# Problem H <br> Necklace Decomposition 

source: necklace.c or necklace. cpp or necklace.java

## Description

The set of cyclic rotations of a string are the strings obtained by embedding the string clockwise on a ring, with the first character following on the last, starting at any character position and moving clockwise on the ring until the character preceeding the starting character is reached. A string is a necklace if it is the lexicographically smallest among all its cyclic rotations. For instance, for the string 01011 the cyclic rotations are ( $10110,01101,11010,10101,01011$ ), and furthermore 01011 is the smallest string and hence, a necklace.

Any string $S$ can be written in a unique way as a concatenation $S=T_{1} T_{2} \ldots T_{k}$ of necklaces $T_{i}$ such that $T_{i+1}<T_{i}$ for all $i=1, \ldots, k-1$, and $T_{i} T_{i+1}$ is not a necklace for any $i=1, \ldots, k-1$. This representation is called the necklace decomposition of the $\operatorname{string} S$, and your task is to find it.

The relation $<$ on two strings is the lexicographical order and has the usual interpretation: $A<B$ if $A$ is a proper prefix of $B$ or if $A$ is equal to $B$ in the first $j-1$ positions but smaller in the $j$ th position for some $j$. For instance, $001<0010$ and $1101011<1101100$.

## Input

On the first line of the input is a single positive integer $n$, telling the number of test scenarios to follow. Each scenario consists of one line containing a non-empty string of zeros and ones of length at most 100 .

## Output

For each scenario, output one line containing the necklace decomposition of the string. The necklaces should be written as '(' necklace ')'.

## Sample

| Input | Output |
| :--- | :--- |
| 5 | $(0)$ |
| 0 | $(0101)$ |
| 0101 | $(0001)$ |
| 0001 | $(001)(0)$ |
| 0010 | $(111)(01111)(011)$ |
| 11101111011 |  |

