional, user-defined executability constraint.

**Examples**

The declaration:

```plaintext
byte a, b;
active proctype A() provided (a > b)
{
    ...
}
```

makes the execution of all instances of proctype A conditional on the truth of the expression \(a > b\), which is, for instance, not true in the initial system state. The expression can contain global references, or references to the process's `_pid`, but no references to any local variables or parameters.

If both a priority clause and a provided clause are specified, the priority clause should come first.

```plaintext
active proctype name() priority 2 provided (a > b )
{
    ...
}
```

**Notes**

Provided clauses are incompatible with partial order reduction. They can be useful during random simulations, or in rare cases to control and reduce the complexity of verifications.

**See Also**

`_pid`, active, hidden, priority, proctype
**rand**

**Name**

rand - for random number generation.

**Description**

There is no predefined random number generation function in PROMELA. The reason is that during a verification we effectively check for all possible executions of a system. Having even a single occurrence of a call on the random number generator would increase the number of cases to inspect by the full range of the random numbers that could be generated: usually a huge number. Random number generators can be useful on a simulation, but they can be disastrous when allowed in verification.

In almost all cases, PROMELA's notion of non-determinism can replace the need for a random number generator. Note that to make a random choice between N alternatives, it suffices to place these N alternatives in a selection structure with N options. The verifier will interpret the non-determinism accurately, and is not bound to the restrictions of a pseudo-random number generation algorithm.

During random simulations, SPIN will internally make calls on a (pseudo) random number generator to resolve all cases of non-determinism. During verifications no such calls are made, because effectively all options for behavior will be explored in this mode, one at a time.

PROMELA's equivalent of a "random number generator" is the following program:

```c
active proctype randnr()
{
   /*
   * don't call this rand()...
   * to avoid a clash with the C library routine
   */
   byte nr; /* pick random value */
   do
      :: nr++ /* randomly increment */
      :: nr-- /* or decrement */
      :: break /* or stop */
   do;
   printf("nr: %d\n") /* nr: 0..255 */
}
```

Note that the verifier would generate at least 256 distinct reachable states for this model. The simulator, on the other hand, would traverse the model only once, but it could execute a sequence of any length (from one to infinitely many execution steps). A simulation run will only terminate if the simulator eventually selects the break option (which is guaranteed only in a statistical sense).

**Notes**

Through the use of embedded C code, a user can surreptitiously include calls on an external C library rand() function into a model. To avoid problems with irreproducible behavior, the SPIN-generated verifiers intercept such calls and redefine them in such a way that the depth-first search process at the very least remains deterministic. SPIN accomplishes this by pre-allocating an integer array of the maximum search depth maxdepth, and filling that array with the first maxdepth random numbers that are generated. Those numbers are then reused each time the search returns to a previously visited point in the search, to secure the sanity of the search process.

The seed for this pre-computation of random numbers is fixed, so that subsequent runs will always give the same result, and to allow for the faithful replay of error scenarios. Even though this provides some safeguards, the use of random number generation is best avoided, also in embedded C code.

**See Also**
c_code, c_expr, if, do
real-time

Name

real time - for relating properties to real-time bounds.

Description

In the basic PROMELA language there is no mechanism for expressing properties of clocks or of time related properties or events. There are good algorithms for integrating real-time constraints into the model checking process, but most attention has so far been given to real-time verification problems in hardware circuit design, rather than the real-time verification of asynchronous software, which is the domain of the SPIN model checker.

The best known of these algorithms incur significant performance penalties compared with untimed verification. Each clock variable added to a model can increase the time and memory requirements of verification by an order of magnitude. Considering that one needs at least two or three such clock variables to define meaningful constraints, this seems to imply, for the time being, that a real-time capability requires at least three to four orders of magnitude more time and memory than the verification of the same system without time constraints.

The good news is that if a correctness property can be proven for an untimed PROMELA model, it is guaranteed to preserve its correctness under all possible real-time constraints. The result is therefore robust, it can be obtained efficiently, and it encourages good design practice. In concurrent software design it is usually unwise to link logical correctness with real-time performance.

PROMELA is a language for specifying systems of asynchronous processes. For the definition of such a system we abstract from the behavior of the process scheduler and from any assumption about the relative speed of execution of the various processes. These assumptions are safe, and the minimal assumptions required to allow us to construct proofs of correctness. The assumptions differ fundamentally from those that can be made for hardware systems, which are often driven by a single known clock, with relative speeds of execution precisely known. What often is just and safe in hardware verification is, therefore, not necessarily just and safe in software verification.

SPIN guarantees that all verification results remain valid independent of where and how processes are executed, timeshared on a single CPU, in true concurrency on a multiprocessor, or with different processes running on CPUs of different makes and varying speeds. Two points are worth considering in this context: first, such a guarantee can no longer be given if real-time constraints are introduced, and secondly, most of the existing real-time verification methods assume a true concurrency model, which inadvertently excludes the more common method of concurrent process execution by timesharing.

It can be hard to define realistic time bounds for an abstract software system. Typically, little can be firmly known about the real-time performance of an implementation. It is generally unwise to rely on speculative information, when attempting to establish a system's critical correctness properties.

See Also

priorities, probabilities
receive

Name

receive statement - for receiving messages from channels.

Syntax

name ? recv_args
name ?? recv_args
name ?< recv_args >
name ??< recv_args >

Executability

The first and the third form of the statement, written with a single question mark, are executable if the first message in
the channel matches the pattern from the receive statement.

The second and fourth form of the statement, written with a double question mark, are executable if there exists at
least one message anywhere in the channel that matches the pattern from the receive statement. The first such message
is then used.

A match of a message is obtained if all message fields that contain constant values in the receive statement equal the
values of the corresponding message fields in the message.

Effect

If a variable appears in the list of arguments to the receive statement, the value from the corresponding field in the
message that is matched is copied into that variable upon reception of the message. If no angle brackets are used, the
message is removed from the channel buffer after the values are copied. If angle brackets are used, the message is not
removed and remains in the channel.

Description

The number of message fields that is specified in the receive statement must always match the number of fields that is
declared in the channel declaration for the channel addressed. The types of the variables used in the message fields
must be compatible with the corresponding fields from the channel declaration. For integer data types, an equal or
larger value range for the variable is considered to be compatible (e.g., a byte field may be received in a short
variable, etc.). Message fields that were declared to contain a user-defined data type or a chan must always match
precisely.

The first form of the receive statement is most commonly used. The remaining forms serve only special purposes, and
can only be used on buffered message channels.

The second form of the receive statement, written with two question marks, is called a random receive statement.
The variants with angle brackets have no special name.

Because all four types of receive statements discussed here can have side effects, they cannot be used inside
expressions (see the manual page poll for some alternatives).

Examples
remoterefs

Name

remote references - a mechanism for testing the local control state of an active process, or the value of a local variable in an active process from within a never claim.

Syntax

name ['[ ' any_expr ' ]'] @labelname

name ['[ ' any_expr ' ]'] : varname

Description

The remote reference operators take either two or three arguments: the first, required, argument is the name of a previously declared proctype, a second, optional, argument is an expression enclosed in square brackets, which provides the process instantiation number of an active process. With the first form of remote reference, the third argument is the name of a control-flow label that must exist within the named proctype. With the second form, the third argument is the name of a local variable from the named proctype.

The second argument can be omitted, together with the square brackets, if there is known to be only one instantiated process of the type that is named.

A remote reference expression returns a non-zero value if and only if the process referred to is currently in the local control state that was marked by the label name given.

Examples

active proctype main () { byte x;
  L: (x < 3) ->
      x++
}
never { /* process main cannot remain at L forever */
  accept: do
    :: main@L
  od
}

Notes

Because init, never, trace, and notrace are not valid proctype names but keywords, it is not possible to refer to the state of these special processes with a remote reference:

init@label    /* invalid */
never[0]@label /* invalid */

Note that the use of init, can always be avoided, by replacing it with an active proctype.

A remote variable reference, the second form of a remote reference, bypasses the standard scope rules of PROMELA by making it possible for the never claim to refer to the current value of local variables inside a running process.

For instance, if we wanted to refer to the variable count in the process of type Dijkstra in the example on page 77, we could do so with the syntax Dijkstra[0] : count, or if there is only one such process, we can use the shorter form Dijkstra : count.

The use of remote variable references is not compatible with SPIN’s partial order reduction strategy. A wiser strategy is therefore usually to turn local variables whose values are relevant to a global correctness property into global variables, so that they can be referenced as such. See especially the manual page for hidden for an efficient way of doing this that preserves the benefits of partial order reduction.

See Also

_pid, active, condition, hidden, proctype, run
run

Name
run - predefined, unary operator for creating new processes.

Syntax
run name ([ arg_lst ])

Description
The run operator takes as arguments the name of a previously declared proctype, and a possibly empty list of actual parameters that must match the number and types of the formal parameters of that proctype. The operator returns zero if the maximum number of processes is already running, otherwise it returns the process instantiation number of a new process that is created. The new process executes asynchronously with the existing active processes from this point on. When the run operator completes, the new process need not have executed any statements.

The run operator must pass actual parameter values to the new process, if the proctype declaration specified a non-empty formal parameter list. Only message channels and instances of the basic data types can be passed as parameters. Arrays of variables cannot be passed.

Run can be used in any process to spawn new processes, not just in the initial process. An active process need not disappear from the system immediately when it terminates (i.e., reaches the end of the body of its process type declaration). It can only truly disappear if all younger processes have terminated first. That is, processes can only disappear from the system in reverse order of their creation.

Examples
proctype A(byte state; short set)
{  
  (state == 1) -> state = set  
}
init {
  run A(1, 3)
}

Notes
Because PROMELA defines finite state systems, the number of processes and message channels is required to be bounded. SPIN limits the number of active processes to 255.

Because run is an operator, run A() is an expression that can be embedded in other expressions. It is the only operator allowed inside expressions that can have a side effect, and therefore there are some special restrictions that are imposed on expressions that contain run operators.

Note, for instance, that if the condition statement

(run A() && run B())
**scanf**

**Name**

`scanf` - to read input from the standard input stream.

**Description**

There is no routine in PROMELA comparable to the C library function `scanf` to read input from the standard input stream or from a file or device. The reason is that PROMELA models must be closed to be verifiable. That is, all input sources must be part of the model. It is relatively easy to build a little process that acts as if it were the `scanf` routine, and that sends to user processes that request its services a non-deterministically chosen response from the set of anticipated responses.

As a small compromise, PROMELA does include a special predefined channel named `STDIN` that can be used to read characters from the standard input during simulation experiments. The use of `STDIN` is not supported in verification runs.

**See Also**

c_code, `printf`, `STDIN`
**send**

**Name**

send statement - for sending messages to channels.

**Syntax**

name ! send_args

ame !! send_args

**Executability**

A send statement on a buffered channel is executable in every global system state where the target channel is non-full. SPIN supports a mechanism to override this default with option -m. When this option is used, a send statement on a buffered channel is always executable, and the message is lost if the target channel is full.

The execution of a send statement on a rendezvous channel consists, conceptually, of two steps: a rendezvous offer and a rendezvous accept. The rendezvous offer can be made at any time (see Chapter 7). The offer can be accepted only if another active process can perform the matching receive operation immediately (i.e., with no intervening steps by any process). The rendezvous send operation can only take place if the offer made is accepted by a matching receive operation in another process.

**Effect**

For buffered channels, assuming no message loss occurs (see above), the message is added to the channel. In the first form of the send statement, with a single exclamation mark, the message is appended to the tail of the channel, maintaining fifo (first in, first out) order. In the second form, with a double exclamation mark, the message is inserted into the channel immediately ahead of the first message in the channel that succeeds it in numerical order. To determine the numerical order, all message fields are significant.

Within the semantics model, the effect of issuing the rendezvous offer is to set global system variable handshake to the channel identity of the target channel (see Chapter 7).

**Description**

The number of message fields that is specified in the send statement must always match the number of fields that is declared in the channel declaration for the target channel, and the values of the expressions specified in the message fields must be compatible with the datatype that was declared for the corresponding field. If the type of a message field is either a user-defined type or chan, then the types must match precisely.

The first form of the send statement is the standard fifo send. The second form, with the double exclamation mark, is called a sorted send operation. The sorted send operation can be exploited by, for instance, listing an appropriate message field (e.g., a sequence number) as the first field of each message, thus forcing a message ordering in the target channel.

**Examples**

In the following example our test process uses sorted send operations to send three messages into a buffered channel named x. Then it adds one more message with the value four.

```plaintext
chan x = [4] of { short };
```
separators

Name

Separators - for sequential composition of statements and declarations.

Syntax

step ; step
step -> step

Description

The semicolon and the arrow are equivalent statement separators in PROMELA; they are not statement terminators, although the parser has been taught to be forgiving for occasional lapses. The last statement in a sequence need not be followed by a statement separator, unlike, for instance, in the C programming language.

Examples

```plaintext
x = 3;
atomic {
    x = y;
    y = x  /* no separator is required here */
};        /* but it is required here... */
y = 3
```

Notes

The convention is to reserve the use of the arrow separator to follow condition statements, such as guards in selection or repetition structures. The arrow symbol can thus be used to visually identify those points in the code where execution could block.

See Also

break, labels, goto
sequence

Name

sequence - curly braces, used to enclose a block of code.

Syntax

{ sequence }

Description

Any sequence of PROMELA statements may be enclosed in curly braces and treated syntactically as if it were a statement. This facility is most useful for defining unless constructs, but can also generally be used to structure a model.

Examples

if
:: a < b -> { tmp = a; a = b; b = a }
:: else ->
    { printf("unexpected case\n");
      assert(false)
    }
fi

The more common use is for structuring unless statements, as in:

( tmp = a; a = b; b = a; )
unless
(a >= b )

Note the differences between these two examples. In the first example, the value of the expression a < b is checked once, just before the bracketed sequence is executed. In the second example, the value of the negated expression is checked before each statement execution in the main sequence, and execution is interrupted when that expression becomes true.

Notes

The last statement in a sequence need not be followed by a statement separator, but if the sequence is followed by another statement, the sequence as a whole should be separated from that next statement with a statement separator.

See Also

atomic, d_step, unless
show

Name

show - to allow for tracking of the access to specific variables in message sequence charts.

Syntax

show typename name

Description

This keyword has no semantic content. It only serves to determine which variables should be tracked and included in message sequence chart displays in the XSPIN tool. Updates of the value of all variables that are declared with this prefix are maintained visually, in a separate process line, in these message sequence charts.

Notes

The use of this prefix only affects the information that XSPIN includes in message sequence charts, and the information that SPIN includes in Postscript versions of message sequence charts under SPIN option -M.

See Also

datatypes, hidden, local, show
skip

Name

skip - shorthand for a dummy, nil statement.

Syntax

skip

Description

The keyword skip is a meta term that is translated by the SPIN lexical analyzer into the constant value one (1), just like the predefined boolean constant true. The intended use of the shorthand is stand-alone, as a dummy statement. When used as a statement, the skip is interpreted as a special case of a condition statement. This condition statement is always executable, and has no effect when executed, other than a possible change of the control-state of the executing process.

There are few cases where a skip statement is needed to satisfy syntax requirements. A common use is to make it possible to place a label at the end of a statement sequence, to allow for a goto jump to that point. Because only statements can be prefixed by a label, we must use a dummy skip statement as a placeholder in those cases.

Examples

proctype A()
{
 L0:   if
      :: cond1 -> goto L1 /* jump to end */
      :: else -> skip     /* skip redundant */
   fi;
   ...

 L1:   skip
}

The skip statement that follows label L1 is required in this example. The use of the skip statement following the else guard in the selection structure above is redundant. The above selection can be written more tersely as:

L0:   if
      :: cond1 -> goto L1
      :: else
      fi;

Because PROMELA is an asynchronous language, the skip is never needed, nor effective, to introduce delay in process executions. In PROMELA, by definition, there can always be an arbitrary, and unknowable, delay between any two subsequent statement executions in a proctype body. This semantics correspond to the golden rule of concurrent systems design that forbids assumptions about the relative execution speed of asynchronous processes in a concurrent system. When SPIN's weak fairness constraint is enforced we can tighten this semantics a little, to conform to, what is known as, Dijkstra's finite progress assumption. In this case, when control reaches a statement, and that statement is and remains executable, we can are allowed to assume that the statement will be executed within a finite period of time (i.e., we can exclude the case where the delay would be infinite).

Notes

The opposite of skip is the zero condition statement (0), which is never executable. In cases where such a blocking statement might be needed, often an assertion statement is more effective. Note that assert(false) and assert(0) are equivalent. Similarly, assert(true) and assert(1) are equivalent and indistinguishable from both assert(skip) and skip.

Because skip is intercepted in the lexical analyzer as a meta term, it does not appear literally in error traces. It will only show up as its numeric equivalent (1).

See Also

assert, condition, else, false, true
**STDIN**

**Name**

STDIN - predefined read-only channel, for use in simulation.

**Syntax**

```
chan STDIN; STDIN?var
```

**Description**

During simulation runs, it is sometimes useful to be able to connect SPIN to other programs that can produce useful input, or directly to the standard input stream to read input from the terminal or from a file.

**Examples**

A sample use of this feature is this model of a word count program:

```plaintext
chan STDIN; /* no channel initialization */

init {
  int c, nl, nw, nc;
  bool inword = false;
  do
    :: STDIN?c ->
      if
        :: c == -1 -> break /* EOF */
        :: c == '\n' -> nc++; nl++
        :: else -> nc++
      fi;
      if
        :: c == ' ' || c == '\t' || c == '\n' ->
          inword = false
        :: else ->
          if
            :: !inword ->
              nw++; inword = true
            :: else /* do nothing */
          fi
      fi
    od;
  printf("%d\t%d\t%d\n", nl, nw, nc)
}
```

**Notes**

The STDIN channel can be used only in simulations. The name has no special meaning in verification. A verification for the example model would report an attempt to receive data from an uninitialized channel.

**See Also**

chan, poll, printf, receive
timeout

Name

timeout - a predefined, global, read-only, boolean variable.

Syntax

timeout

Description

Timeout is a predefined, global, read-only, boolean variable that is true in all global system states where no statement is executable in any active process, and otherwise is false (see also Chapter 7).

A timeout used as a guard in a selection or repetition construct provides an escape from a system hang state. It allows a process to abort waiting for a condition that can no longer become true.

Examples

The first example shows how timeout can be used to implement a watchdog process that sends a reset message to a channel named guard each time the system enters a hang state.

```active proctype watchdog()
{       do
    :: timeout -> guard!reset
    od
}
```

A more traditional use is to place a timeout as an alternative to a potentially blocking statement, to guard against a system deadlock if the statement becomes permanently blocked.

```do
:: q?message -> ...
:: timeout -> break
od```

Notes

The timeout statement can not specify a timeout interval. Timeouts are used to model only possible system behaviors, not detailed real-time behavior. To model premature expiration of timers, consider replacing the timeout variable with the constant value true, for instance, as in:

```#define timeout true```

A timeout can be combined with other expressions to form more complex wait conditions, but can not be combined with else. Note that timeout, if used as a condition statement, can be considered to be a system level else statement.
trace

Name

trace, notrace - for defining event sequences as properties.

Syntax

trace { sequence }

notrace { sequence }

Description

Much like a never claim declaration, a trace or notrace declaration does not specify new behavior, but instead states a correctness requirement on existing behavior in the remainder of the system. All channel names referenced in a trace or notrace declaration must be globally declared message channels, and all message fields must either be globally known (possibly symbolic) constants, or the predefined global variable _, which can be used in this context to specify don't care conditions. The structure and place of a trace event declaration within a PROMELA model is similar to that of a never claim: it must be declared globally.

An event trace declaration defines a correctness claim with the following properties:

- Each channel name that is used in an event trace declaration is monitored for compliance with the structure and context of the trace declaration.

- If only send operations on a channel appear in the trace, then only send operations on that channel are subject to the check. The same is true for receive operations. If both types appear, both are subject to the check, and they must occur in the relative order that the trace declaration gives.

- An event trace declaration may contain only send and receive operations (that is, events), but it can contain any control flow construct. This means that no global or local variables can be declared or referred to. This excludes the use of assignments and conditions. Send and receive operations are restricted to simple sends or receives; they cannot be variations such as random receive, sorted send, receive test, etc.

- Message fields that must be matched in sends or receives must be specified either with the help of symbolic mtype names, or with constants. Message fields that have don't care values can be matched with the predefined write-only variable _ (underscore).

- Sends and receives that appear in an event trace are called monitored events. These events do not generate new behavior, but they are required to match send or receive events on the same channels in the model with matching message parameters. A send or receive event occurs whenever a send or a receive statement is executed, that is, an event occurs during a state transition.

- An event trace can capture the occurrence of receive events on rendezvous channels.

- An event trace causes a correctness violation if a send or receive action is executed in the system that is within the scope of the event trace, but that cannot be matched by a monitored event within that declaration.
true

Name

ture - predefined boolean constant.

Syntax

ture

Description

The keyword true is a synonym of the constant value one (1), and can be used in any context. Because of the mapping to (1), true is also a synonym of skip. It supports a more natural syntax for manipulating boolean values.

Notes

Because it is intercepted in the lexical analyzer as a meta term, true is always replaced by its numeric equivalent in error traces.

Semantically, true, skip, and (1) are indistinguishable. Which term is best used depends on context and convention.

See

ccondition, false, skip
typedef

Name

typedef - to declare a user-defined structured data type.

Syntax

typedef name { decl_lst }

Description

Typedef declarations can be used to introduce user-defined data types. User-defined types can be used anywhere predefined integer data types can be used. Specifically, they can be used as formal and actual parameters for proctype declarations and instantiations, as fields in message channels, and as arguments in message send and receive statements.

A typedef declaration can refer to other, previously declared typedef structures, but it may not be self-referential. A typedef definition must always be global, but it can be used to declare both local and global data objects of the new type.

Examples

The first example shows how to declare a two-dimensional array of elements of type byte with a typedef.

typedef array { /* typedefs must be global */
   byte aa[4]
};

init {
   array a[8]; /* 8x4 = 32 bytes total */
}

The following example introduces two user-defined types named D and Msg, and declares an array of two objects of type Msg, named top:

typedef D {
   short f;
   byte g
};
typedef Msg {
   byte a[3];
   int fld1;
   D   fld2;
   chan p[3];
   bit b
};
Msg top[2];

The elements of top can be referenced as, for instance:

top[1].fld2.g = top[0].a[2]

Objects of type Msg can be passed through a channel, provided that they do not contain any field of type unsigned.

chan q = [2] of { Msg };
qu!top[0]; qu?top[1]

If we delete the arrays from the declaration of type Msg we can also use objects of this type in a run parameter, for instance, as follows:

typedef D {
   short f;
   byte g
};
typedef Msg {
   int fld1;
   D   fld2;
   bit b
};
Msg top[2];
proctype boo(Msg m)
{
   printf("fld1=%d
", m.fld1);
}
init {
   chan q = [2] of { Msg };
top[0].fld1 = 12;
qu!top[0]; qu?top[1];
run boo(top[1])
}

Notes

The current SPIN implementation imposes the following restrictions on the use of typedef objects. It is not possible to assign the value of a complete typedef object directly to another such object of the same type in a single assignment. A typedef object may be sent through a message channel as a unit provided that it contains no fields of type unsigned. A typedef object can also be used as a parameter in a run statement, but in this case it may not contain arrays.

Beware that the use of this keyword differs from its namesake in the C programming language. The working of the C version of a typedef statement is best approximated with a macro definition.

See Also

arrays, datatypes, macros, mtype
**unless**

**Name**

unless - to define exception handling routines.

**Syntax**

`stmt unless stmt`

**Description**

Similar to the repetition and selection constructs, the unless construct is not really a statement, but a method to define the structure of the underlying automaton and to distinguish between higher and lower priority of transitions within a single process. The construct can appear anywhere a basic PROMELA statement can appear.

The first statement, generally defined as a block or sequence of basic statements, is called the main sequence. The second statement is called the escape sequence. The guard of either sequence can be either a single statement, or it can be an if, do, or lower level unless construct with multiple guards and options for execution.

The executability of all basic statements in the main sequence is constrained to the non-executability of all guard statements of the escape sequence. If and when one of the guard statements of the escape sequence becomes executable, execution proceeds with the remainder of the escape sequence and does not return to the main sequence. If all guards of the escape sequence remain unexecutable throughout the execution of the main sequence, the escape sequence as a whole is skipped.

The effect of the escape sequence is distributed to all the basic statements inside the main sequence, including those that are contained inside atomic sequences. If a `d_step` sequence is included, though, the escape affects only its guard statement (that is, the first statement) of the sequence, and not the remaining statements inside the `d_step`. A `d_step` is always equivalent to a single statement that can only be executed in its entirety from start to finish.

As noted, the guard statement of an unless construct can itself be a selection or a repetition construct, allowing for a non-deterministic selection of a specific executable escape. Following the semantics model from Chapter 7, the guard statements of an escape sequence are assigned a higher priority than the basic statements from the main sequence.

Unless constructs may be nested. In that case, the guard statements from each unless statement take higher priority than those from the statements that are enclosed. This priority rule can be reversed, giving the highest priority to the most deeply nested unless escapes, by using SPIN run-time option `-J`. This option is called `-J` because it enforces a priority rule that matches the evaluation order of nested catch statements in Java programs.

PROMELA unless statements are meant to facilitate the modeling of error handling methods in implementation level languages.

**Examples**

Consider the following unless statement:

```
{ B1; B2; B3 } unless { C1; C2 }
```

where the parts inside the curly braces are arbitrary PROMELA fragments. Execution of this unless statement begins with the execution of B1. Before each statement execution in the sequence B1;B2;B3, the executability of the first statement, or guard, of fragment C1 is checked using the normal PROMELA semantics of executability. Execution of
XR

Name

xr, xs - for defining channel assertions.

Syntax

xr name [, name ] *
xs name [, name ] *

Description

Channel assertions such as

xr q1;
xs q2;

can only appear within a proctype declaration. The channel assertions are only valid if there can be at most one single instantiation of the proctype in which they appear.

The first type of assertion, xr, states that the executing process has exclusive read-access to the channel that is specified. That is, it is asserted to be the only process in the system (determined by its process instantiation number) that can receive messages from the channel.

The second type of assertion, xs, states that the process has exclusive write-access to the channel that is specified. That is, it is asserted to be the only process that can send messages to the channel.

Channel assertions have no effect in simulation runs. With the information that is provided in channel assertions, the partial order reduction algorithm that is normally used during verification, though, can optimize the search and achieve significantly greater reductions.

Any test on the contents or length of a channel referenced in a channel assertion, including receive poll operations, counts as both a read and a write access of that channel. If such access conflicts with a channel assertion, it is flagged as an error during the verification. If the error is reported, this means that the additional reductions that were applied may be invalid.

The only channel poll operations that are consistent with the use of channel assertions are nempty and nfull. Their predefined negations empty and full have no similar benefit, but are included for symmetry. The grammar prevents circumvention of the type rules by attempting constructions such as !nempty(q), or !full(q).

Summarizing: If a channel-name appears in an xs(xr) channel assertion, messages may be sent to (received from) the corresponding channel by only the process that contains the assertion, and that process can only use send (receive) operations, or one of the predefined operators nempty or nfull. All other types of access will generate run-time errors from the verifier.

Examples

chan q = [2] of { byte };
chan r = [2] of { byte };
active proctype S()
{       xs q;
xr r;
do
:: q!12
:: r?0 -> break
od
}
active proctype R()
{
xr q;
xs r;
do
:: q?12
:: r!0 -> break
od
}
Chapter 17. Embedded C Code

"The purpose of analysis is not to compel belief but rather to suggest doubt."

—(Imre Lakatos, Proofs and Refutations)

SPIN, versions 4.0 and later, support the inclusion of embedded C code into PROMELA models through the following five new primitives:

c_expr, c_code, c_decl, c_state, c_track

The purpose of these new primitives is primarily to provide support for automatic model extraction from C code. This means that it is not the intent of these extensions to be used in manually constructed models. The primitives provide a powerful extension, opening SPIN models to the full power of, and all the dangers of, arbitrary C code. The contents of the embedded code fragments cannot be checked by SPIN, neither in the parsing phase nor in the verification phase. They are trusted blindly and copied through from the text of the model into the code of the verifier that SPIN generates. In particular, if a piece of embedded C code contains an illegal operation, like a divide by zero operation or a nil-pointer dereference, the result can be a crash of the verifier while it performs the model checking. Later in this chapter we will provide some guidance on locating the precise cause of such errors if you accidentally run into them.

The verifiers that are generated by SPIN version 4.0 and higher use the embedded code fragments to define state transitions as part of a PROMELA model. As far as SPIN is concerned, a c_code statement is an uninterpreted state transformer, defined in an external language, and a c_expr statement is a user-defined boolean guard, similarly defined in an external language. Since this "external" language (C) cannot be interpreted by SPIN itself, simulation runs now have to be performed in a different way, as we will discuss. All verifications can be performed as before, though, with the standard C compiler providing the required interpretation of all embedded code.

The primitives c_decl and c_state deal with various ways of declaring data types and data objects in C that either become part of the state vector, or that are deliberately hidden from it. The c_track primitive is used to instrument the code of the verifier to track the value of data objects holding state information that are declared elsewhere, perhaps even in in separately compiled code that is linked with the SPIN-generated verifier.

Because the SPIN parser does not attempt to interpret embedded C code fragments, random and guided simulation can no longer be done directly by SPIN itself. To account for this, the SPIN-generated verifiers are now provided with their own built-in error trail playback capability if the presence of embedded C code is detected.
An Example

We will illustrate the use of these features with the example shown in Figure 17.1. The c_decl primitive introduces a new data type named Coord. To avoid name clashes, the new data type name should not match any of the existing type names that are already used inside the SPIN-generated verifiers. The C compiler will complain if this accidentally happens; SPIN itself cannot detect these conflicts.

Figure 17.1 Example of Embedded C Code

```c
// Example of embedded C code

// Typedef for the Coord data type
typedef struct Coord {
    int x, y;
} Coord;

c_state "Coord pt" "Global" /* goes inside state vector */

int z = 3;               /* standard global declaration */

active proctype example()
{
    c_code { now.pt.x = now.pt.y = 0; };

    do
        :: c_expr { now.pt.x == now.pt.y } ->
            c_code { now.pt.y++; };
        :: else ->
            break
    od;

c_code {
    printf("values %d: %d, %d,%d\n", 
        Pexample->_pid, now.z, now.pt.x, now.pt.y);
}

assert(false)        /* trigger an error trail */
}
```

Because the new data type name may need to be referenced in other statements, we must secure that its definition is placed high up in the generated code for the verifiers. The c_decl statement accomplishes precisely that. The c_decl statement, then, is only meant to be used for the definition of new C data types, that may be referred to elsewhere in the model.

The c_state primitive introduces a new global data object pt of type Coord into the state vector. The object is initialized to zero.

There is only one active process in this model. It reinitializes the global variable pt to zero (in this case this is redundant), and then executes a loop. The loop continues until the elements of structure pt differ, which will, of course, happen after a single iteration. When the loop terminates, the elements of the C data object pt are printed. To make sure an error trail is generated, the next statement is a false assertion.

Arbitrary C syntax can be used in any c_code and c_expr statement. The difference between these two types of statements is that a c_code statement is always executed unconditionally and atomically, while a c_expr statement can only be executed (passed) if it returns non-zero when its body is evaluated as a C expression. If the evaluation returns zero, execution is blocked. The evaluation of a c_expr is again indivisible (i.e., atomic). Because SPIN may have to evaluate c_expr statements repeatedly until one of them becomes executable, a c_expr is required to be free from side effects: it may only evaluate data, not modify it.
Data References

A global data object that is declared with the normal PROMELA declaration syntax in the model (i.e., not with the help of c_code or c_state) can be referenced from within c_code and c_expr statements, but the reference has to be prefixed in this case with the string now followed by a period. In the example, for instance, the global z can be referenced within a c_code or c_expr statement as now.z. (The name now refers to the internal state vector, where all global data is stored during verification.) Outside embedded C code fragments, the same variable can be referenced simply as z.

A process local data object can also be referenced from within c_code and c_expr statements within the same process (i.e., if the object is declared within the current scope), but the syntax is different. The extended syntax again adds a special prefix that locates the data object in the state vector. The prefix starts with an uppercase letter P which is followed by the name of the proctype in which the reference occurs, followed by the pointer arrow. For the data objects declared locally in proctype example, for instance, the prefix to be used is Pexample->.

In the example, this is illustrated by the reference to the predefined local variable _pid from within the c_code statement as Pexample->_pid.

The _pid variable of the process can be referenced, within the init process itself, as Pinit->_pid.

Another way to write this particular model is shown in Figure 17.2. In this version we have avoided the need for the prefixes on the variable names, by making use of the c_track primitive. The differences with the version in Figure 17.1 are small, but important.

Figure 17.2 Replacing c_state with c_track Primitives

```
c_decl {
    typedef struct Coord {
        int x, y;
    } Coord;
}

c_code { Coord pt; } /* embedded declaration */
c_track "&pt" "sizeof(Coord)" /* track value of pt */

int z = 3; /* standard global declaration */

active proctype example() {
    c_code { pt.x = pt.y = 0; } /* no 'now.' prefixes */
    do :: c_expr { pt.x == pt.y } ->
        c_code { pt.y++; }
    :: else ->
        break
    od;
}

    c_code {
        printf("values %d: %d, %d,%d\n",
            Pexample->_pid, now.z, pt.x, pt.y);
    }
    assert(false) /* trigger an error trail */
}
```

We have declared the variable pt in a global c_code statement, which means that it gets included this time as a regular global variable that remains outside the state vector. Since this object holds state information, we add a c_track statement, specifying a pointer to the object and its size. SPIN will now arrange for the value of the object to be copied into (or out of) a specially reserved part of the state vector on each step. This is obviously less efficient than the method using c_state, but it avoids the need for the sometimes clumsy now. prefixes that are required for references to variables that are placed directly into the state vector. Note that the reference to a variable in the c_code

Execution

When a PROMELA model contains embedded C code, SPIN cannot simulate its execution in the normal way because it cannot directly interpret the embedded code fragments. If we try to run a simulation anyway, SPIN will make a best effort to comply, but it will only print the text of the c_expr and c_code fragments that it encounters, without actually executing them.

To faithfully execute all embedded C code fragments, we must first generate the pan.chmbt files and compile them. We now rely on the standard C compiler to interpret the contents of all embedded code as part of the normal compilation process. For the first example, we proceed as follows:

```
$ spin -a example
$ cc -o pan pan.c       # compile
$ ./pan                 # and run
values 0: 3, 0,1
pan: error: assertion violated 0 (at depth 5)
pan: wrote coord.trail
```

The assertion violation was reported, as expected, but note that the embedded printf statement was also executed, which shows that it works differently from a PROMELA print statement. We can get around this by calling an internal SPIN routine named Printf instead of the standard library routine printf within embedded c_code fragments. This causes the verifier to enable the execution of the print statement only when reproducing an error trail, but not during the verification process itself.

The counterexample is stored in a trail file as usual, but SPIN itself cannot interpret the trail file completely because of the embedded C code statements that it contains. If we try anyway, SPIN produces something like this, printing out the embedded fragments of code without actually executing them:

```
$ spin -t -p example
  c_code2: { now.pt.x = now.pt.y = 0; }
    1: proc 0 (example) line 11 ... (state 1) [{c_code2}]
  c_code3: now.pt.x == now.pt.y
    2: proc 0 (example) line 14 ... (state 2) [{c_code3}]
  c_code4: { now.pt.y++; }
    3: proc 0 (example) line 15 ... (state 3) [{c_code4}]
    4: proc 0 (example) line 16 ... (state 4) [else]
  c_code5: { printf("values %d: %d %d,%d\n", \
               Example->pid, now.z now.pt.x, now.pt.y); }
    5: proc 0 (example) line 19 ... (state 9) [{c_code5}]
spin: line 20 ..., Error: assertion violated
spin: text of failed assertion: assert(0)
    6: proc 0 (example) line 20 ... (state 10) [assert(0)]
spin: trail ends after 6 steps
#processes: 1
  6: proc 0 (example) line 21 ... (state 11)
1 process created
```

The assertion is violated at the end, but this is merely because it was hardwired to fail. None of the C data objects referenced were ever created during this run, and thus none of them had any values that were effectively assigned to them at the end. Note also that the text of the c_code fragment that is numbered c_code5 here is printed out, but that the print statement that it contains is not itself executed, or else the values printed would have shown up in the output near this line.
Issues to Consider

The capability to embed arbitrary fragments of C code into a PROMELA model is powerful and therefore easily misused. The intent of these features is to support mechanized model extractors that can automatically extract an accurate, possibly abstract, representation of application level C code into a SPIN verification model. The model extractor (see Appendix D) can include all the right safeguards that cannot easily be included in SPIN without extending it into a full ANSI-C compiler and analyzer. Most of the errors that can be made with the new primitives will be caught, but not necessarily directly by SPIN. The C compiler, when attempting to compile a model that contains embedded fragments of code, may object to ill-defined structures, or the verifier may crash on faults that can be traced back to coding errors in the embedded code fragments.

If data that is manipulated inside the embedded C code fragments contains relevant state information, but is not declared as such with c_state or c_track primitives, then the search process itself can get confused, and error trails may be produced by the verifier that do not correspond to feasible executions of the modeled system. With some experience, these types of errors are relatively easy to diagnose. Formally, they correspond to invalid "abstractions" of the model. The unintended "abstractions" are caused by missing c_state or c_track primitives.

To see what happens when we forget to treat externally declared data objects as carrying state information, consider the following simple model:

```c
C_code { int x; }

active proctype simple()
{
    C_code { x = 2; };
    if
    :: C_code { x = x+2; }; assert(c_expr { x==4 })
    :: C_code { x = x*3; }; assert(c_expr { x==6 })
    fi
}
```

We have declared the variable x in a c_code statement, but omitted to track its value. The verifier will therefore ignore value changes in this variable when it stores and compares states, although it will faithfully perform every assignment or test of this variable in the execution of the model.

At first sight, it would seem obvious that neither one of the two could possibly fail, but when we perform the verification we see:

```
$ spin -a simple1.pr
$ cc -o pan pan.c
$ ./pan
pan: assertion violated (x == 6)
pan: wrote simple.pr.trail
...```

To understand the reason for this error, consider for a moment how the depth-first search process proceeds in this case. The verifier starts by executing the assignment

```c
C_code { x = 2; };
```
Deferring File Inclusion

It is often convenient to include a collection of C code into a model with a preprocessor include directive, for instance, as follows:

```c
#include "promela.h"   /* Promela data definitions */
c_decl {
    #include "c_types.h"   /* C data type definitions */
}
c_code {
    #include "functions.c" /* C function definitions */
}
#include "model.pr"    /* the Promela model itself */
```

When SPIN invokes the C preprocessor on this model, the contents of the included files are inserted into the text before the model text is parsed by the SPIN parser. This works well if the files that are included are relatively small, but since there is a limit on the maximum size of a c_code or c_decl statement, this can fail if the files exceed that limit. (At the time of writing, this limit is set at 64Kbytes.)

There is an easy way to avoid hitting this limit. Because C code fragments are not interpreted until the verifier code is parsed by the C compiler, there is no need to actually have the body of a c_code or c_decl statement inserted into the text of the model before it is passed to the SPIN parser. We can achieve this by prefixing the pound sign of the corresponding include directives with a backslash, as follows:

```c
#include "model.pr"    /* the Promela model itself */
c_decl {
    \#include "c_types.h"   /* C data type definitions */
}
c_code {
    \#include "functions.c" /* C function definitions */
}
```

The SPIN parser will now simply copy the include directive itself into the generated C code, without expanding it first. The backslash can only be used in this way inside c_decl and c_code statements, and it is the recommended way to handle included files in these cases.
**c_code**

**Name**

c_code – embedded C code fragments.

**Syntax**

```c

C_code { /* c code */ }
```

**Executability**

true

**Effect**

As defined by the semantics of the C code fragment placed between the curly braces.

**Description**

The `c_code` primitive supports the use of embedded C code fragments inside PROMELA models. The code must be syntactically valid C, and must be terminated by a semicolon (a required statement terminator in C).

There are two forms of the `c_code` primitive: with or without an embedded expression in square brackets. A missing expression clause is equivalent to `[ 1 ]`. If an expression is specified, its value will be evaluated as a general C expression before the C code fragment inside the curly braces is executed. If the result of the evaluation is non-zero, the `c_code` fragment is executed. If the result of the evaluation is zero, the code between the curly braces is ignored, and the statement is treated as an assertion violation. The typical use of the expression clause is to add checks for nil-pointers or for bounds in array indices. For example:

```c

C_code [Pex->ptr != 0 && now.i < 10 && now.i >= 0] {
    Pex->ptr.x[now.i] = 12;
}
```

A `c_code` fragment can appear anywhere in a PROMELA model, but it must be meaningful within its context, as determined by the C compiler that is used to compile the complete model checking program that is generated by SPIN from the model.

Function and data declarations, for instance, can be placed in global `c_code` fragments preceding all proctype definitions. Code fragments that are placed inside a proctype definition cannot contain function or data declarations. Violations of such rules are caught by the C compiler. The SPIN parser merely passes all C code fragments through into the generated verifier uninterpreted, and therefore cannot detect such errors.

There can be any number of C statements inside a `c_code` fragment.

**Examples**
**c_decl**

**Name**

c_decl, c_state, c_track – embedded C data declarations.

**Syntax**

\[
\begin{align*}
\text{c_decl} & \{ \ /* \ c \ declaration */ \ } \\
\text{c_state} & \text{ string string [ string ]} \\
\text{c_track} & \text{ string string}
\end{align*}
\]

**Executability**

true

**Description**

The primitives c_decl, c_state, and c_track are global primitives that can only appear in a model as global declarations outside all proctype declarations.

The c_decl primitive provides a capability to embed general C data type declarations into a model. These type declarations are placed in the generated pan.h file before the declaration of the state-vector structure, which is also included in that file. This means that the data types introduced in a c_decl primitive can be referenced anywhere in the generated code, including inside the state vector with the help of c_state primitives. Data type declarations can also be introduced in global c_code fragments, but in this case the generated code is placed in the pan.c file, and therefore appears necessarily after the declaration of the state-vector structure. Therefore, these declarations cannot be used inside the state vector.

The c_state keyword is followed by either two or three quoted strings. The first argument specifies the type and the name of a data object. The second argument the scope of that object. A third argument can optionally be used to specify an initial value for the data object. (It is best not to assume a known default initial value for objects that are declared in this way.)

There are three possible scopes: global, local, or hidden. A global scope is indicated by the use of the quoted string "Global." If local, the name Local must be followed by the name of the proctype in which the declaration is to appear, as in "Local ex2." If the quoted string "Hidden" is used for the second argument, the data object will be declared as a global object that remains outside the state vector.

The primitive c_track is a global primitive that can declare any state object, or more generally any piece of memory, as holding state information. This primitive takes two string arguments. The first argument specifies an address, typically a pointer to a data object declared elsewhere. The second argument gives the size in bytes of that object, or more generally the number of bytes starting at the address that must be tracked as part of the system state.

**Examples**

The first example illustrates how c_decl, c_code and c_state declarations can be used to define either visible or hidden state variables, referring to type definitions that must precede the internal SPIN state-vector declaration. For an explanation of the rules for prefixing global and local variables inside c_code and c_expr statements, see the manual pages for these two statements.
c_expr

Name
c_expr – conditional expressions as embedded C code.

Syntax
c_expr { /* c code */ }
c_expr '/* c expr */' { /* c code */ }

Executability
If the return value of the arbitrary C code fragment that appears between the curly braces is non-zero, then true; otherwise false.

Effect
As defined by the semantics of the C code fragment that is placed between the curly braces. The evaluation of the C code fragment should have no side effects.

Description
This primitive supports the use of embedded C code inside PROMELA models. A c_expr can be used to express guard conditions that are not necessarily expressible in PROMELA with its more restrictive data types and language constructs.

There are two forms of the c_expr primitive: with or without an additional assertion expression in square brackets. A missing assertion expression is equivalent to [ 1 ]. If an assertion expression is specified, its value is evaluated as a general C expression before the code inside the curly braces is evaluated. The normal (expected) case is that the assertion expression evaluates to a non-zero value (that is to an equivalent of the boolean value true). If so, the C code between the curly braces is evaluated next to determine the executability of the c_expr as a whole.

If the evaluation value of the assertion expression is zero (equivalent to false), the code between the curly braces is ignored and the statement is treated as an assertion violation.

The typical use of the assertion expression clause is to add checks for nil-pointers or for possible array bound violations in expressions. For example:

c_expr [Pex->ptr != NULL] { Pex->ptr->y }

Note that there is no semicolon at the end of either C expression. If the expression between square brackets yields false (zero), then an assertion violation is reported. Only if this expression yields true (non-zero), is the C expression between curly braces evaluated. If the value of this second expression yields true, the c_expr as a whole is deemed executable and can be passed; if false, the c_expr is unexecutable and blocks.

Examples
The following example contains a do-loop with four options. The first two options are equivalent, the only difference being in the way that local variable x is accessed: either via an embedded C code fragment or with the normal PROMELA constructs.

active proctype ex1()
{
    int x;
do
    :: c_expr { Pex1->x < 10 } -> c_code { Pex1->x++; }
    :: x < 10 -> x++
    :: c_expr { fct() } -> x--
    :: else -> break
    od
}

The local variable x is declared here as a PROMELA variable. Other primitives, such as c_decl, c_state, and c_track allow for the declaration of data types that are not directly supported in PROMELA.

The references to local variable x have a pointer prefix that always starts with a fixed capital letter P that is followed by the name of the proctype and an pointer arrow. This prefix locates the variable in the local state vector of the proctype instantiation.

The guard of the third option sequence invokes an externally defined C function named fct() that is presumed to return an integer value. This function can be declared in a global c_code fragment elsewhere in the model, or it can be declared externally in separately compiled code that is linked with the pan.[chtmb] verifier when it is compiled.

Notes
Note that there is no semicolon before the closing curly brace of a c_expr construct. It causes a C syntax error if such a semicolon appears here. All syntax errors on embedded C code fragments are reported during the compilation of the generated pan.[chtmb] files. These errors are not detectable by the SPIN parser.

Because embedded C code is not processed by the SPIN parser, inline parameter substitutions are not applied to those code fragments. In cases where this is needed, the inline definitions can be replaced with macro preprocessor definitions.

See Also
c_code, c_decl, c_state, c_track, macros
Chapter 18. Overview of SPIN Options

"An error does not become a mistake unless you refuse to correct it."

—(Manfred Eigen, 1927–)

In this chapter we discuss all available SPIN options. The options are grouped into seven categories according to their primary use, as follows:

- Compile-time options, which can be used to compile the SPIN source itself for different platforms and for different types of use
- Simulation options, which can be used for customizing simulation runs of PROMELA models
- Syntax checking options, for performing a basic check of the syntactic correctness of PROMELA models
- LTL conversion options, describing various ways in which the conversion from LTL formulae to PROMELA never claims can be done
- Model checker generation options
- Postscript generation options
- Miscellaneous options

Except for the first category above, all these options are defined as run-time parameters to the SPIN tool. Since SPIN is an evolving tool, new options will continue to be added to the tool from time to time. An up-to-date list of these options in the specific version of SPIN that is installed on your system can always be printed with the command:

```
$ spin --
```

The discussion in this chapter covers all compile-time and run-time options that are available in SPIN version 4.
Compile-Time Options

There are eight compile-time directives that can be used to change the default settings for the compilation of the SPIN sources. They are: __FreeBSD__, CPP, MAXQ, NO_OPT, NXT, PC, PRINTF, and SOLARIS.

These directives are typically set in the SPIN makefile at the time the tool is first installed on a system, and should rarely need modification later. The settings are typically included by changing the definition of the CFLAGS parameter in SPIN's makefile. As an example, to change the default location of the C preprocessor in the compiled version of SPIN, we could change the line

```
CFLAGS=-ansi -D_POSIX_SOURCE
```

into this new setting

```
CFLAGS=-ansi -D_POSIX_SOURCE -DCPP=/opt/prep/cpp
```

We first discuss the use of the CPP directive together with the two special cases __FreeBSD__ and SOLARIS.

-DCPP=..., -DSOLARIS, -D__FreeBSD__

SPIN always preprocesses the source text of PROMELA models with the standard C preprocessor before it attempts to parse it. The preprocessor takes care of the interpretation of all #include and #define directives. On most UNIX systems, the location of the C preprocessor is /lib/cpp, so the default compilation of SPIN implies -DCPP=/lib/cpp.

On PCs the preprocessor is usually installed as a separate program, and therefore when SPIN is compiled with the directive -DPC, the default setting of the CPP parameter changes to -DCPP=cpp.

To override the default settings, an explicit value for the CPP parameter can be provided.

Two standard cases are predefined. By compiling SPIN with the directive -D__FreeBSD__, the default setting for the preprocessor changes to cpp, which matches the requirements on these systems. By compiling SPIN with the directive -DSOLARIS, the default setting for the preprocessor changes to /usr/ccs/lib/cpp, matching the location of the C preprocessor on Solaris systems.

These settings only affect the compilation of the main.c file from the SPIN sources.

There is also another way to define a switch to another preprocessor—by using SPIN's command line arguments P and E. For instance, on an OS2 system one might say:

```
$ spin -Picc -E/Pd+ -E/Q+ model
```

to notify SPIN that preprocessing is done by calling icc with parameters /Pd+ /Q+. Similarly, on a Windows system with the Visual C++ compiler installed, one can say:
Simulation Options

The command line options to SPIN that we discuss in this section are all meant to define or modify the type of output that is produced during a simulation run, that is, they do not affect any verification settings.

SPIN can be used for three main types of model simulation: random (default), interactive (option -i), and guided simulation (option -t).

When invoked with only a filename as an argument and no other command-line options, for instance,

```
$ spin model
```

SPIN performs a random simulation of the model that is specified in the file. If no filename is provided, SPIN attempts to read a model from the standard input. This can of course be confusing if it is unexpected, so SPIN gives a warning when it is placed in this mode:

```
$ spin
Spin Version 4.0.7 -- 1 August 2003
reading input from stdin:
```

Typing an end-of-file symbol gets the tool out of this mode again (control-d on UNIX systems, or control-z on Windows systems).

Also possibly confusing at first, even if a filename is provided, may be that a simulation run of the model by itself may not generate any visible output; for instance, when the PROMELA model does not contain any explicit print statements. At the end of the simulation run, though, if it does terminate, SPIN always prints some details about the final state that is reached when the simulation completes. By adding additional options (e.g., -c, or -p) more detail on a simulation run in progress will be provided, but only the information that the user explicitly requests is generated. Every line of output that is produced by the simulator normally also contains a reference to the source line in the model that generated it.

Summarizing: A random simulation is selected by default. If run-time option -i is used, the simulation will be performed in interactive mode, which means that the SPIN simulator will prompt the user each time that a non-deterministic choice has to be resolved. The user can then choose from a list of alternatives, and in this way interactively guide the execution towards a point of interest. If run-time option -t is used, the simulator is put into guided simulation mode, which presumes the existence of a trail file that must have been produced by the verification engine prior to the simulation.

Alphabetical Listing

-B

Suppresses the printout at the end of a simulation run, giving information on the final state that is reached in each process, the contents of channels, and the value of variables.

-b

Suppresses the output from print statements during a simulation run.

-c

Prints all receive statements that are executed, giving the name and number of the receiving process and the corresponding source line number. For each message parameter this shows the message type and the message channel number and name. For instance:

```
channel number and name. For instance:
Prints all receive statements that are executed, giving the name and number of the receiving process and the corresponding source line number. For each message parameter this shows the message type and the message channel number and name. For instance:
```

-deep-limit (-u100 steps) reached

Also possibly confusing at first, even if a filename is provided, may be that a simulation run of the model by itself may not generate any visible output; for instance, when the PROMELA model does not contain any explicit print statements. At the end of the simulation run, though, if it does terminate, SPIN always prints some details about the final state that is reached when the simulation completes. By adding additional options (e.g., -c, or -p) more detail on a simulation run in progress will be provided, but only the information that the user explicitly requests is generated. Every line of output that is produced by the simulator normally also contains a reference to the source line in the model that generated it.

Summarizing: A random simulation is selected by default. If run-time option -i is used, the simulation will be performed in interactive mode, which means that the SPIN simulator will prompt the user each time that a non-deterministic choice has to be resolved. The user can then choose from a list of alternatives, and in this way interactively guide the execution towards a point of interest. If run-time option -t is used, the simulator is put into guided simulation mode, which presumes the existence of a trail file that must have been produced by the verification engine prior to the simulation.

Alphabetical Listing

-B

Suppresses the printout at the end of a simulation run, giving information on the final state that is reached in each process, the contents of channels, and the value of variables.

-b

Suppresses the output from print statements during a simulation run.

-c
Syntax Checking Options

-a

Normally, when simulation runs are performed, SPIN tries to be forgiving about minor syntax issues in the model specification. Because the PROMELA model is interpreted on-the-fly during simulations, any part of the model that is not executed may escape checking. It is therefore possible that some semantic issues are missed in simulation runs.

When SPIN option -a is used, though, a more thorough check of the complete model is performed, as the source text for a model-specific verifier is also generated. This means that, quite apart from the generation of the verifier source files, the -a option can be useful as a basic check on the syntactical correctness of a PROMELA model. More verbose information is generated if the -v flag is also added, as in:

$ spin -a -v model

-A

When given this option, SPIN will apply a property-based slicing algorithm to the model which can generate warnings about statements and data objects that are likely to be redundant, or that could be revised to use less memory. The property-based information used for the slicing algorithm is derived from basic assertion statements and PROMELA never claims that appear in the model.

-I

This option will cause SPIN to print the body text of each proctype specification after all preprocessing and inlining operations have been completed. It is useful to check what the final effect is of parameter substitutions in inline calls, and of ordinary macro substitutions.

-Z

This option will run only the preprocessor over the model source text, writing the resulting output into a file named pan.pre. Good for a very mild syntax check only. The option is there primarily for the benefit of XSPIN.
Postscript Generation

-M

Generates a graphical version of a message sequence chart as a Postscript file. A long chart is automatically split across multiple pages in the output that is produced. This representation is meant to closely resemble the version that is produced by XSPIN. The result is written into a file called model.ps, where model is the name of the file with the PROMELA source text for the model. The option can be used for random simulation runs, or to reproduce a trail generated by the verifier (in combination with option -t). See also option -c for a non-Postscript alternative.
Model Checker Generation

The following options determine how verification runs of PROMELA models can be performed. The verifications are always done in several steps. First, optimized and model-specific source code for the verification process is generated. Next, that source code can be compiled in various ways to fine-tune the code to a specific type of verification. Finally, the compiled code is run, again subject to various run-time verification options.

-a

Generates source code that can be compiled and run to perform various types of verification of a PROMELA model. The output is written into a set of C files named pan.[cbhmt], that must be compiled to produce an executable verifier. The specific compilation options for the verification code are discussed in Chapter 19. This option can be combined with options -J and -m.

-N file

Normally, if a model contains a PROMELA never claim, it is simply included as part of the model. If many different types of claims have to be verified for the same model, it can be more convenient to store the claim in a separate file. The -N option allows the user to specify a claim file, containing the text of a never claim, that the SPIN parser will include as part of the model. The claim is appended to the model, that is, it should not contain definitions or declarations that should be seen by the parser before the model itself is read.

The remaining five options control which optimizations that may be used in the verifier generation process are enabled or disabled. Most optimizations, other than more experimental options, are always enabled. Typically, one would want to disable these optimizations only in rare cases, for example, if an error in the optimization code were to be discovered.

-o1

Disables data-flow optimizations in verifier. The data-flow optimization attempts to identify places in the model where variables become dead, that is, where their value cannot be read before it is rewritten. The value of such variables is then reset to zero. In most cases, this optimization will lower verification complexity, but it is possible to create models where the reverse happens.

-o2

Disables the elimination of write-only variables from the state descriptor. It should never be necessary to use this option, other than to confirm its effect on the length of the state vector and the resulting reduction in the memory requirements.

-o3

Disables the statement merging technique. Statement merging can make it hard to read the output of the pan -d output (see Chapter 19), which dumps the internal state assignments used in the verifier. Disabling this option restores the old, more explicit format, where only one statement is executed per transition. Disabling this option, however, also loses the reduction in verification complexity that the statement merging technique is designed to accomplish.

-o4

Enables a more experimental rendezvous optimization technique. This optimization attempts to precompute the feasibility of rendezvous operations, rather than letting the model checker determine this at run time. It is hard to find cases where the use of this option brings convincing savings in the verification process, so it is likely that this option will quietly disappear in future SPIN versions.

-o5

Disables the case caching technique. Leaving this option enabled allows the verifier generator to make smarter use of case statements in the pan.m and pan.b files, especially for larger models. This allows for a sometimes considerable speedup in the compilation of the generated verifier.

-S1 and -S2

Separate compilation options. If the size of the verification model is much larger than the size of a never claims, and there are very many such claims that need to be verified for a single model, it can be more efficient to compile the verification source text for the model separately from the source text for the claim automata. If the file model.pml contains both the main model specification and the never claim, in the simplest case the verifier is then generated and compiled in two separate steps:

$ spin -S1 model.pml # source for model without claim
$ spin -S2 model.pml # source for the claim

This generates two sets of sources, with file names pan._[chmbt] and pan_t.[chmbt], respectively. These sources can be compiled separately and then linked to produce an executable verifier:

$ cc -c pan_s.c         # source for model without claim
$ cc -c pan_t.c         # source for the claim
$ cc -o pan pan_s.o pan_t.o             # link both parts

Alternatively, on a Windows machine using the Gnu C compiler, the command sequence might look as follows:

$ gcc -c pan_s.c        # source for model without claim
$ gcc -c pan_t.c        # source for the claim
$ gcc -o pan.exe pan_s.obj pan_t.obj    # link both parts

The idea is that the first part, generating and compiling the source for the main model without the claim, needs to be done only once, independent of the number of different never claims that must be verified. The second part, generating and compiling the source for the claim automata, can be repeated for each new claim, but is generally much faster, since the claim automata are typically much smaller than the model to be verified.

Chapter 11, p. 261, contains a more detailed discussion of these options.
LTL Conversion

These two options support the conversion of formulae specified in Linear Temporal Logic (LTL) into PROMELA never claims. The formula can either be specified on the command line or read from a file.

-f formula

This option reads a formula in LTL syntax from the second argument and translates it into the equivalent PROMELA syntax for a never claim. Note that there must be a space between the -f argument and the formula. If the formula contains spaces, or starts with the diamond operator $\Box$, it should be quoted to form a single argument and to avoid misinterpretation by the shell. The quoting rules may differ between systems. On UNIX systems either double or single quotes can be used. On many Windows or Linux systems only single quotes work. In case of problems, use the -F alternative below.

-F file

This option behaves like option -f except that it will read the formula from the given file and not from the command line. The file should contain the formula on the first line. Any text that follows this first line is ignored, which means that it can be used to store arbitrary additional comments or annotation on the formula.
### Miscellaneous Options

**-d**

Produces symbol table information for the PROMELA model. For each PROMELA object, this information includes the type, name, and number of elements (if declared as an array); the initial value (if a data object) or size (if a message channel), the scope (global or local), and whether the object is declared as a variable or as a parameter. For message channels, the data types of the message fields are also listed. For structure variables, the third field in the output defines the name of the structure declaration that contained the variable.

**-C**

Prints information on the use of channel names in the model. For instance:

```
$ spin -C tpc6
chan rtpc
  never used under this name
chan manager-child[2]
  exported as run parameter by: manager to Session par 3
  sent to by: manager
chan manager-parent
  exported as run parameter by: manager to Session par 4
  received from by: manager
```

In this example, the names Session, manager, parent, and child are the names of proctypes in the model. Local channel names are identified as the pair of a proctype name and a channel name, separated by a hyphen. A channel name is said to be exported if it appears as an actual parameter in a run statement. In effect, the channel is then passed from one process to another. The listing gives the number of the parameter in the call to run in which the channel name appears.

When combined with option -g, the output will also include information on known access patterns to all globally declared channels:

```
$ spin -C -g tpc6
chan handler
  received from by: manager
  sent to by: local_tpc
chan tpc
  received from by: local_tpc
  sent to by: user
chan rtpc
  never used under this name
chan Session-me
  imported as proctype parameter by: Session par 1
  received from by: Session
chan Session-parent
  imported as proctype parameter by: Session par 1
  sent to by: Session
chan manager-child[2]
  exported as run parameter by: manager to Session par 3
  sent to by: manager
chan manager-parent
  exported as run parameter by: manager to Session par 4
  received from by: manager
```
Chapter 19. Overview of PAN Options

"The only reasonable way to get a program right is to assume that it will at first contain errors and take steps to discover these and correct them."

—(Christopher Strachey, 1916–1975)

This chapter summarizes all verification options. The options apply to the verification code that is generated with SPIN's run-time option -a. Also included is an explanation of the information that is generated by the program at the end of a verification run (unless disabled with PAN run-time option -n).

The three main sections of this chapter cover:

- **PAN Compile-Time Options:**
  Options that are available at the time of compilation of the verifier source code.

- **PAN Run-Time Options:**
  Options that are available as command-line arguments to the executable PAN code that is generated by the compiler.

- **PAN Output Format:**
  An explanation of the information that is generated by the PAN verifiers at the end of a run.

The primary reason for the reliance of compile-time options for the automatically generated verifier code is efficiency: using compile-time directives allows for the generation of more efficient executables than if all options were handled through the use of command line arguments.

If the XSPIN user interface is used, most options are selected automatically by XSPIN (based on user preferences), so in that case there is no strict need to be familiar with the information that is presented in this chapter.
PAN Compile-Time Options

There are quite a few compile-time options for the PAN sources. We will divide them into the following groups, depending on their main purpose:

- Basic options
- Options related to partial order reduction
- Options to increase speed
- Options to reduce memory use
- Options for use only when prompted by PAN
- Options for debugging PAN verifiers
- Experimental options

Usage of all compile-time directives is optional. In its most minimal form, the generation, compilation, and execution of the verification code would simply proceed as follows:

```
$ spin -a spec
$ cc -o pan pan.c
$ ./pan
```

The compile-time directive can modify the default behavior of the verifier to achieve specific effects, as explained in more detail shortly. For instance, to enable breadth-first search and bitstate hashing, the compilation command would change into:

```
$ cc -DBFS -DBITSTATE -o pan pan.c
```
Basic Options

-DBFS

Arranges for the verifier to use a breadth-first search algorithm rather than the standard depth-first search. This uses more memory and restricts the type of properties that can be verified to safety properties only, but within these restrictions it is the easiest way to find a short error path. This option can be combined with the various methods for reducing memory use, such as hash-compact, bitstate hashing, collapse compression, and minimized automaton compression.

-DMEMCNT=N

Sets an upper-bound to the amount of memory that can be allocated by the verifier to 2N bytes. This limit should be set as closely as possible to the amount of physical (not virtual) memory that is available on the machine. Without this limit, the verifier would pass this limit and start using virtual memory, which in this type of search can lead to a serious degradation of performance, and in the worst case (when the amount of virtual memory used exceeds the amount of physical memory used) to thrashing. For example,

```
$ cc -DMEMCNT=29 -o pan pan.c
```

sets the memory limit at 229 = 512 Megabyte. The next step up would bring this to 1 Gigabyte. Somewhat finer control is available with the directive MEMLIM.

-DMEMLIN=N

Sets an upper-bound to the amount of memory that can be allocated by the verifier to N Megabytes. For example,

```
$ cc -DMEMLIN=600 -o pan pan.c
```

sets the limit at 600 Megabyte.

-DNOCLAIM

If a PROMELA never claim is part of the model, the addition of this directive will exclude it from the verification attempt. It is safe to use this directive even if no never claim is present. The code that would ordinarily be used for the handling of the claim is disabled, which can also improve performance slightly.

-DNP

Includes the code in the verifier for non-progress cycle detection, which in turn enables run-time option -l and simultaneously disables run-time option -a for the detection of standard acceptance cycles.

-DON_EXIT=STRING

The name ON_EXIT can be used to define an external procedure name that, if defined, will be called immediately after the verifier has printed its final statistics on a verification run and just before the verifier exits. A possible use can be, for instance:
Options Related to Partial Order Reduction

-DNOREDUCE

Disables the partial order reduction algorithm and arranges for the verifier to perform an exhaustive full state exploration, without reductions. This clearly increases both the time and the memory requirements for the verification process. The partial order reduction method used in SPIN is explained in Chapter 9 (p. 191).

-DXUSAFE

Disables the validity checks on xr and xs assertions. This improves the performance of the verifier and can be useful in cases where the default check is too strict.
Options Used to Increase Speed

-DNOBOUNDCHECK

Disables the default check on array indices that is meant to intercept out-of-bound array indexing errors. If these types of errors are known to be absent, disabling the check can improve performance.

-DNOFAIR

Disables the code for the weak fairness algorithm, which means that the corresponding run-time option -f will disappear. If it is known that the weak fairness option will not be used, adding this directive can improve the performance of the verifier.

-DSAFETY

Optimizes the code for the case where no cycle detection is needed. This option improves performance by disabling run-time options -l and -a, and removing the corresponding code from the verifier.
Options Used to Decrease Memory Use

- **DBITSTATE**

  Uses the bitstate storage algorithm instead of default exhaustive storage. The bitstate algorithm is explained in Chapter 9 (p. 206).

- **DHC**

  Enables the hash-compact storage method. The state descriptor is replaced with a 64-bit hash value that is stored in a conventional hash table. Variations of the algorithm can be chosen by adding a number from zero to four to the directive: HC0, HC1, HC2, HC3, or HC4 to use 32, 40, 48, 56, or 64 bits, respectively. The default setting with HC is equivalent to HC4, which uses 64 bits. The hash-compact algorithm is explained in Chapter 9 (p. 212).

- **DCOLLAPSE**

  Compresses the state descriptors using an indexing method, which increases run time but can significantly reduce the memory requirements. The collapse compression algorithm is explained in Chapter 9 (p. 198).

- **DMA=N**

  Enables the minimized automaton storage method to encode state descriptors. Often combines a very significant reduction in memory requirements with a very significant increase in the run-time requirements. The value N sets an upper-bound to the size of the state descriptor as stored. This method can often fruitfully be combined with -DCOLLAPSE compression.

- **DSC**

  Enables a stack cycling method, which can be useful for verifications that require an unusually large depth-limit. The memory requirements for the stack increase linearly with its maximum depth. The stack cycling method allows only a small fraction of the stack to reside in memory, with the remainder residing on disk. The algorithm swaps unused portions of the search stack to disk and arrange for just a working set to remain in-core. With this method, the run-time flag -m determines only the size of the in-core portion of the stack, but does not restrict the stack's maximum size. This option is meant only for those rare cases where the search stack may be millions of steps long, consuming the majority of the memory requirements of a verification.
Options to Use When Prompted by PAN

If the verifier discovers a problem at run time that can be solved by recompiling the verifier with different directives, the program prints a recommendation for the recompilation before it exits. This applies to two directives in particular: -DNFAIR and -DVECTORSZ.

-DNFAIR=N

Allocates memory for enforcing weak fairness. By default, that is, in the absence of an explicit setting through the use of this directive, the setting used is N=2. If this setting is insufficient, the verifier will prompt for recompilation with a higher value. The default setting can be exceeded if there is an unusually large number of active processes. Higher values for N imply increased memory requirements for the verification.

-DVECTORSZ=N

The default maximum size for the state vector (i.e., state descriptor) is 1,024 bytes. If this is insufficient, for unusually large models, the verifier will prompt for recompilation with a higher value. For example:

$ cc -DVECTORSZ=2048 -o pan pan.c

There is no predefined limit for the size of the state vector that can be set in this way. Often, a large state vector can successfully be compressed losslessly by also using the -DCOLLAPSE directive.
Options for Debugging PAN Verifiers

-DVERBOSE

Adds elaborate debugging printouts to the run. This is useful mostly for small models, where a detailed dump of the precise actions of the verifier is needed to trace down suspect or erroneous behavior.

-DCHECK

Provides a slightly more frugal version of the -DVERBOSE directive.

-DSVDUMP

Enables an additional run-time option -pN to the verifier which, if selected, writes a binary dump of all unique state descriptors encountered during a verification run into a file named sv_dump. The file is only generated at the end of the verification run, and uses a fixed integer size of N bytes per recorded state. State descriptors shorter than N bytes are padded with zeros. See also -DSDUMP.

-DSDUMP

If used in combination with the directive -DCHECK this adds an ASCII dump of all state descriptors encountered in the search to the verbose debugging output that is generated.
Experimental Options

-DBCOMP

If used in combination with the directive -DBITSTATE, modifies the code to compute hash functions over not the original but the compressed version of the state descriptor (using the standard masking technique). In some cases this has been observed to improve the coverage of a bitstate run.

-DCOVEST

If used in combination with the directive -DBITSTATE, this option compiles in extra code for computing an alternative coverage estimate at the end a run. On some systems, the use of this code also requires linkage of the object code with the math library, for instance, with the compiler flag -lm.

The experimental formula that is used to compute the coverage in this mode was derived by Ulrich Stern in 1997. Stern estimated that when a run has stored \( R \) states in a hash array of \( B \) bits, then the true number of reachable states \( R' \) is approximately

\[
R' = \frac{\ln (1 - R/B)}{\ln (1 - 1/B)}
\]

When the verifier is compiled with directive -DCOVEST it reports the estimated state space coverage as the percentage of states that was reached compared to the estimated total number of reachable states, that is:

\[
\frac{R}{R'} \times 100\%
\]

-DCTL

Allows only those partial order reductions that are consistent with branching time logics, such as CTL. The rule used here is that each persistent set that is computed contains either all outgoing transitions or precisely one.

-DGLOB_ALPHA

Considers process death to be a globally visible action, which means that the partial order reduction strategy cannot give it priority over other actions. The resulting verification mode restores compatibility with SPIN version numbers from 2.8.5 to 2.9.7.

-DHYBRID_HASH

Using this option can reduce the size of every state descriptor by precisely one word (4 bytes), but this benefit will only be seen in 25% of all cases. In the standard storage method, when the state descriptor is one, two, or three bytes longer than a multiple of four, the memory allocator pads the amount of memory that is effectively allocated with one, two, or three bytes, respectively. This padding is done to secure memory alignment. To avoid this in at least some of the cases, the HYBRID_HASH will consider state descriptors that exceed a multiple of four by precisely one byte, and truncate the state vector by that amount. The one byte that is removed is now added to the hash value that is computed. This can cause more hash collisions to occur, but it does preserve a correct search discipline, and it can save memory.

-DLC

If used in combination with the directive -DBITSTATE, this option replaces exhaustive storage of states in the depth-first search stack with a four-byte hash-compact representation. This option slows down the verification process, but it can reduce the memory requirements. There is a very small additional risk of hash collisions on stack entries, but this is avoided by using a different random number generator for the hash values.
Run-Time Options

The following options can be given as command-line arguments to the compiled version of the verifiers generated by SPIN. They are listed here in alphabetical order.

-A

Suppresses the reporting of basic assertion violations. This is useful if, for instance, the verification process targets a different class of errors, such as non-progress cycles or Büchi acceptance cycles. See also -E.

-a

Arranges for the verifier to report the existence, or absence, of Büchi acceptance cycles. This option is disabled when the verifier is compiled with the directive -DNP, which replaces the option with -l, for non-progress cycle detection.

-b

Selecting this bounded search option makes it an error, triggering an error trail, if an execution can exceed the depth limit that is specified with the -m option. Normally, exceeding the search depth limit only generates a warning.

-c N

Stops the search after the Nth error has been reported. The search normally stops after the first error is reported. Using the setting -c0 will cause all errors to be reported. See also run-time option -e.

-d

Prints the internal state tables that are used for the verification process and stops. For the leader election protocol example from the SPIN distribution, the output looks as follows. One state table is generated for each proctype that appears in the SPIN model, with one line per transition.

[1] Not all transitions are shown. Long lines are split into two parts here for layout purposes.

```
$ spin -a leader
$ ./pan -d
proctype node
state 1 - (tr 8) -> state 3 [id 0 tp 2] [-----L] \ line 16 => Active = 1
state 3 - (tr 9) -> state 30 [id 2 tp 5] [-----L] \ line 18 => outfirst,id [(3,2)]
state 30 - (tr 10) -> state 15 [id 3 tp 504] [---e-L] \ line 19 => in?first,number [(2,3)]
state 30 - (tr 17) -> state 28 [id 16 tp 504] [---e-L] \ line 19 => in?second,number
...
proctype init
state 10 - (tr 3) -> state 7 [id 33 tp 2] [A---L] \ line 49 => proc = 1
state 7 - (tr 4) -> state 3 [id 34 tp 2] [A---L] \ line 51 => ((proc<=5))
state 7 - (tr 6) -> state 9 [id 37 tp 2] [A---L] \ line 51 => ((proc>5))
state 3 - (tr 5) -> state 7 [id 35 tp 2] [A---L] \ line 53 => (run node(...))
state 9 - (tr 1) -> state 11 [id 41 tp 2] [-----L] \ line 51 => break
```
**Pan Output Format**

A typical printout of a verification run is shown in Figure 19.1. This is what each line in this listing means:

**Figure 19.1 Example Output Generated by Pan**

```
$ ./pan
(Spin Version 4.0.7 -- 1 August 2003)
   + Partial Order Reduction

Full statespace search for:
   never claim       - (none specified)
   assertion violations +
   acceptance cycles  - (not selected)
   invalid end states +

State-vector 32 byte, depth reached 13, errors: 0
  74 states, stored
  30 states, matched
  104 transitions (= stored+matched)
  1 atomic steps
hash conflicts: 2 (resolved)
(max size 2^18 states)

1.533   memory usage (Mbyte)

unreached in proctype ProcA
   line 7, state 8, "Gaap = 4"
   (1 of 13 states)
unreached in proctype :init:
   line 21, state 14, "Gaap = 3"
   line 21, state 14, "Gaap = 4"
   (1 of 19 states)

(Spin Version 4.0.7 -- 1 August 2003)

Identifies the version of SPIN that generated the pan.c source from which this verifier was compiled.

   + Partial Order Reduction

The plus sign means that the default partial order reduction algorithm was used. A minus sign would indicate compilation for exhaustive, non-reduced verification with option -DNOREDUCE. If the verifier had been compiled with the breadth-first search option, using compiler directive -DBFS, then this fact would have been noted here as well.

Full statespace search for:

Indicates the type of search. The default is a full state space search. If the verifier is instead compiled with one of the various types of state compression enabled (e.g., collapse compression, bitstate search, or hash-compact storage), this would be noted in this line of output.
Literature

"I find that a great part of the information I have was acquired by looking up something and finding something else on the way."

—(Franklin P. Jones, 1853-1935)


Appendix A. Automata Products

"Beyond each corner new directions lie in wait."

—(Stanislaw Lec, 1909–1966)

SPIN is based on the fact that we can use finite state automata to model the behavior of asynchronous processes in distributed systems. If process behavior is formalized by automata, the combined execution of a system of asynchronous processes can be described as a product of automata.

Consider, for instance, a system A of n processes, each process given in automaton form, say: A1, A2, . . ., An. Next, consider an LTL formula f and the Büchi automaton B that corresponds to its negation ¬f. Using the automata theoretic verification procedure, we can check if A satisfies f by computing the global system automaton S

\[ S = B \otimes \prod_{i=1}^{n} A_i \]

We use the operator \( \prod \) here to represents an asynchronous product of multiple component automata, and \( \otimes \) to represent the synchronous product of two automata.

The result S of this computation is another finite state automaton that can now be analyzed for its acceptance properties. If formula f can be violated (that is, if ¬f can be satisfied), then S will have accepting \( \omega \)-runs that demonstrate it. We can check if S has accepting runs with the algorithms discussed in Chapter 8.

The definition of the component automata that are used in the computation of the asynchronous product are derived from proctype declarations, and the Büchi automaton B is defined by a never claim.

We have so far taken for granted how the asynchronous and synchronous products of automata are computed and how properties such as Büchi acceptance, non-progress, and the existence of invalid end states can be expressed within this framework. We will discuss those details here.

For each finite state automaton A = (S, s0, L, T, F) that is derived from a proctype declaration or a never claim we can identify three interesting subsets of A. S that capture the assignment of the special label-types used in PROMELA. We will name them as follows:

A. A is the set of states marked with accept-state labels,

A. E is the set of states marked with end-state labels,

A. P is the set of states marked with progress-state labels.

We present the definition of asynchronous and synchronous product first within the standard automata theoretic framework. Within this framework we reason about \( \omega \)-runs (infinite runs) that do or do not satisfy standard Büchi acceptance conditions. The set of final states A. F for each component automaton is in this case identical to set A. A: the set of local states that is explicitly labeled with an accept-state label.

SPIN also has separate verification modes for verifying the absence of non-progress cycles and for verifying pure safety properties, including the verification of absence of deadlock. At the end of this Appendix we will show how the definitions can be modified slightly to also capture these other types of verification.
Asynchronous Products

The asynchronous product of \( n \) component automata is defined as follows:

**Definition A.1 (Asynchronous Product)**

The asynchronous product of a finite set of finite state automata \( A_1, \ldots, A_n \) is another finite state automaton \( A = (S, s_0, L, T, F) \), where

- \( S \) is the Cartesian product \( A_1 \times \cdots \times A_n \times S \),
- \( s_0 \) is the n-tuple \( (A_1. s_0, \ldots, A_n. s_0) \),
- \( L \) is the union set \( A_1. L \cup \ldots \cup A_n. L \), and
- \( T \) is the set of tuples \( ((x_1, \ldots, x_n), I, (y_1, \ldots, y_n)) \) such that \( \exists i, 1 \leq i \leq n, (x_i, I, y_i) \in A_i. T \) and \( \forall j, 1 \leq j \leq n, j \neq i \rightarrow (x_j \equiv y_j) \),
- \( F \) is the subset of those elements of \( A. S \) that satisfy the condition \( \forall (A_1. s, \ldots, A_n. s) \in A. F, \exists i, A_i. s \in A_i. F \).

Note that not all the states in this product automaton are necessarily reachable. Their reachability depends on the semantics we attach to the labels in set \( A. L \) (cf. p. 129).

Recall that the labels from the sets \( A_i. L \) in each component automaton record basic PROMELA statements, such as assignment, assertion, print, condition, send, and receive statements. The intended interpretation of these labels is given by the semantics of PROMELA, as outlined in Chapter 7. Because PROMELA statements can manipulate data objects, when we interpret the semantics on the labels, we really expand automata into extended finite state automata. The automata still remain finite-state under this extension, due to the fact that in PROMELA all data types can have only finite domains. Each extended automaton can be converted fairly trivially into a pure finite state automaton by expanding out the data values. When SPIN computes the asynchronous product, it does this expansion on the fly.

Another interesting aspect of Definition A.1 is that it states that the transitions in the product automaton are the transitions from the component automata, arranged in such a way that only one of the component automata can execute one transition at a time, indivisibly. This corresponds to the standard interpretation of the semantics of concurrency based on the interleaving of process actions. This is of course not the only possible interpretation. Some of the alternatives are discussed in Appendix B (The Great Debates).
Encoding Atomic Sequences

PROMELA has a notion of atomic sequences that allows a sequence of transitions from a single process component to be executed indivisibly. In effect, the interleaving of transitions is temporarily disabled in this case. This feature can easily be captured within the automata framework we have discussed, as also shown in Chapter 7. To do so, we can introduce a special global integer data object named exclusive, with initial value 0. The component processes (represented by automata) are assigned unique positive integer numbers (pids) to distinguish them. We can now add a clause to the precondition of each transition in component p that makes the executability of the transition dependent on the truth if: exclusive $\equiv 0 \lor$ exclusive $\equiv p$. pid. The first transition in each atomic sequence in component p now gets an extra side effect exclusive = p. pid, and the last transition gets an extra side effect exclusive = 0. These few changes suffice to produce the desired semantics.
Rendezvous

PROMELA also has a notion of synchronous rendezvous that is not directly addressed by Definition A.1. These types of operations can also be encoded within the given framework with relatively little effort.

In a rendezvous event, matching send and receive operations from different processes meet in a single event that is executed atomically. Since we do not have simultaneous executions, we must be able to secure in some other way that synchronous send and receive operations indeed execute atomically in that order.

One way to accomplish this is to define another special global integer data object, call it handshake, with initial value 0. Each rendezvous port in the system is now assigned a unique positive integer number.

We now again add some new clauses to the preconditions of transitions in the system. For all receive operations on rendezvous port i, this extra condition is handshake \(\equiv i\), to restrict the states in which they are enabled to those in which a rendezvous operation on port i has been initiated. For all non-rendezvous transitions, and all send operations on rendezvous ports, the extra clause is handshake \(\equiv 0\), to prevent their execution when a rendezvous action on any queue is currently in progress.

Next, we add some side effects to the transitions that correspond to rendezvous send or receive operations. For each send operation on rendezvous port i, we add the side effect handshake = i, and to each rendezvous receive operation we add the side effect handshake = 0.

The additions guarantee that as long as handshake \(\equiv 0\), all transitions, except the receive halves of rendezvous operations, are executable as before. Whenever the send half of a rendezvous operation is initiated, however, the value of handshake becomes positive, and it allows only a matching receive handshake to take place. Once that happens, the value of handshake returns to its default initial value. (In the SPIN implementation this handshake variable is called boq, which was originally chosen as an acronym for "blocked on queue.")
Synchronous Products

The synchronous product of two finite state automata is defined as follows:

**Definition A.2 (Synchronous Product)**

The synchronous product of finite state automata P and B is a finite state automaton $A = (S, s_0, L, T, F)$, where

- **A. $S$** is the Cartesian product $P' \times B. S$, where $P'$ is the stutter-closure of $P$ in which a nil self-loop is attached to every state in $P$ that has no successor,

- **A. $s_0$** is the tuple $(P. s_0, B. s_0)$,

- **A. $L$** is $P'. L \times B. L$,

- **A. $T$** is the set of pairs $(t_1, t_2)$ such that $t_1 \in P'. T$ and $t_2 \in B. T$,

- **A. $F$** is the set of pairs $(s_1, s_2) \in A. S$ where $s_1 \in P. F \lor s_2 \in B. F$.

The intuition expressed here is that one of the two automata, say, automaton B, is a standard Büchi automaton that is, for instance, derived from an LTL formula, or directly given as a PROMELA never claim. As in Definition A.1, we again assume that sets of final states $P. F$ and $B. F$ in the component automata are identical to the corresponding sets of acceptance states $P. A$ and $B. A$.

The main difference between an asynchronous and a synchronous product is in the definition of sets $L$ and $T$. In a synchronous product, the transitions in the product automaton correspond to joint transitions of the component automata. The labels on the transitions now also consist of two parts: the combination of the two labels from the original transitions in the components. The semantics of a combination of two labels is defined in SPIN as the logical and combination of the preconditions of the two original statements, and the concatenation of the two actions. (Hence, $P \otimes B$ is not necessarily the same as $B \otimes P$.) When SPIN computes the synchronous product of a system and a claim automaton, the labels in the claim automaton B define only conditions (i.e., state properties) and no actions. Since one of the actions is always nil, the catenation of actions from the two automata is now independent of the ordering, and we have $P \otimes B \equiv B \otimes P$. 

An Example

Consider the PROMELA model of two asynchronous processes and a never claim derived from the LTL formula $<>[]p$, shown in Figure A.1.

**Figure A.1 Example PROMELA Model**

```c
#define N 4
#define p (x < N)
int x = N;

active proctype A()
{
    do
    :: x%2 -> x = 3*x+1
    od
}

active proctype B()
{
    do
    :: !(x%2) -> x = x/2
    od
}

never {    /* <>[]p */
    T0_init:
    if
    :: p -> goto accept_S4
    :: true -> goto T0_init
    fi;
    accept_S4:
    if
    :: p -> goto accept_S4
    fi;
}
```

The control-flow graph of each of these three components can be formalized as a finite state automaton, as illustrated in Figure A.2.

**Figure A.2. Finite State Automata A1, A2, and B**

The full asynchronous product of A1 and A2 is shown in Figure A.3. The states in the product automaton have been marked with pairs of statenames $p$, $q$ with $p$ the name of the corresponding state in component automaton A1, and $q$ the corresponding state in component automaton A2. State $s_0$, $s_0$ is the initial state. Since neither A1 nor A2 contained accepting states, the product automaton has no accepting states either.

**Figure A.3. Asynchronous Product of A1 and A2**

The initial state of the product is $s_0$, $s_0$. If we apply PROMELA semantics and interpret the labels on the transitions, it is clear that all paths leading into state $s_1$, $s_1$ are infeasible, since they require both the condition (x%2) and its negation to evaluate to true without an intervening change in the value of x. State $s_1$, $s_1$ is therefore effectively unreachable under the intended label semantics.

Applying PROMELA semantics, we can compute the expanded version of the asynchronous product from Figure A.3 (fully expanding all possible values of integer data object x) which can now be interpreted as a pure finite state automaton. This automaton is shown in Figure A.4. The states are marked with a triple $p$, $q$, $v$, with $p$ and $q$ referring to the states of component automata A1 and A2 as before, and $v$ giving the integer value of variable x at each state.

**Figure A.4. Expanded Asynchronous Product for Initial Value x = 4**

The synchronous product of the automaton in Figure A.4 and the property automaton B is illustrated in Figure A.5.

**Figure A.5. (Expanded) Synchronous Product of Figure A.4 and Automaton B**

The states are now marked with a tuple $p$, $q$, $v$, $r$, with the first three fields matching the markings from Figure A.4, and the last field recording the state from component property automaton B. All transitions in the automaton from Figure A.5 are now joint transitions from the automaton in Figure A.4 and the property automaton B. The transitions from B are not explicitly indicated in Figure A.5, since they will be clear from context. All transitions in the top half of the figure correspond to self-loop labeled true on B. $s_0$; all transitions in the bottom half similarly correspond to the self-loop labeled $x < 4$ on B. $s_1$, and all transitions between top and bottom half correspond to the transition from B. $s_0$ to B. $s_1$ labeled $x < 4$ in B. Note that some transitions are not possible, and not drawn in the figure, because the property automaton B forbids them once it has reached state B. $s_1$.

If the automaton in Figure A.5 allows any $\omega$-accepting runs, they correspond to executions that satisfy the LTL formula $<>[]p$. The automaton has four reachable accepting states, but it is easy to see that none of these states is reachable from themselves (i.e., part of a cycle or a strongly connected component in the reachability graph). Hence, the sample PROMELA model we started this example with does not satisfy the LTL formula given.
Non-Progress Cycles

SPIN uses a simple mechanism to encode the detection of non-progress cycles in terms of standard Büchi acceptance, thus avoiding the need for a special algorithm. When the verifier sources are compiled with the directive -DNP, a predefined never claim is included in the model that corresponds to the LTL formula ($\Diamond \Box \neg p_\neg$), which states that it is impossible for the system to eventually ($\Diamond$) reach a point its execution from which it always ($\Box$) traverses only non-progress ($\neg p_\neg$) states (cf. page 447).

In a synchronous or asynchronous product of component automata, the product automaton is considered to be in a progress state if and only if at least one of the component automata is in a progress state (that is, a state within set A_P as defined on page 554). A never claim in PROMELA syntax corresponding to the predefined formula can be written as follows:

```promela
never { /* <>[] np_ */
    do
        :: np_ -> break
        :: true
    od;
accept:
    do
        :: np_ od
}
```

This claim defines a non-deterministic Büchi automaton. Note, for instance, that in the initial state of the automaton the option true is always executable. The only accepting runs are the infinite runs in which eventually no more progress states are reached. The true self-loop in the initial state allows the automaton to remain in its initial state for an arbitrary number of initial steps in the run. When a non-progress state is reached, the automaton can, but need not, switch to its accepting state. It is, for instance, possible that the first few non-progress states encountered in a run do not immediately lead to a point in the run where a return to a progress state is impossible. The structure of the automaton as given allows us to skip over such states, in a hunt for the real violations.
Deadlock Detection

Absence of deadlock is a system property that cannot be expressed directly in LTL, and hence it does not easily fit within the standard framework of $\omega$-automata that we have sketched here.

To define a notion of acceptance that captures precisely the set of deadlocking runs of a finite state automaton, we have to reconsider the definitions of set $A. F$ for the asynchronous and synchronous product computations.

To do so, we start with the assumption that set $A. F$ in each component automaton is now defined to contain only the normal termination state of automaton $A$ (i.e., the state that corresponds to the point immediately before the closing curly brace of a PROMELA proctype or never claim body declaration).

For the asynchronous product, we now redefine the set of final states $A. F$ from Definition A.1 as follows, using the definition of $A. E$ that was given on page 554:

$$ A. F_\text{s} \text{ is the subset of those elements of } A. S \text{ that satisfy } \forall (A_1. s, \ldots, A_n. s) \in A. F, \exists i, (s \in A_i. F \lor \forall s \in A_i. E), \text{ further, we require that } \forall (s, i, t) \in A. T, s \not\in A. F. $$

That is, the product state is in set $A. F$ if and only if all component automata are either in their normal termination state, or in a specially marked end state, and further if the state has no successors. This precisely captures the notion of an invalid end state, which is SPIN's formalization of a system deadlock state.

We can do something similar for Definition A.2. Note that we may still want to make use of the SPIN machinery to compute synchronous products also if we perform a verification of only safety properties, because we can make good use of never claims as a pruning device: the never claim can be used to restrict a verification run to a subset of behaviors that is deemed to be of primary interest.

To make this possible, it suffices to redefine the set of final states of a synchronous product from Definition A.2 as follows:

$$ A. F_\text{s} \text{ is the set of pairs } (s_1, s_2) \in A. S \text{ where } s_1 \in P. F. $$

The only change from the version used in Definition A.2 is that the criterion for determining if a state is in $A. F$ now uniquely depends on the system automaton $P$, and is independent of the state of the never claim (i.e., Büchi automaton $B$).
Appendix B. The Great Debates

"It is not necessary to understand things in order to argue about them."
—(Pierre Augustin Caron de Beaumarchais, 1732–1799)

Quite a few issues in formal verification have sparked heated debates over the years, without ever coming to a clear resolution. Perhaps the first such issue came up when temporal logic was first being explored, in the late seventies, as a suitable formalism for reasoning about concurrent systems. The issue was whether it was better to use a branching-time or a linear-time logic. Much later, the debate was between symbolic or explicit verification methods. Many of these issues directly relate to design decisions that have to be made in any verifier, including SPIN. We discuss the more important ones here, briefly motivating the rationale for the choices that were made in the design of SPIN. The issues we discuss are:

- Branching Time versus Linear Time
- Symbolic Verification versus Explicit Verification
- Breadth-First Search versus Depth-First Search
- Tarjan's SCC Algorithms versus SPIN's Nested Depth-First Search
- Events versus States
- Realtime Verification versus Timeless Verification
- Probabilities versus Possibilities
- Asynchronous Systems versus Synchronous Systems
- Interleaving Semantics versus True Concurrency
- Open versus Closed Systems
Branching Time vs Linear Time

The two main types of temporal logic that are used in model checking are CTL, short for Computation Tree Logic, and LTL, short for Linear Temporal Logic. CTL is a branching time logic, and is almost exclusively used for applications in hardware verification. LTL is a linear time logic, and is almost exclusively used for applications in software verification. The main issues that have been debated concern the relative expressiveness of the two logics and the relative complexity of verification.

Perhaps one reason why the debate has persisted for so long is that the two logics are not really comparable: their expressiveness overlaps, but each logic can express properties that are outside the domain of the other. The standard examples that are used to illustrate the difference are that LTL can express fairness properties and CTL cannot, but CTL can express the so-called reset property and LTL cannot. Fairness properties are often used as constraints on cyclic executions, stating, for instance, that every cyclic execution either must traverse or may not traverse specific types of states infinitely often. The reset property expresses that from every state there exists at least one execution that can return the system to its initial state. Not surprisingly, this type of property is more important in hardware than in software specifications. The overlap between CTL and LTL is sufficiently broad that most properties of interest can easily be expressed in both logics. A notion of fairness, though not expressible in CTL, can be embedded into the verification algorithms, so this is also not much of an issue.

This leaves the issue of complexity, which continues to be a source of confusion. The main argument here is based on an assessment of the theoretical worst-case complexity of verifying either CTL or LTL formulae. Consider a system with \( R \) reachable states and a formula of "length" \( n \), where the length of a formula is the number of state subformulae it contains. The standard procedure for CTL model checking can visit every reachable state up to \( n \) times, giving a worst-case complexity of \( O(R \cdot n) \). The standard procedure for LTL model checking, however, first requires the conversion of the LTL formula into an \( \omega \)-automaton of, say, \( m \) states, and then computing the synchronous product of that automaton and the system, which in the worst case can be of size \( R \cdot m \). This gives a complexity of \( O(R \cdot m) \). The focus of the argument is now that in the worst case \( m \) can be exponentially larger than \( n \). This argument leads to the statement that CTL model checking is "of linear complexity," while LTL model checking is "of exponential complexity." Those who read this and try to find a significant difference between the run-time or memory requirements of CTL model checkers and LTL model checkers are often surprised: there is no such difference and in many cases LTL model checkers like SPIN have been shown to significantly outperform CTL model checkers when presented with the same verification problem. So what is going on?

Let us first consider the worst-case complexity of converting an LTL formula into an \( \omega \)-automaton. As a simple example, consider the formula \([[(p -> (q U r))]\). The CTL equivalent \([1]\) of this formulae is \(AG((!p) || A(q U r))\), where \( A \) is the universal path quantifier, \( G \) is the equivalent of the LTL box operator \([\]\), and || is the logical or operator. There are six state subformulae (properties that can be true or false in any given state): \( p, q, r, A(q U r), (\langle p \rangle || A(q U r)), \) and \( AG((!p) || A(q U r))\). The standard CTL model checking algorithm marks each system state with the truth value of the propositional symbols \( p \) and \( q, r \) in a first pass, and then in three new passes it will mark those states in which the remaining state subformulae hold. In the worst case, this requires four visits to each state.

[1] The equivalence assumes that there are no states without outgoing transitions in the system being verified.

The worst-case \( \omega \)-automaton generated from the LTL version of the formula would have \( 2^6 = 64 \) states. A good implementation of an LTL converter, however, generates an equivalent \( \omega \)-automaton of only two states. The size of the synchronous product of this automaton and the system is somewhere between \( R \), the original system size, and \( 2 \cdot R \). With SPIN's nested depth-first search algorithm, in the worst case we would visit every state four times to perform the verification. Whether the CTL verification method or the LTL verification method performs better depends entirely on the unpredictable specifics of the system structure being verified: there is no predetermined winner.

A few things are worth observing.

1. The worst-case behavior of LTL converters is rare. In most cases, the converters perform significantly better than worst-case.

2.
Symbolic Verification vs Explicit Verification

Symbolic verification algorithms, or BDD-based methods, offer an ingenious strategy to combat state-space explosion problems. They are, of course, not the only such strategy, but in the domain of hardware verification they are often extremely effective. When applied to software verification problems, they tend to perform more poorly, but in that domain strategies such as partial order reduction often perform exceptionally well. There are no guarantees in either domain, though. The performance of the symbolic verification methods depends critically on the variable ordering that is chosen for the BDDs. Choosing an optimal variable ordering is an NP-complete problem, so in practice only heuristic methods are used. Similarly, in applications of partial order reduction methods, computing the optimal reduction is an NP-complete problem, so heuristics are used here as well. The method implemented in SPIN, for instance, is based on a fairly conservative static approximation of data independence relations that tends to give the majority of the benefits of the reduction at a very small run-time cost.

Because of the conservative approximation used in SPIN, it is hard to construct a case where a verification attempt with partial order reduction enabled behaves worse than one without it. The difference in even the worst case is limited to a few percent of run-time. With the use of BDDs in hardware verification, the odds are less favorable. Undeniably, the best-case performance of these methods is outstanding, but it is relatively easy to find or construct cases where the symbolic verification methods behave significantly worse than explicit state methods. Worse still, it is often unpredictable when this happens, and there is very little that can be done about it when it is encountered (short of solving the NP-hard problem of variable ordering).

When symbolic verification and partial order reduction methods are compared, some popular statistics tend to be misused a little. The memory use of a BDD-based method is ultimately determined by the number of nodes in the BDD structures, and for an explicit state method it is determined by the number of states stored. It can be very misleading, though, to compare the number of potentially reachable states that is captured by a BDD structure with the number of states that is explored with an explicit state method based on partial order reduction. First, of course, potentially reachable does not mean effectively reachable. Secondly, and more importantly, the states explored in an explicit search based on partial order methods are equivalent to a possibly exponentially larger set of effectively reachable states. It is the very purpose of the partial order reduction method to make this difference as large as possible. If memory use is compared between the two methods, the only valid metric is to compare true memory use: bytes. The results of such comparisons can be very surprising, and can contradict the artificial counts that are meant to show a disproportionally large benefit for symbolic methods.

Neither method is necessarily superior to the other. Some trends seem fairly generally agreed upon, though. Within the domain of software verification, partial order methods tend to give better performance, and within the domain of hardware verification, the symbolic methods tend to perform better. There are reasons for the difference. Binary or boolean data, often bit-vectors, tend to dominate in hardware verification problems: structures that favor BDD representations. More complex, and highly correlated, higher-level data structures tend to dominate in software verification problems, and are not easily exploited with BDDs. Asynchronous process execution tends to dominate in software applications, a phenomenon exploited by partial order techniques; while synchronous, clocked, operation is more the rule in hardware applications, not easily exploited by partial order reduction.
Breadth-First Search vs Depth-First Search

Perhaps even an older point of debate is whether, in explicit state model checkers, it is better to use a breadth-first or a depth-first discipline as the default search algorithm. SPIN uses depth-first search as its default algorithm, and contains a breadth-first search only as a user-defined option, which is effective only for safety properties. The main advantage of a breadth-first search algorithm is that for safety properties it can find the shortest path to an error state, while the depth-first search often finds a longer path. For liveness properties, or properties of infinite sequences, the advantages disappear. There are two well-known and efficient variants of the depth-first search that can be used to demonstrate the existence of strongly connected components in a reachability graph: Tarjan's classic depth-first search algorithm, and the more recent nested depth-first search method that is implemented in SPIN.

We can think of a variant of the nested depth-first search method that is based on breadth-first search. Starting the breadth-first search from the initial system state, we proceed with the search normally. Each accepting state found in this process would be placed on a special watch list. We are interested in identifying at least one accepting state that is reachable from itself. To solve that problem is harder. We can consider performing a second breadth-first search (the nested search step) from each of the states on the watch list, but an essential property of the nested depth-first search is missing: the second search can no longer be done in post-order. Therefore, we may need to create as many copies of the state space as there are reachable accepting states. This increases the worst-case complexity of the search from linear to quadratic.

Quite apart from this technical problem in constructing an effective algorithm for proving liveness properties with a breadth-first search, is the issue of memory requirements. Even if we could manage to restrict the state space to just a single copy of each reachable state, we no longer have the depth-first search stack to fall back on for reconstructing counterexample error paths. The breadth-first search needs a queue to store each new generation of states that are to be explored further, which fulfills a similar role as the stack in a depth-first search. To be able to construct error paths, though, the breadth-first search needs to store links (pointers) at each state, pointing to at least one of the state's predecessors in the reachability graph. Each such pointer takes at least 32-bits of memory. The nested depth-first search method does not need to store such links between states, trading the inconvenience of longer error paths for a savings in memory.

SPIN has an option to find a shorter error path that is based on depth-first search that works for both safety and liveness properties. In this variant of the search we store with each reachable state also the distance from the initial system state at which that state was found. If a shorter path to the state is found later in the search, its successors are re-explored, up to a user-defined maximum search depth. Clearly, finding the shortest possible error path is almost always more expensive than just plain proving the existence any error path.
Tarjan Search vs Nested Search

The automata theoretic verification procedure as implemented in SPIN relies on our ability to detect the presence of infinite accepting runs in a finite reachability graph. The classic way of doing so would be to use Tarjan's depth-first search algorithm to construct the strongly connected components of the graph, and then analyze each such component for the presence of accepting states. The memory and time requirements of this procedure are well-known. In the worst case, we may have to visit every reachable state twice: once to construct the reachability graph, and once in the analysis of a strongly connected component. The storage requirements for each reachable state increase with two, typically 32-bit wide, integer values: one to store the so-called depth-first number and one to store the lowlink number. Further, to be able to reconstruct an accepting path through a strongly connected component, at least one 32-bit pointer to a predecessor state would need to be stored at each reachable state, bringing the total to three 32-bit values of overhead per state. The benefit of Tarjan's algorithm is clearly that it can produce all accepting runs.

The innovation of the nested depth-first search algorithm lies in the fact that it is not necessary to produce all accepting runs. The search is set up in such a way that an accepting run corresponds to a counterexample of a correctness claim. Any one counterexample suffices to invalidate the claim. The nested depth-first search algorithm has the property that it is able to detect at least one accepting run, if one or more such runs exist. It does so at the same worst-case time complexity (maximally visiting every state twice), but at a lower memory overhead. Only two bits of memory need to be added to each state, instead of three 32-bit values. No pointers between states need to be stored, making it possible to also support very memory-frugal approximation algorithms such as the supertrace or bitstate hashing method, which are among SPIN's main features.

One point in favor of Tarjan's algorithm is that it makes it easier to implement a range of different fairness constraints, including the strong fairness option that is currently not supported by SPIN.
Events vs States

SPIN is an explicit state model checker. To perform verification, the system builds a global state reachability graph, which can be stored in various ways in memory. The focus on states, rather than transitions or events, also extends to the way in which correctness properties are formalized. A correctness property, such as a temporal logic formula, is built up from simple boolean properties of system states. That means, to express the property that after an off-hook event a telephone subscriber will always receive a dial tone signal, we have to find a way to express the occurrence of the related events as state properties, rather than directly as events. An off-hook condition, for instance, will likely be registered somewhere in a status field, and similarly the generation of dial tone by the system will be recorded somewhere. This strict adherence to the notion of a state as the single mechanism to support correctness arguments is sometimes clumsy. For instance, we may want to state the correctness property that always within a finite amount of time after the transmission of a message the message will be received at its destination. Clearly, the state of a message channel will change as a result of both types of events, provided that the message is sent through a buffered channel. If send and receive events are rendezvous handshakes, however, it becomes much harder, and we have to find more subtle ways of recording their execution in a way that is observable to SPIN during verification.

In principle, it would be possible to switch to a purely event-based formalism for expressing correctness requirements. That too would have limitations, because many types of properties lend themselves more easily to state-based reasoning. A hybrid approach may be the most attractive, shifting some of the ensuing complexity into the model checker itself. To date, we have not explored this extension for SPIN yet.
Realtime Verification vs Timeless Verification

One of the most frequently asked questions about SPIN concerns the preferred way of modeling time. Verification of system properties is based on the fundamental assumption that correctness should be independent of performance. As Edsger Dijkstra first articulated, under no circumstances should one let any argument about the relative speed of execution of asynchronous processes enter into correctness arguments. PROMELA has only a rudimentary way for modeling the concept of a timeout, through the use of a predefined and read-only global boolean variable named timeout. The timeout variable is true only when all processes are simultaneously blocked, and it is false otherwise. This allows us to model the functional intent of a timeout condition: it takes effect to relieve the system from an apparent hang state. There is a pleasing analogy with the predefined read-only local boolean variable else in PROMELA (yes, this is a variable, and not a control-flow keyword, as in most implementation languages). The else variable becomes true only when the process that contains it cannot make any other transitions.

If we replace an occurrence of timeout with skip we can capture the assumption that timeouts may also happen when the system is not actually stuck, and we can verify the validity of our correctness claims under those much more severe conditions. Generally, though, this will cause a flood of pseudo error scenarios that are of only marginal interest to a designer. All this reinforces the notion that SPIN is not meant to be used as a performance analysis tool.

There are indeed algorithms for doing real-time analysis with model checkers, but the penalty one pays for this additional functionality is almost always severe: typically an increase in computational complexity of several orders of magnitude. By focusing on only functional and logical correctness issues, SPIN can gain significant efficiency, and handle a broader class of problems.
Probability vs Possibility

This issue is very similar to the previous one. It is possible to modify the standard model checking algorithms to take into account a notion of probability. One could, for instance, tag the options in every selection construct with relative probabilities to indicate their relative likelihood of occurrence.

There are many problems with this approach. First, it can increase the verification complexity, depriving us of the ability to verify properties of larger systems. Second, it can be difficult to correctly interpret the results of a verification run that is based on probability estimates. We could, for instance, compute the combined probability of occurrence of an error scenario, but that would be meaningless as a metric. Almost all error scenarios, including the devastating ones that can cause huge damage, have an exceedingly low probability of occurrence. Errors almost always have a low probability of occurrence, since the normal design practices will easily shake out the higher probability bugs. It is the very goal of model checking to find the low probability scenarios that cause systems to fail. It would be a grave error to restrict a verification to only higher probability behaviors. Finally, it can be hard to come up with a realistic estimate for the relative probability of different options for execution. More often than not, if such tags have to be assigned, they will be guessed, which undermines the validity of the verification process.
Asynchronous Systems vs Synchronous Systems

Most hardware model checkers have adopted a synchronous view of the world where in principle all process actions are clock-driven. In such a system, at every clock-tick every process takes a step. One can model asynchronous process behavior in such systems by including a non-deterministic pause option at every move in every process. At each step, then, a process can choose to either pause or to advance with its execution. SPIN is one of the few systems that adopts an asynchronous view of the world. Since in a distributed system different processes cannot see each other’s clock (and clock synchronization in a distributed system is actually a pretty difficult task in its own right), the speed of execution of processes is fundamentally asynchronous and cannot be controlled by any device or process: it is beyond the control of the programmer, just like it is in the real world of distributed computing.

This choice has both advantages and disadvantages. The main disadvantage is that it is hard to model synchronous system behavior with an asynchronous model checker. Then again, it is precisely the point of the choice to make this hard, so this is not too surprising. Yet it does, for all practical purposes, eliminate SPIN as an effective candidate for doing hardware verification. There are very good systems for addressing that problem, so this is not a significant loss.

Apart from a better fit for the types of design problems that SPIN targets, there is also an unexpected benefit of adopting the asynchronous view of the world: greater verification efficiency. Assume a model with N asynchronous processes. Modeling these processes in a synchronous tool with non-deterministic pause transitions to emulate asynchronous behavior incurs an N-fold overhead: at every step the model checker must explore N additional pause transitions compared to the SPIN-based graph exploration. This efficiency argument, though, applies only to explicit state verification methods; it disappears when symbolic verification algorithms are used.
Interleaving vs True Concurrency

Sometimes a distinction is made between true concurrency semantics and the interleaving semantics we have described. In addition to the interleaving of actions, a true concurrency semantics allows also for the simultaneous execution of actions. In Definition A.1 (p. 554), this would mean the introduction of many extra transitions into set $T$ of the product automaton, one extra transition for each possible combination of transitions in the component automata.

In distributed computer systems, it is indeed possible that two asynchronous processes execute actions in the same instant of time, at least as far as could be determined by an outside observer. To see how such events can be modeled, we must consider two cases.

First, consider the case where the process actions access either distinct data objects, or none at all. In this case, the simultaneous execution of these actions is indistinguishable from any arbitrarily chosen sequential interleaving. The interleaving semantics, then, gives a correct representation. The addition of the simultaneous transitions cannot add new functionality.

Secondly, consider the case where two or more process actions do access a shared data object. Let us first assume that the object is a single entity that resides at a fixed location in the distributed system, and is accessed by a single control unit. That control unit obviously can do only one thing at a time. At some level of granularity, the control unit will force an interleaving of atomic actions in time. If we pick the granularity of the actions that are defined within our labeled transition systems at that level, the interleaving semantics will again accurately describe everything that can happen.

But, what if the data object is not a single entity, but is itself distributed over several places in the distributed system where it can be accessed in parallel by different control units? Also in this case, the same principles apply. We can represent the data objects in our automata model at a slightly lower level of granularity, such that each distinct data object resides in a fixed place.

The important thing to note here is that automata are modeling devices: they allow us to model real-world phenomena. The theoretical framework must allow us to describe such phenomena accurately. For this, interleaving semantics offer the simplest model that suffices.
Open vs Closed Systems

Traditionally, model checking is based on two requirements: the model must be finite and it must be closed. The benefit of the finiteness assumption will need few words here, although it does mean that we can only reason about infinite state systems if we can make finitary abstractions of them.

To be closed, a model must include all possible sources of input and it must include explicit descriptions of all process behaviors that could affect its correctness properties. The most often quoted benefit of an open systems description, where not all elements of a system are necessarily specified, is that of convenience. In most cases, though, it is not very hard to extend a system's model with a minimal set of worst case assumptions about the environment in which it is meant to execute. These worst case assumptions can effectively match the defaults that would be presumed in an open systems model.

In the design phase, it can be quite helpful to a designer to focus explicitly on the otherwise hidden assumptions. There is also significant extra power in the use of a closed systems model. The designer can, for instance, modify the environment assumptions to see what effect they can have on critical correctness properties. The assumptions can also be used to focus a verification task more precisely on the correct operation of a system under a specific set of conditions. The convention of working with closed system models, finally, naturally matches a standard assume-guarantee style of reasoning.
Appendix C. Exercises With SPIN

"I hear and I forget; I see and I remember; I do and I understand."

—Confucius, 551–479 BC
C.1.

How many reachable states do you predict the following PROMELA model will generate?

```pexpla
init { /* example ex1 */
    byte i = 0;
    do
        i = i+1
    od
}
```

Try a simulation run:

```
$ spin -p -l -u100 ex1
```

Will the simulation terminate if the -u100 argument is omitted? Try it.
C.2.

Estimate the total number of reachable states that should be inspected in an exhaustive verification run. Is it a finite number? Will a verification run terminate? Try it as follows, and explain the result.

$ spin -a ex1
$ cc -o pan pan.c
$ ./pan
C.3.

What would happen if you had declared local variable \( i \) to be a short or an int instead of a byte?
Predict accurately how many reachable states there are for the following model. Write down the complete reachability tree for \( N \) equal to two, as specified.

```c
#define N 2

init { /* example ex2 */
    chan dummy = [N] of { byte };
    do
        :: dummy!85
        :: dummy!170
    od
}
```

Check your prediction by generating, compiling, and running the verifier as follows:

```
$ spin -m -a ex2
$ cc -o pan pan.c
$ time ./pan
```

(Option -m defines that messages appended to a full buffer are to be lost.)
C.5.

What happens to the number of reachable states if you set N to three? Express the number of states as a function of N. Use the formula to calculate how many states there will be if you set N equal to 14. Check your prediction by running the verification, and write down:

T: the sum of user time plus system time for the run,

S: the number of states stored in the state space,

G: the number of total number of states generated and analyzed,

V: the vector size, that is, the state descriptor size, which is the amount of memory needed to store one state.

Compute G/T as a measure for the efficiency of the run. The product of S and V gives you the minimal amount of memory that was needed to store the state space. This is of course not the only place where memory is used during a verification (the stack, for instance, also consumes memory), but it is often the largest memory requirement.

The efficiency of a standard exhaustive verification run is determined by the state space storage functions. To study this, repeat the last run first with a smaller and then with a bigger hash table than the predefined default:

```
$ time ./pan -w10  # hash table with 2^10 slots
$ time ./pan -w20  # hash table with 2^20 slots
```

Explain the results. [Hint: Compare the number of hash conflicts.]
C.6.

Estimate how much memory you would need to do a run with $N$ equal to 20? (Warning: Both the number of reachable states and the number of bytes per state goes up with $N$. Estimate about 30 bytes per state for $N$ equal to 20.) If you have about 8 Megabytes of physical memory available to perform the verification, what maximal fraction of the state-space would you expect to be able to reach?

Now set $N$ to 20 and perform a bitstate verification, as follows:

```
$ spin -m -a ex2
$ cc -DBITSTATE -o pan pan.c
$ time ./pan
```

If you did the calculation, you probably estimated that there should be 2,097,151 reachable system states for $N$ equal to 20. What percentage of these states was reached in the bitstate run? How much memory was used? Compare this to the earlier estimated maximal coverage for a standard exhaustive verification and explain the difference.
C.7.

The default state space in the bitstate verification we performed in the last exercise allocates a hash array of 222 bits (i.e., one quarter Megabyte of memory). Repeat the run with larger amount of memory and check the coverage. Check what percentage of the number of states is reached when you use the 8 Megabyte state space on which your first estimate for maximal coverage in a full state space search was based (223 bytes is 226 bits, which means a run-time flag -w26). You should be able to get reasonably good coverage and between 40,000 and 400,000 states stored per second, depending on the speed of the machine that is used. Note that the actual number of states reached is about twice as large as the number of states stored in this experiment: The number of states reached equals the number of transitions that were executed.

On a 2.5 GHz Pentium 4 Windows PC, for instance, the run reaches 99% coverage at a rate of 400,000 states per second.

```bash
$ spin -a ex2
$ cl -DPC -DSAFETY -O pan.c
$ time ./pan -w26
(Spin Version 4.0.7 -- 1 August 2003)
  + Partial Order Reduction

Bit statespace search for:
  never claim             - (none specified)
  assertion violations    +
  cycle checks            - (disabled by -DSAFETY)
  invalid end states      +

State-vector 38 byte, depth reached 20, errors: 0
2.07474e+006 states, stored
2.07474e+006 states, matched
4.14948e+006 transitions (= stored+matched)
  0 atomic steps
2.07223e+006 lost messages
hash factor: 32.3456 (expected coverage: >= 98% on avg.)
(max size 2^26 states)

Stats on memory usage (in Megabytes):
  87.139  equivalent memory usage for states
  16.777  memory used for hash array (-w26)
  0.280   memory used for DFS stack (-m10000)
  17.262  total actual memory usage

unreached in proctype :init:
  line 8, state 6, "-end-
   (1 of 6 states)

real    0m5.247s
user    0m0.015s
sys     0m0.000s
$
```

If enough memory is available, also perform an exhaustive (non-bitstate) verification and compare the total actual memory usage for the two runs.
C.8.

How many states should the following program generate?

```c
#define N 20

int a;
byte b;

init {
    do
        :: atomic { (b < N) ->
            if
                :: a = a + (1<<b)
                :: skip
            fi;
        b=b+1 } od

```

Run a bitstate analysis, using the command

```
$ time ./pan -c0 -w26
```

and explain all numbers reported.
It is often much easier to build a little validation model and mechanically verify it than it is to understand a manual proof of correctness in detail. Petri Nets are relatively easy to model as PROMELA validation models. A PROMELA model for the net in **Figure C.1**, for instance, is quickly made.

**Figure C.1. Petri Net with Hang State**

![Petri Net Diagram]

```c
#define Place   byte      /* < 256 tokens per place */

Place p1, p2, p3;
Place p4, p5, p6;

#define inp1(x)           (x>0) -> x--
#define inp2(x,y)         (x>0&&y>0) -> x--; y--
#define out1(x)           x++
#define out2(x,y)         x++; y++

init
{       p1 = 1; p4 = 1; /* initial marking */

do
  /*t1*/  :: atomic { inp1(p1)    -> out1(p2) }
  /*t2*/  :: atomic { inp2(p2,p4) -> out1(p3) }
  /*t3*/  :: atomic { inp1(p3)    -> out2(p1,p4) }
  /*t4*/  :: atomic { inp1(p4)    -> out1(p5) }
  /*t5*/  :: atomic { inp2(p1,p5) -> out1(p6) }
  /*t6*/  :: atomic { inp1(p6)    -> out2(p4,p1) }
  od
}
```

For this exercise, consider the following PROMELA model of a Petri Net taken from a journal paper that was published in 1982 and proven to be deadlock-free in that paper with manual proof techniques.

```c
#define Place   byte      /* < 256 tokens per place */

Place P1, P2, P4, P5, RC, CC, RD, CD;
Place p1, p2, p4, p5, rc, cc, rd, cd;

#define inp1(x)         (x>0) -> x--
#define inp2(x,y)       (x>0&&y>0) -> x--; y--
#define out1(x)         x++
#define out2(x,y)       x++; y++

init
{       P1 = 1; p1 = 1; /* initial marking */

do
  /*t1*/  :: atomic { inp1(P1)    -> out2(rc,P2) }
  /*t2*/  :: atomic { inp2(P2,CC) -> out1(P4)    }
  /*t3*/  :: atomic { inp1(P4)    -> out2(P5,rd) }
  /*t4*/  :: atomic { inp2(P5,CD) -> out1(P1)    }
  /*t5*/  :: atomic { inp2(P1,RC) -> out2(P4,cc) }
  /*t6*/  :: atomic { inp2(P4,RD) -> out2(P1,cd) }
  /*t7*/  :: atomic { inp2(P5,RD) -> out1(P1)    }
  /*t8*/  :: atomic { inp1(p1)    -> out2(RC,p2) }
  /*t9*/  :: atomic { inp2(p2,cc) -> out1(p4)    }
  /*t10*/ :: atomic { inp1(p4)    -> out2(p5,RD) }
  /*t11*/ :: atomic { inp2(p5,cd) -> out1(p1)    }
  /*t12*/ :: atomic { inp2(p1,rc) -> out2(p4,CC) }
  /*t13*/ :: atomic { inp2(p4,rd) -> out2(p1,CD) }
  /*t14*/ :: atomic { inp2(p5,rd) -> out1(p1)    }
  od
}
```

See if SPIN can find a deadlock in the model.
Appendix D. Downloading Spin

"On two occasions I have been asked, 'Pray, Mr. Babbage, if you put into the machine wrong figures, will the right answers come out?' I am not able rightly to apprehend the kind of confusion of ideas that could provoke such a question."

—(Charles Babbage, 1792–1871)

SPIN can be run on most systems, including most flavors of UNIX and Windows PCs. The only strict requirement is the availability of a standard, ANSI compatible, C preprocessor and compiler. If these programs are not already installed on your system, good quality public domain versions can be readily found on the Web. A recommended source for these tool, plus a host of other UNIX applications, is

http://www.cygwin.com

Instructions for installing SPIN, documentation, test cases, and the complete set of SPIN sources, are maintained and kept up to date at

http://spinroot.com/spin/index.html

The SPIN package has been freely available in this form since 1991. Officially, the SPIN sources are not considered to be in the public domain, since they are protected by a copyright from Bell Labs and Lucent Technologies. In effect, though, the software is very widely distributed and for all practical purposes treated as freeware. The tool is used for educational purposes, for research in formal verification, and has found considerable use in industry.

Commercial use of SPIN requires the acceptance of a standard license agreement from Bell Labs, which can be done by clicking an accept button, and entering some contact information, at URL

http://cm.bell-labs.com/cm/cs/what/spin/spin_license.html

The commercial license also requires no fees. SPIN continues to evolve, with new releases appearing every few months. The changes made in each new release of the tool—bug fixes, extensions, and revisions—are documented in update files that are part of the distribution.

Perhaps the best way to stay up to date on new developments related to SPIN is through the SPIN Workshop series. International SPIN Workshops have been held annually since 1995. The proceedings of the workshops are published by Springer Verlag in their series of Lecture Notes in Computer Science.
LTL Conversion

Etessami's eqltl tool, for the conversion of extended LTL formulae, containing precisely one existential quantifier that we discussed in Chapter 6, can be downloaded from:

http://www.bell-labs.com/project/TMP/

The alternative converter developed by Denis Oddoux and Paul Gastin for the conversion of standard LTL formulae into PROMELA never claims is available from the SPIN Web site at:

http://spinroot.com/spin/Src/ltl2ba.tar.gz

The original package can also be obtained from the authors of this software via:

http://verif.liafa.jussieu.fr/ltl2ba/
Model Extraction

In Chapter 10 we discussed the use of a model extraction tool to facilitate the mechanical construction of SPIN verification models from implementation level code. The model extractor is available from Bell Labs via URL http://cm.bell-labs.com/cm/cs/what/modex/index.html

The distribution package includes documentation, as well as the FeaVer graphical user interface that can facilitate the use of the model extraction software.
Timeline Editor

The timeline editor tool, discussed in Chapter 13, is part of the FeaVer interface for the model extractor (see above). It can also be run as a stand-alone tool. This stand-alone version of the tool can be downloaded via URL

http://cm.bell-labs.com/cm/cs/what/timeedit/index.html
Tables and Figures

"An undetected error [...] is like a sunken rock at sea yet undiscovered, upon which it is impossible to say what wrecks may have taken place."

—(Sir John Herschel, 1842)
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